First measurement of the forward-backward charge asymmetry in top quark pair production

We present the first measurement of the integrated forward-backward charge asymmetry in top-antitop quark pair ($t\bar{t}$) production in proton-antiproton ($pp$) collisions in the lepton+jets final state.
Using a 6-jet tagging algorithm and kinematic reconstruction assuming $t\bar{t}+X$ production and decay, a sample of 0.9 fb$^{-1}$ of data, collected by the D0 experiment at the Fermilab Tevatron Collider, is used to measure the asymmetry for different jet multiplicities. The result is also used to set upper limits on $t\bar{t}+X$ production via a $Z^*$ resonance.

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At lowest order in quantum chromodynamics (QCD), the standard model (SM) predicts that the kinematic distributions in $p\bar{p} \rightarrow t\bar{t} + X$ production are charge symmetric. But this symmetry is accidental, as the initial $p\bar{p}$ state is not an eigenstate of charge conjugation. Next-to-leading order (NLO) calculations predict forward-backward asymmetries of $(5–10)\%$ [1, 2], but recent next-to-next-to-leading order (NNLO) calculations predict significant corrections for $t\bar{t}$ production in association with a jet [3]. The asymmetry arises mainly from interference between contributions symmetric and antisymmetric under the exchange $t \leftrightarrow \bar{t}$ [1], and depends on the region of phase space being probed and, in particular, on the production of an additional jet [2]. The small asymmetries expected in the SM make this a sensitive probe for new physics [4].

A charge asymmetry in $p\bar{p} \rightarrow t\bar{t} + X$ can be observed as a forward-backward production asymmetry. The signed difference between the rapidities [5] of the $t$ and $\bar{t}$, $\Delta y \equiv y_t - y_{\bar{t}}$, reflects the asymmetry in $t\bar{t}$ production. We define the integrated charge asymmetry as $A_{fb} = (N_t - N_{\bar{t}}) / (N_t + N_{\bar{t}})$, where $N_t$ ($N_{\bar{t}}$) is the number of events with a positive (negative) $\Delta y$.

This Letter describes the first measurement of $A_{fb}$ in $p\bar{p} \rightarrow t\bar{t} + X$ production. The 0.9 fb$^{-1}$ data sample used was collected at $\sqrt{s} = 1.96$ TeV with the D0 detector [6], using triggers that required a jet and an electron or muon. In the lepton+jets final state of the $t\bar{t}$ system, one of the two $W$ bosons from the $t\bar{t}$ pair decays into hadronic jets and the other into leptons, yielding a signature of two $b$-jets, two light-flavor jets, an isolated lepton, and missing transverse energy ($E_T^\star$). This decay mode is well suited for this measurement, as it combines a large branching fraction ($\sim 34\%$) with high signal purity, the latter a consequence of requiring an isolated electron or muon with large transverse momentum ($p_T$). The main background is from $W+jets$ and multijet production. This channel allows accurate reconstruction of the $t$ and $\bar{t}$ directions in the collision rest frame, and the charge of the electron or muon distinguishes between the $t$ and $\bar{t}$ quarks.

The dependence of $A_{fb}$ on the region of phase space, as calculated by the MC@NLO event generator [7], is demonstrated in Fig. 1. The large dependence on the fourth-highest jet $p_T$ is not available in the calculations of Refs. [1–3], as these do not consider decays of the top quarks, and include only acceptance for jets from additional radiation.

We conclude that acceptance can strongly affect the asymmetry. To facilitate comparison with theory, the analysis is therefore designed to have an acceptance which can be described simply. Event selection is limited to either: (i) selections on directions and momenta that can be described at the particle level (which refers to produced particles before they start interacting with material in the detector) or (ii) criteria with high signal efficiency, so that their impact on the region of acceptance is negligible. In addition, the observable quantity and the fitting procedure are chosen to ensure that all events have the same weight in determining the asymmetry.

