

# Forward Jet Production in DIS at HERA



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Workshop on Low-x Physics  
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## Outline

- DIS Events at HERA
- QCD Dynamics at low  $x$
- NLO QCD Calculations & MC Models
- Inclusive Forward Jet Measurements
  - Conclusions

Forward Jet Production in deep inelastic scattering and low- $x$  parton dynamics at HERA

[DESY-05-017](#)  
hep-ex/0502029



# DIS Events at HERA



$$\sqrt{s} = \sqrt{4E_e E_p} \cong 300 \text{ (320) GeV}$$

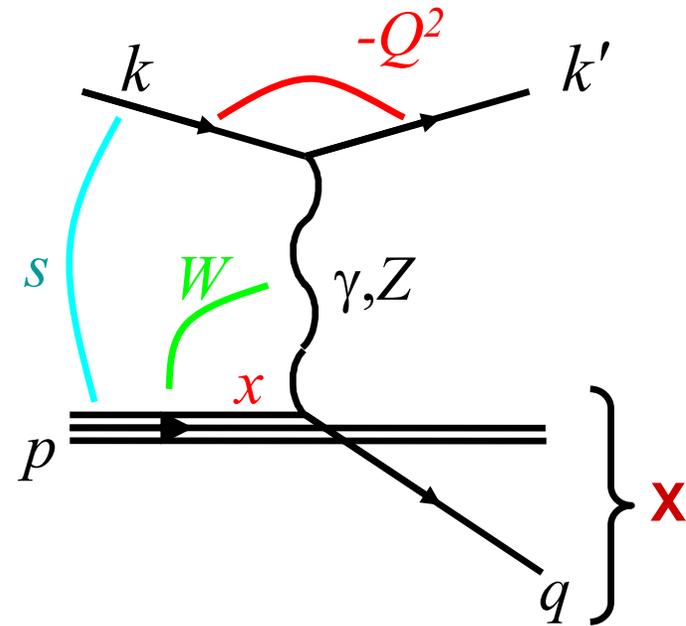
The Lorentz invariant kinematic variables to describe DIS are;

$$Q^2 = -q^2 = (k - k')^2$$

$$Q^2 \cong sxy$$

$$x = \frac{Q^2}{2(P \cdot q)} \quad 0 \leq x \leq 1$$

$$y = \frac{(P \cdot q)}{(P \cdot k)} \quad 0 \leq y \leq 1$$



$s$ : e-p c.m. energy

$Q^2 = -q^2$ : 4-momentum transfer squared

$x$ : fraction of proton momentum carried by struck quark

$y$ : inelasticity parameter

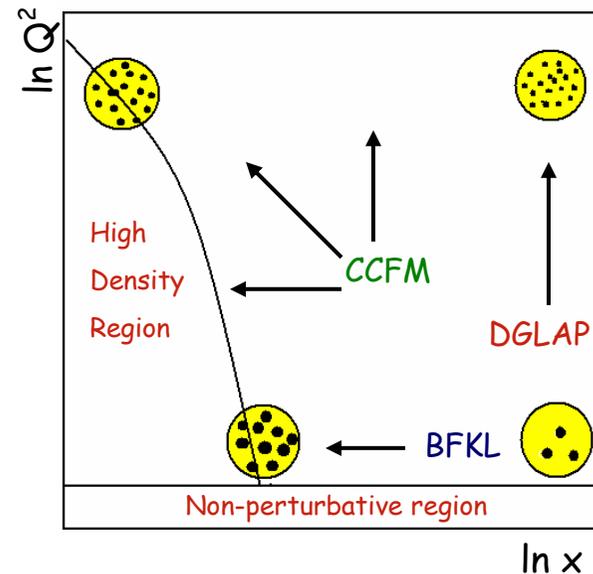
$W$ :  $\gamma$ -p c.m. energy

Jet/particle production has been successfully described by DGLAP at high scales ( $Q^2$ )

★ **DGLAP: strong  $k_T$  ordering**

$$\alpha_s(Q^2) \ln(Q^2), \quad \alpha_s(Q^2) \ln \frac{1}{x} \approx 1$$

- DGLAP is expected to break down at low scales and low x
- This break down might be observed in forward jet production at HERA