The measurement is not corrected for acceptance and reconstruction effects, but a prescription provides the acceptance at the particle level. Reconstruction effects are also accommodated at the particle level by defining the asymmetry as a function of the generated $|\Delta y|$

\[ A_{fb}(|\Delta y|) = \frac{g(\Delta y) - g(-|\Delta y|)}{g(\Delta y) + g(-|\Delta y|)} \]

where $g$ is the probability density for $\Delta y$ within the acceptance. This asymmetry can be folded with the “geometric dilution,” $D$, which is described later:

\[ A_{fb}^{\text{pred}} = \int_{0}^{\infty} A_{fb}(\Delta y) D(\Delta y) \left[ g(\Delta y) + g(-\Delta y) \right] d\Delta y. \]

This procedure yields the predictions in Table I. The values are smaller than those of Ref. [1, 2], because of the inclusion of jet acceptance and dilution.

We select events with at least four jets reconstructed using a cone algorithm [8] with an angular radius $R = 0.5$ (in rapidity and azimuthal angle). All jets must have $p_T > 20$ GeV and pseudorapidity (relative to the reconstructed primary vertex) $|\eta| < 2.5$. The leading jet must have $p_T > 35$ GeV. Events are required to have
$E_T > 15$ GeV and exactly one isolated electron with $p_T > 15$ GeV and $|\eta| < 1.1$ or one isolated muon with $p_T > 18$ GeV and $|\eta| < 2.0$. More details on lepton identification and trigger requirements are given in Ref. [9].

Events in which the lepton momentum is mismeasured by more than 2% (absolute). This is verified using several simulated samples with generated asymmetries and high impact parameter inside the jet.

The jet-$p_T$ selection criteria strongly affect the observed asymmetry (see Fig. 1), and this must be considered when comparing a model to data. Fortunately, these effects can be approximated by simple cuts on particle-level momenta without changing the asymmetry by more than 2% (absolute). This is verified using several simulated samples with generated asymmetries and particle jets clustered using the PXCONE algorithm [12] ("E" scheme and $R = 0.5$). The particle jet cuts are $p_T > 21$ GeV and $|\eta| < 2.5$, with the additional requirement on the leading particle jet $p_T > 35$ GeV and the lepton requirements detailed above. Systematic uncertainties on jet energy calibration introduce possible shifts of the particle jet thresholds. The shifts are $\pm 1.3$ GeV for the leading jet and $\pm 1.2$ GeV for the other jets, for $\pm 1$ standard deviation (sd) changes in the jet energy calibration. The resulting changes in the asymmetry predicted using MC@NLO are of the order of 0.5%. The effect of all other selections on the asymmetry is negligible. The predictions in Table I use a more complete description of the acceptance based on efficiencies factorized in $p_T$ and $\eta$, accurate to $< 1\%$ (absolute).

Misreconstructing the sign of $\Delta y$ dilutes the asymmetry. Such dilution can arise from misidentifying lepton charge or from misreconstructing event geometry. The rate for misidentification of lepton charge is taken from the signal simulation and verified using data. False production asymmetries arising from asymmetries in the rate for misidentification of lepton charge are negligible owing to the frequent reversal of the D0 solenoid and toroid polarities.

The dilution, $\mathcal{D}$, depends mainly on $|\Delta y|$. It is defined as $\mathcal{D} = 2P - 1$, where $P$ is the probability of reconstructing the correct sign of $\Delta y$. It is obtained from $t\bar{t} + X$ events generated with PYTHIA [13] and passed through a GEANT-based simulation [14] of the D0 detector, and is parametrized as:

$$\mathcal{D}(|\Delta y|) = c_0 \ln \left(1 + c_1 |\Delta y| + c_2 |\Delta y|^2\right),$$

with the parameters given in Table II (see Fig. 2).

As this measurement is integrated in $|\Delta y|$, the dependence of the dilution on $|\Delta y|$ introduces a model dependence into any correction from observed asymmetry ($A_{\text{obs}}^\text{fb}$) to a particle-level asymmetry. Such a correction factor would depend not only on the model’s $|\Delta y|$ distribution, but also on its prediction of $A_{\text{fb}}(|\Delta y|)$. Furthermore, such a correction would be sensitive to small new physics components of the selected sample. We therefore present a measurement uncorrected for reconstruction effects and provide the reader with a parametrization of $\mathcal{D}$ that describes these effects, to be applied to any model.

### Table I: Predictions based on MC@NLO.

<table>
<thead>
<tr>
<th>$N_{\text{jet}}$</th>
<th>$A_{\text{mc@nlo}}$ (in %)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\geq 4$</td>
<td>$0.8 \pm 0.2$ (stat.) $\pm 1.0$ (accept.) $\pm 0.2$ (dilution)</td>
</tr>
<tr>
<td>$4$</td>
<td>$2.3 \pm 0.2$ (stat.) $\pm 1.0$ (accept.) $\pm 0.2$ (dilution)</td>
</tr>
<tr>
<td>$\geq 5$</td>
<td>$-4.9 \pm 0.4$ (stat.) $\pm 1.0$ (accept.) $\pm 0.2$ (dilution)</td>
</tr>
</tbody>
</table>

### Table II: Parameters of the dilution. The ±1 sd values include both statistical and systematic uncertainties.

<table>
<thead>
<tr>
<th>Variation</th>
<th>$c_0$</th>
<th>$c_1$</th>
<th>$c_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_{\text{jet}} = 4$</td>
<td>0.262</td>
<td>14.6</td>
<td>-1.5</td>
</tr>
<tr>
<td>$+1$ sd variation</td>
<td>0.229</td>
<td>20.3</td>
<td>1.2</td>
</tr>
<tr>
<td>$-1$ sd variation</td>
<td>0.289</td>
<td>11.4</td>
<td>-2.2</td>
</tr>
<tr>
<td>$N_{\text{jet}} = 5$</td>
<td>0.251</td>
<td>17.6</td>
<td>-1.4</td>
</tr>
<tr>
<td>$+1$ sd variation</td>
<td>0.201</td>
<td>30.3</td>
<td>7.7</td>
</tr>
<tr>
<td>$-1$ sd variation</td>
<td>0.293</td>
<td>11.6</td>
<td>-2.3</td>
</tr>
<tr>
<td>$N_{\text{jet}} \geq 6$</td>
<td>0.254</td>
<td>9.6</td>
<td>0</td>
</tr>
<tr>
<td>$+1$ sd variation</td>
<td>0.206</td>
<td>17.4</td>
<td>2.4</td>
</tr>
<tr>
<td>$-1$ sd variation</td>
<td>0.358</td>
<td>5.0</td>
<td>-0.9</td>
</tr>
</tbody>
</table>

**FIG. 2:** The geometric dilution and its uncertainty band as a function of generated $|\Delta y|$ for standard model $t\bar{t} + X$ production and $\geq 4$ jets.
The dilution depends weakly on other variables correlated with $A_{\text{fb}}$, such as the number of jets. This possible bias is included in the systematic uncertainties. Nonstandard production mechanisms can affect reconstruction quality, primarily due to changes in the momenta of the top quarks. By studying extreme cases, we find that when comparing non-standard $t\bar{t} + X$ production to data an additional 15% relative uncertainty on $A_{\text{fb}}$ is needed.

The main background is from $W$+jets production. To estimate it, we define a likelihood discriminant $L$ using variables that are well-described in our simulation, provide separation between signal and $W$+jets background, and do not bias $|\Delta y|$ for the selected signal. The following variables are used: the $p_T$ of the leading $b$-tagged jet, the $\chi^2$ statistic from the kinematic fit, the invariant mass of the jets assigned to the hadronic $W$ boson decay, and $R_{\text{min}} = R_{\text{min}}^{\text{tag}} R_{\text{min}}^{\text{leading}}$, where $R_{\text{min}}$ is the smallest angular distance between any two jets used in the kinematic fit, and $p_T^{\text{min}}$ is the smaller of the corresponding jets’ transverse momenta.