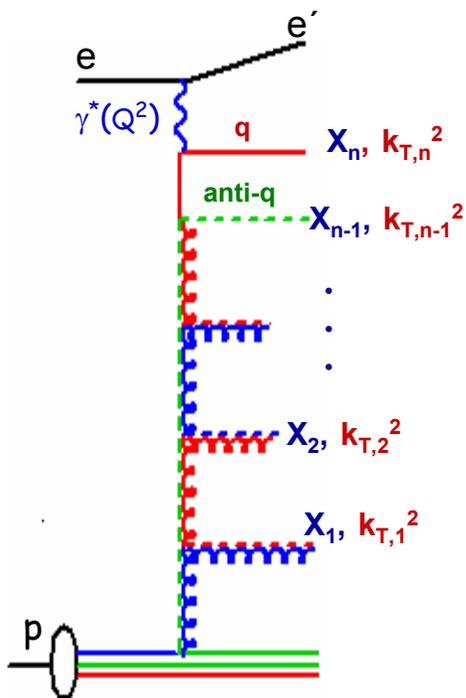


Other approaches to explain parton dynamics at low x :

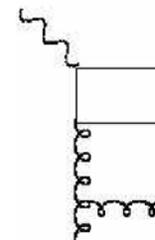
★ **BFKL: no  $k_T$  ordering, ordering in x**  
Applicable at very low-x

$$\alpha_s(Q^2) \ln(Q^2) \approx 1, \quad \alpha_s(Q^2) \ln \frac{1}{x}$$

★ **CCFM: un-integrated PDFs Angular ordering**

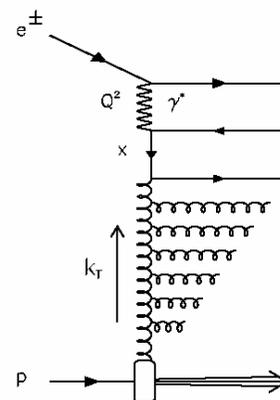


**DISENT:** Fixed order QCD partonic cross section, on mass shell  
 ME + DGLAP , needs to be corrected to hadron level



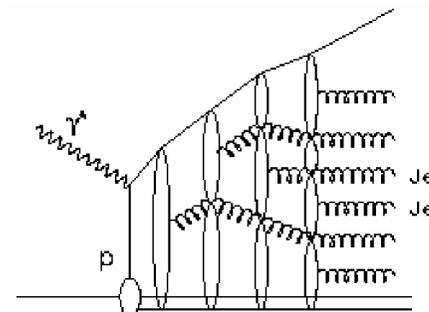
**LEPTO:** LO ME+PS , (DGLAP)

→ Strong ordering in  $k_T$



**ARIADNE:** LO, an implementation of Color Dipole Model (CDM)

- Independently radiating dipoles formed by emitted gluons
- Random walk in  $k_T$
- BFKL-like





**CASCADE**: LO off mass shell ME + PS based on  $k_T$  factorized CCFM evolution model

→ angular ordering in parton emission

$k_{\perp}$  is transverse momentum of emitted gluon  $k_{\perp} > k_{\perp}^{\text{cut}}$

CASCADE set1 :

$$k_{\perp}^{\text{cut}} = 1.33 \text{ GeV}$$

CASCADE set2 :

$$k_{\perp}^{\text{cut}} = 1.18 \text{ GeV}$$

Non-singular terms in CCFM splitting function are also included

All MC models described here use LUND string fragmentation model for hadronization !

## Kinematic range

96-97 Data,  $L \approx 38 \text{ pb}^{-1}$

$$Q^2 > 25 \text{ GeV}^2$$

No restriction for  $x_{Bj}$

$$y > 0.04$$

## Forward Jet selection

Jet Finding with Inclusive  $K_T$  Algorithm in Lab Frame

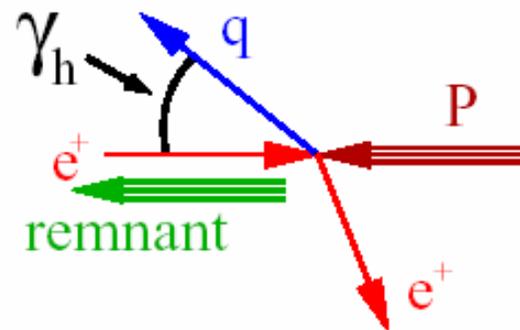
## Global phase space

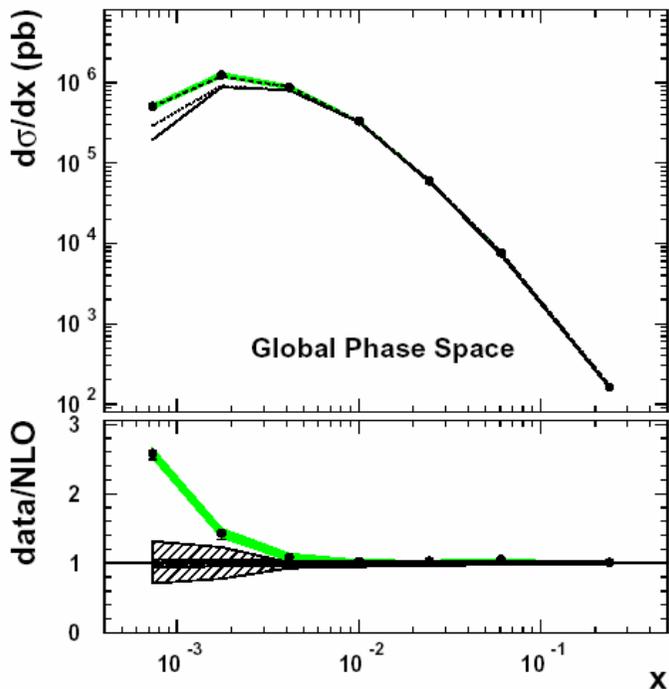
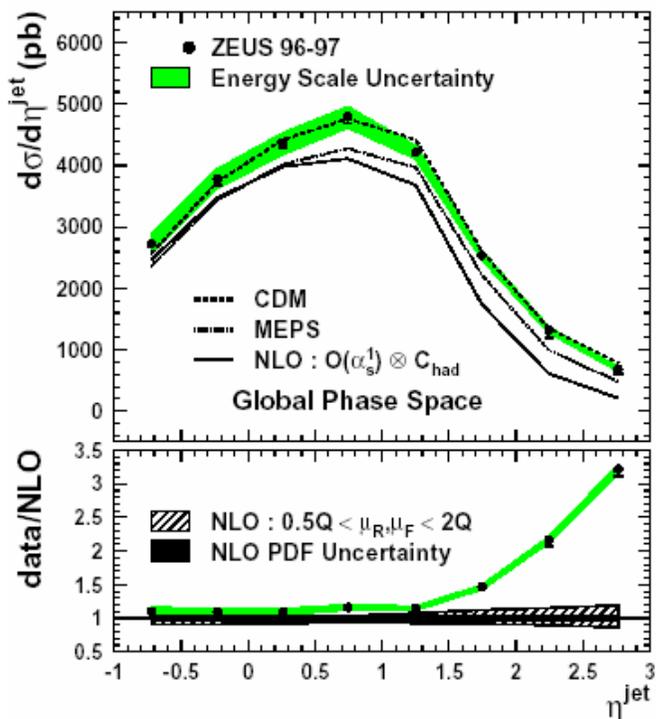
$$E_{T,jet} > 6 \text{ GeV}$$

$$-1 < \eta^{jet} < 3$$

$$\eta = -\log(\tan(\theta/2))$$

Single jet events (QPM) dominant





$$\begin{aligned}
 V^* q &\rightarrow q && \text{QPM} \\
 V^* g &\rightarrow q \bar{q} && \text{BGF} \\
 V^* q &\rightarrow q g && \text{QCDC}
 \end{aligned}$$

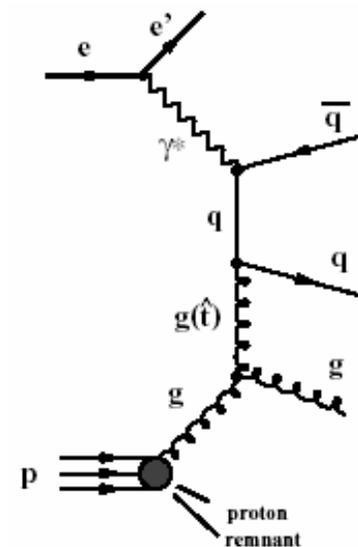
NLO calculations with  $\mu_r^2 = \mu_f^2 = Q^2$ , CTEQ6  
 Corrected to hadron level

CDM is in good agreement with data everywhere.