The next largest background after $W$+jets is from multijet production, where a jet mimics an isolated electron or muon. Following the procedure described in Ref. [9], the distributions in likelihood discriminant and reconstructed asymmetry for this background are derived from samples of data that fail lepton identification. The normalization of this background is estimated from the size of those samples and the large difference in efficiencies of lepton identification for true and false leptons. The effects of additional background sources not considered explicitly in extracting $A_{\text{fb}}$, namely $Z$+jets, single top quark, and diboson production; are evaluated using ensembles of simulated datasets and found negligible.

The sample composition and $A_{\text{fb}}$ are extracted from a simultaneous maximum-likelihood fit to data of a sum of contributions to $L$ and to the sign of the reconstructed $\Delta y$ ($\Delta y_{\text{reco}}$) from forward signal, backward signal, $W$+jets, and multijet production. Both signal contributions are generated with PYTHIA, have the same distribution in $L$, and differ only in their being reconstructed as either forward or backward. The $W$+jets contribution is generated with ALPGEN [15] interfaced to PYTHIA and has its own reconstructed asymmetry. Although $W$ boson production is inherently asymmetric, the kinematic reconstruction to the $t\bar{t} + X$ hypothesis reduces its reconstructed asymmetry to $[4.4 \pm 1.6 \text{ (stat.)}] \%$. The multijet contribution is derived from data, as described above. The fitted parameters are shown in Table III. Correlations between the asymmetry and the other parameters are < 10%. The fitted asymmetries in data are consistent with the SM predictions given in Table I. In Fig. 3 we compare the fitted distributions to data for events with $\geq 4$ jets.

The dominant sources of systematic uncertainty for the measured asymmetry are the relative jet energy calibration between data and simulation ($\pm 0.5\%$), the asymmetry reconstructed in $W$+jets events ($\pm 0.4\%$), and the modeling of additional interactions during a single $p\bar{p}$ bunch crossing ($\pm 0.4\%$). The total systematic uncertainty for the asymmetry is $\pm 1\%$, which is negligible compared to the statistical uncertainty.

We check the simulation of the production asymmetry, and of the asymmetry reconstructed under the $t\bar{t} + X$ hypothesis in the $W$+jets background, by repeating the analysis in a sample enriched in $W$+jets events. The selection criteria for this sample are identical to the main analysis, except that we veto on any $b$-tags. Both the fully reconstructed asymmetry and the forward-backward lepton asymmetry are consistent with expectations. We also find that the fitted sample composition (Table III) is consistent with the cross section for $t\bar{t} + X$ production obtained in a dedicated analysis on this dataset. We check the validity of the fitting procedure, its calibration, and its statistical uncertainties using ensembles of simulated datasets.

To demonstrate the measurement’s sensitivity to new physics, we examine $t\bar{t}$ production via neutral gauge bosons ($Z'$) that are heavy enough to decay to on-shell top and antitop quarks. Direct searches have placed limits on $t\bar{t}$ production via a heavy narrow resonance [17], while the asymmetry in $t\bar{t}$ production may be sensitive to production via both narrow and wide resonances. The $Z' \rightarrow t\bar{t}$ channel is of interest in models with a “leptophobic” $Z'$ that decays dominantly to quarks. We study the scenario where the coupling between the $Z'$ boson and quarks is proportional to that between the $Z$ boson and quarks, and interference effects with SM $t\bar{t}$ production are negligible. Using PYTHIA we simulate $t\bar{t}$ production via $Z'$ resonances with decay rates chosen to yield narrow resonances as in Ref. [17], and find large positive asymmetries [(13–35)\%], which are a consequence of the predominantly left-handed decays. We predict the distribution of $A_{\text{fb}}$ as a function of the fraction $(f)$ of $t\bar{t}$ events produced via a $Z'$ resonance of a particular mass from ensembles of simulated datasets. We use the procedure of Ref. [18] to arrive at the limits shown in Fig. 4. These limits can be applied to wide $Z'$ resonances by averaging over the distribution of $Z'$ mass.