LEPTO (DGLAP) slightly lower than data but doing good for high x region

Fixed-order QCD calculations describe well low  $\eta$  and high x, BUT lower than data at low-x and in forward region,

Scale variations can not reflect the contributions from gluon exchange in *t*-channel which appear only in the higher orders . . .



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## BFKL phase space

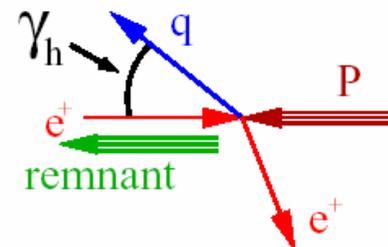
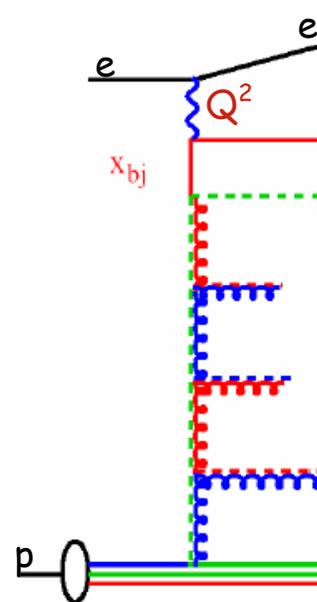
$$E_{T,\text{jet}} > 6 \text{ GeV}$$

$$0.5 < E_{T,\text{jet}}^2 / Q^2 < 2$$

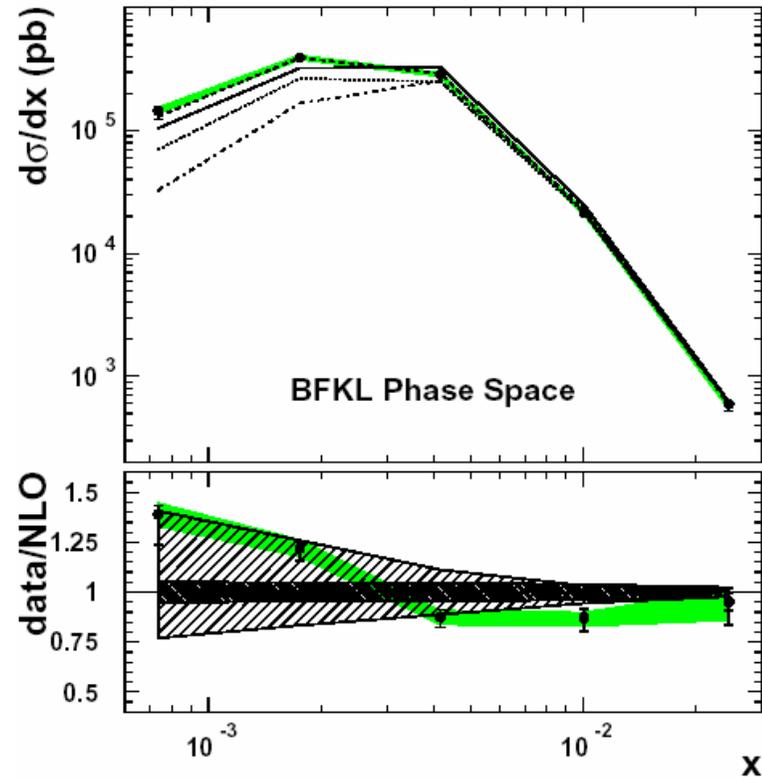
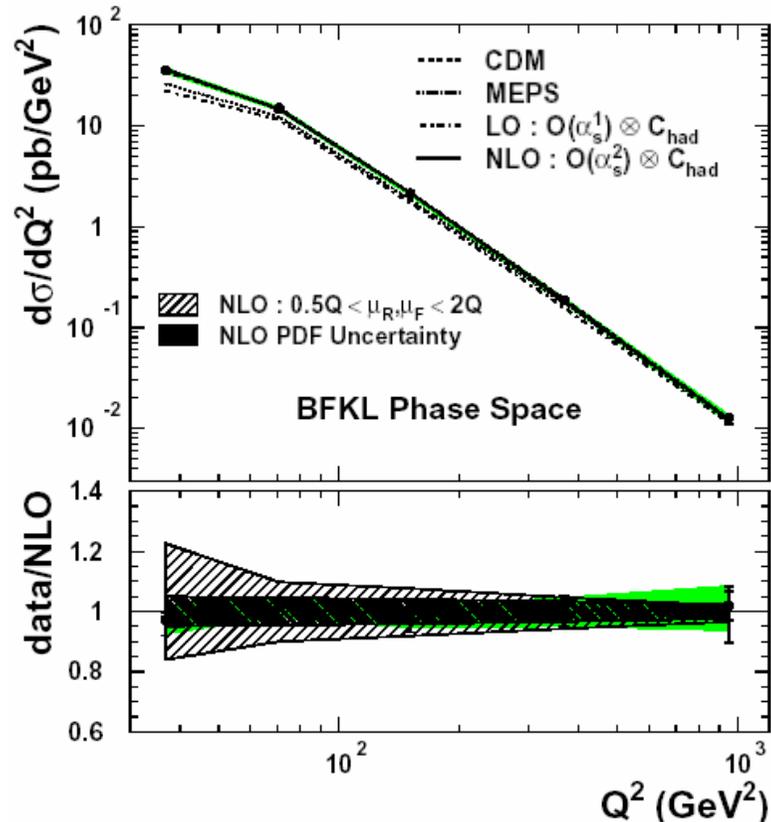
$$0 < \eta^{\text{jet}} < 3$$

$\cos \gamma_{\text{had}} < 0$  Suppresses QPM

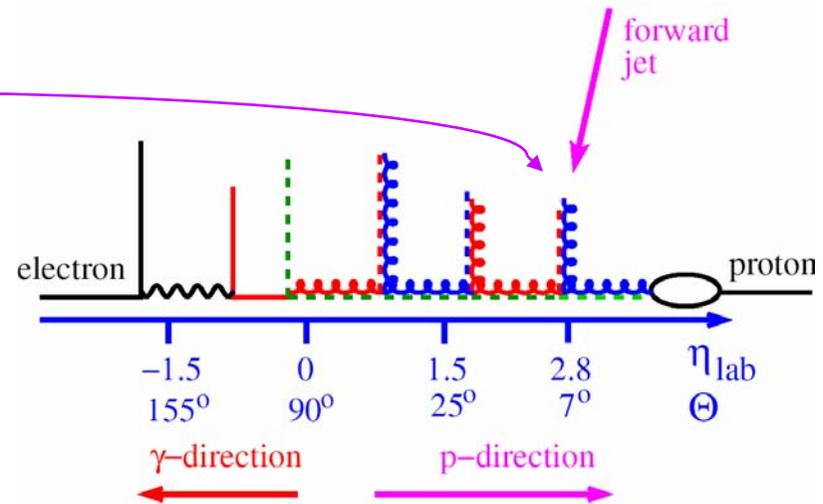
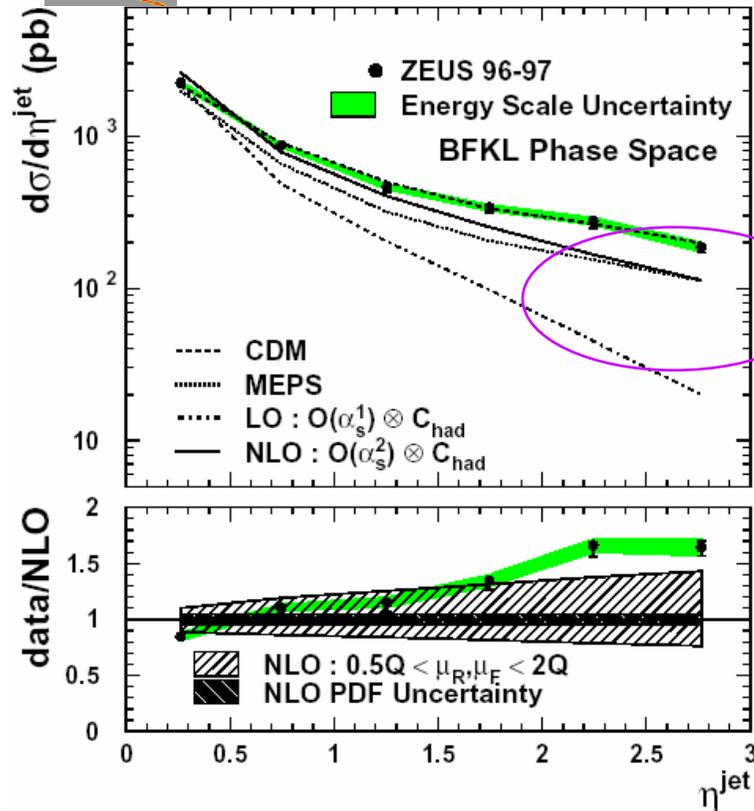
gluon exchange in t-channel is expected to be dominant



$$\cos \gamma = \frac{(\sum_i p_{x,i})^2 + (\sum_i p_{y,i})^2 - (\sum_i (E - p_z)_i)^2}{(\sum_i p_{x,i})^2 + (\sum_i p_{y,i})^2 + (\sum_i (E - p_z)_i)^2}$$