In summary, we present the first measurement of the integrated forward-backward charge asymmetry in $t\bar{t} + X$ production. We find that acceptance affects the asymmetry and must be specified as above, and that correc-

<table>
<thead>
<tr>
<th>No. Events</th>
<th>$\geq 4$ Jets</th>
<th>4 Jets</th>
<th>$\geq 5$ Jets</th>
</tr>
</thead>
<tbody>
<tr>
<td>$t\bar{t} + X$</td>
<td>266 $^{+22}_{-21}$</td>
<td>214 $^{+20}_{-20}$</td>
<td>54 $^{+19}_{-12}$</td>
</tr>
<tr>
<td>$W$+jets</td>
<td>70 $^{+21}_{-21}$</td>
<td>61 $^{+18}_{-18}$</td>
<td>7 $^{+5}_{-5}$</td>
</tr>
<tr>
<td>Multijets</td>
<td>40 $^{+4}_{-4}$</td>
<td>32 $^{+3.5}_{-3.5}$</td>
<td>7.1 $^{+1.6}_{-1.6}$</td>
</tr>
<tr>
<td>$A_{\text{fb}}$</td>
<td>$(12\pm8)%$</td>
<td>$(19\pm9)%$</td>
<td>$(-16\pm15)%$</td>
</tr>
</tbody>
</table>
resonance are shown by the dashed curve, with the shaded bands showing limits one and two standard deviations away. Limits expected in the absence of a $Z'$ resonance as a function of the $Z'$ mass, under assumptions detailed in the text. Limits expected in the absence of a $Z'$ resonance are shown by the dashed curve, with the shaded bands showing limits one and two standard deviations away. The observed limits are shown by the solid curve, and the excluded region is hatched.

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FIG. 4: 95% C.L. limits on the fraction of $t\bar{t}$ produced via a $Z'$ resonance as a function of the $Z'$ mass, under assumptions detailed in the text. Limits expected in the absence of a $Z'$ resonance are shown by the dashed curve, with the shaded bands showing limits one and two standard deviations away. The observed limits are shown by the solid curve, and the excluded region is hatched.

tions for reconstruction effects are too model-dependent to be of use. We observe an uncorrected asymmetry of $A_{\text{obs}}^{t\bar{t}} = [12 \pm 8 \text{ (stat.)} \pm 1 \text{ (syst.)}]\%$ for $t\bar{t} + X$ events with $\geq 4$ jets that are within our acceptance, and we provide a dilution function (Eq. 3) that can be applied to any model (through Eq. 2). For events with only four jets and for those with $\geq 5$ jets, we find $A_{\text{obs}}^{t\bar{t}} = [19 \pm 9 \text{ (stat.)} \pm 2 \text{ (syst.)}]\%$ and $A_{\text{obs}}^{t\bar{t}} = [-16^{+11}_{-12} \text{ (stat.)} \pm 3 \text{ (syst.)}]\%$, respectively, where most of the systematic uncertainty is from migrations of events between the two subsamples. The measured asymmetries are consistent with the MC@NLO predictions for standard model production.

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[5] Rapidity $y$ and pseudorapidity $\eta$ are defined as functions of the polar angle $\theta$ as $y(\theta, \beta) \equiv \frac{1}{2} \ln [(1 + \beta \cos \theta)/(1 - \beta \cos \theta)]; \eta(\theta) \equiv y(\theta, 1)$. where $\beta$ is the ratio of a particle's momentum to its energy.
[9] V.M. Abazov et al. (D0 Collaboration), Phys. Rev. D