- CDM describes both measured cross sections
- ME+PS:LEPTO (DGLAP) fails for low  $x_{Bj}$  and  $Q^2$
- NLO calculations give a good description of  $Q^2$  dependence
- From LO:  $O(\alpha_s^1)$  to NLO:  $O(\alpha_s^2)$  brings NLO prediction closer to data at low- $x$ , since in this case gluon exchange in t-channel is included



- Large increase of cross sections from  $O(\alpha_s^1)$  to NLO:  $O(\alpha_s^2)$  associated with the contribution from t-channel gluon exchange diagrams
- Discrepancy between data and NLO in the forward region  $\eta^{jet} > 1.5$ , this region is more sensitive to higher order radiations (estimation of uncertainty from higher orders is large)
- CDM describes well measured cross section
- ME+PS:LEPTO (DGLAP) fails in all  $\eta^{jet}$  range

## Kinematical range

98-00 Data,  $L \cong 82 \text{ pb}^{-1}$

$$20 < Q^2 < 100 \text{ GeV}^2$$

$$0.0004 < x_{Bj} < 0.005$$

$$0.04 < y < 0.7$$

## Forward Jet selection

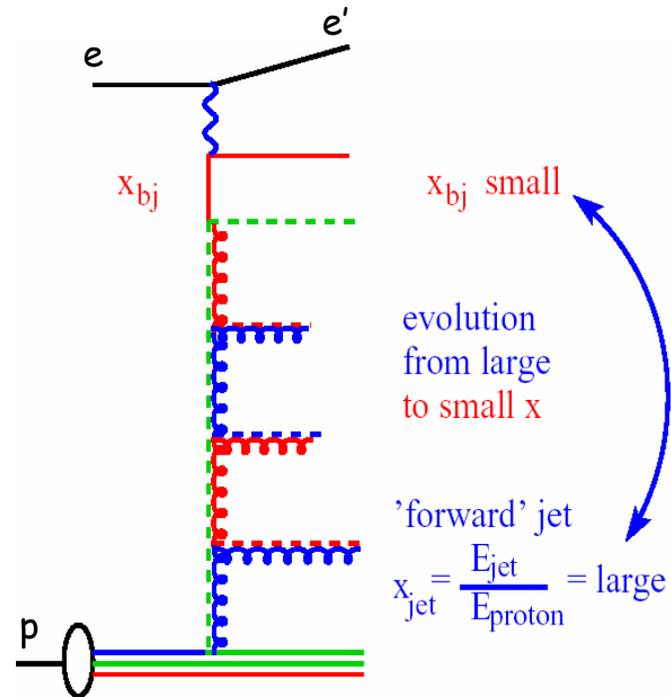
Jet Finding with Inclusive  $K_T$   
Algorithm in Breit Frame

$$E_{T,jet} > 5 \text{ GeV}$$

$$0.5 < E_{T,jet}^2 / Q^2 < 2$$

$$x_{jet} > 0.036$$

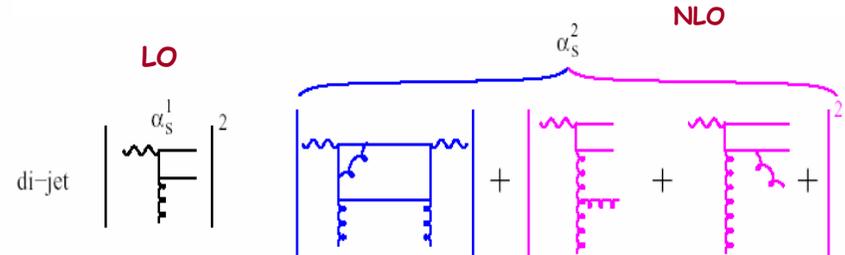
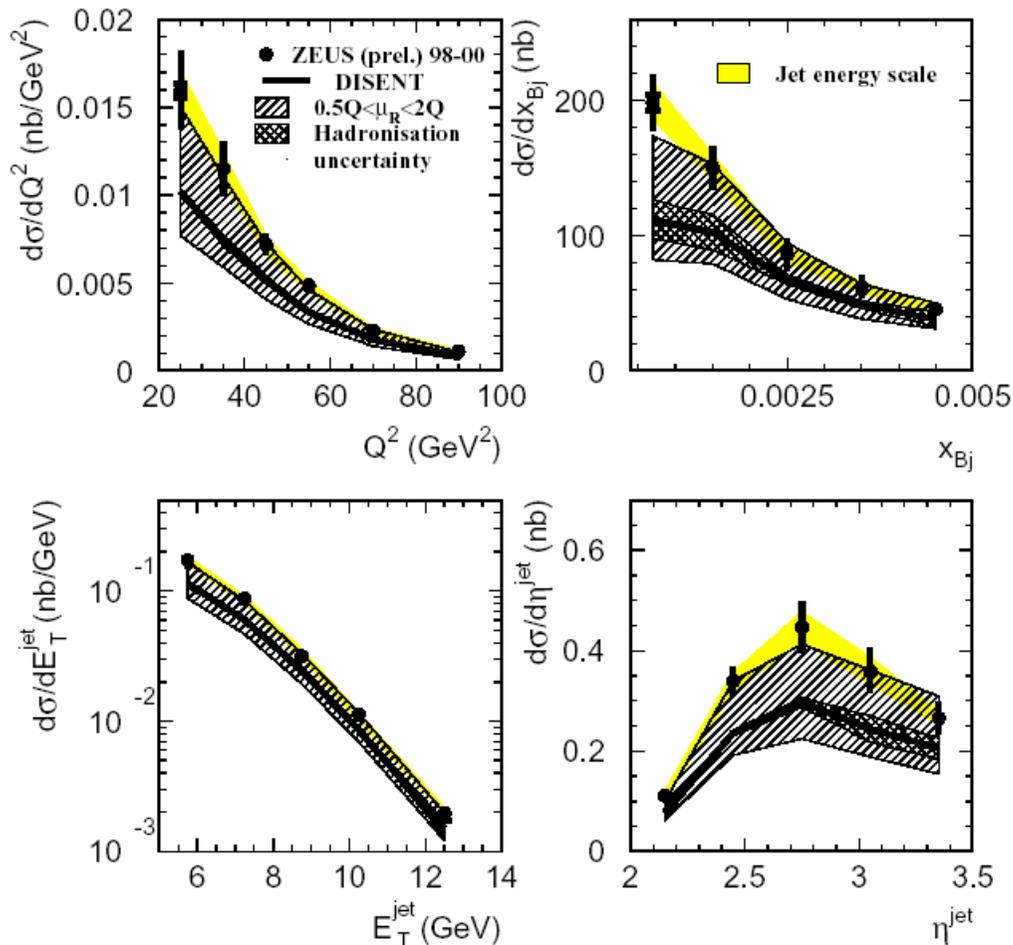
$$2 < \eta^{jet} < 3.5$$



$E_{T,jet}^2 \sim Q^2$  suppress DGLAP evolution

$x_{jet} = E_{jet} / E_{proton} \gg x_{Bj}$  enhances BFKL effect

## ZEUS



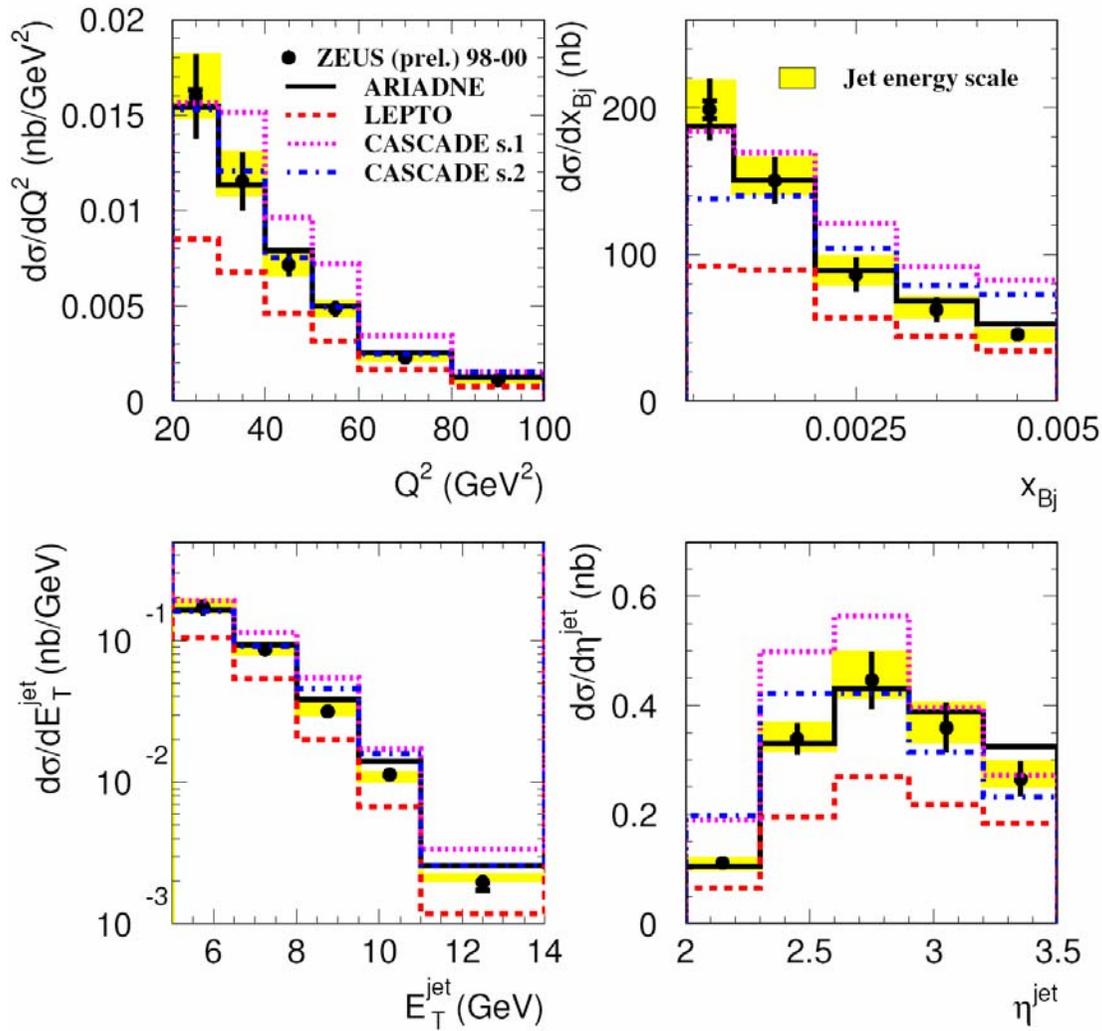
$$\mu_R^2 = \mu_f^2 = Q^2$$

corrected to hadron level

Proton PDF: CTEQ5D

- NLO predictions tend to be below data, however it is within the thr. unc.
- Size of theoretical uncertainties in this phase space region, prevents us to make decisive conclusions

## ZEUS



Look more forward region  
 $2 < \eta^{\text{jet}} < 3.5$

- LEPTO:DGLAP describes the shape but not the normalization ( fails by a factor of  $\sim 2$ )
  - CCFM set1 disagrees with all cross sections
  - CCFM set2 in good agreement with data in  $Q^2$  and  $E_T$  but fails to reproduce the shapes of  $x_{Bj}$  and  $\eta^{\text{jet}}$
  - CDM gives a good description of data in all measured cross sections
- } BFKL-like



# Conclusions

- ✓ Parton dynamics at low- $x$  studied in forward jet production in DIS by ZEUS coll.
- ✓ Lowest-order DGLAP (LEPTO) calculations fail to describe forward jet cross sections
- ✓ NLO calculations predict lower cross sections at low Bjorken- $x$  and for very forward region, the theoretical uncertainty is large in this phase space, indicating that higher order corrections are needed
- ✓ Models beyond DGLAP evolution (CCFM, BFKL) look promising in describing parton dynamics at low  $x$  , NLO calculations based on BFKL & CCFM needed.
- ✓ Forward jet measurements can provide constraint on Un-integrated Gluon Densities

Any idea of a new measurement to search for a BFKL signature is welcome !!!!