

# Top Quark Mass in Lepton+Jets Decays at the Tevatron

**Christian Schwanenberger**

University of Manchester



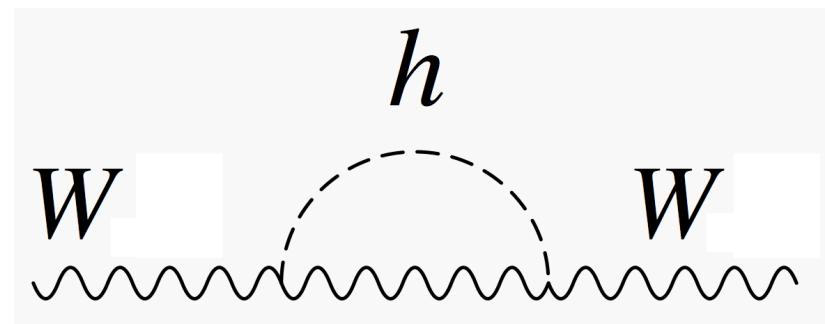
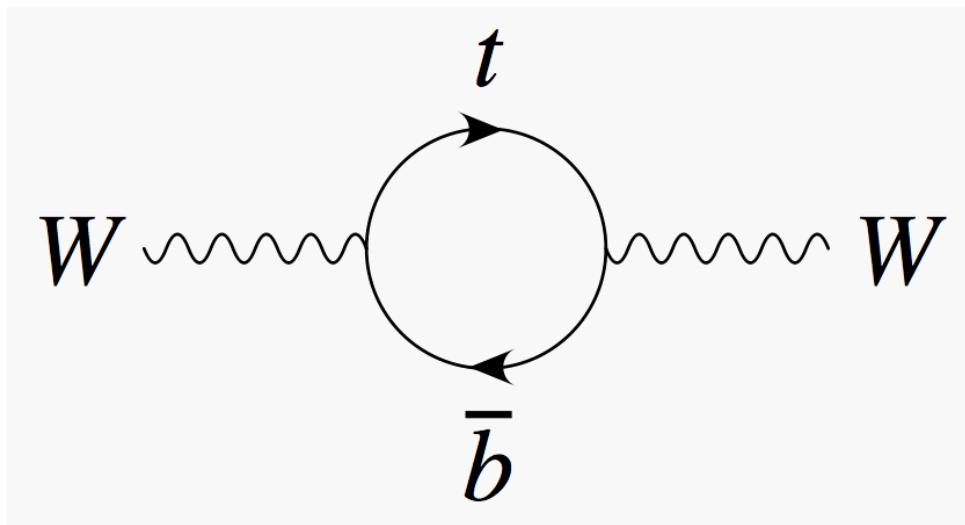
on behalf of



**ICHEP 2008, Philadelphia, 07/30/2008**

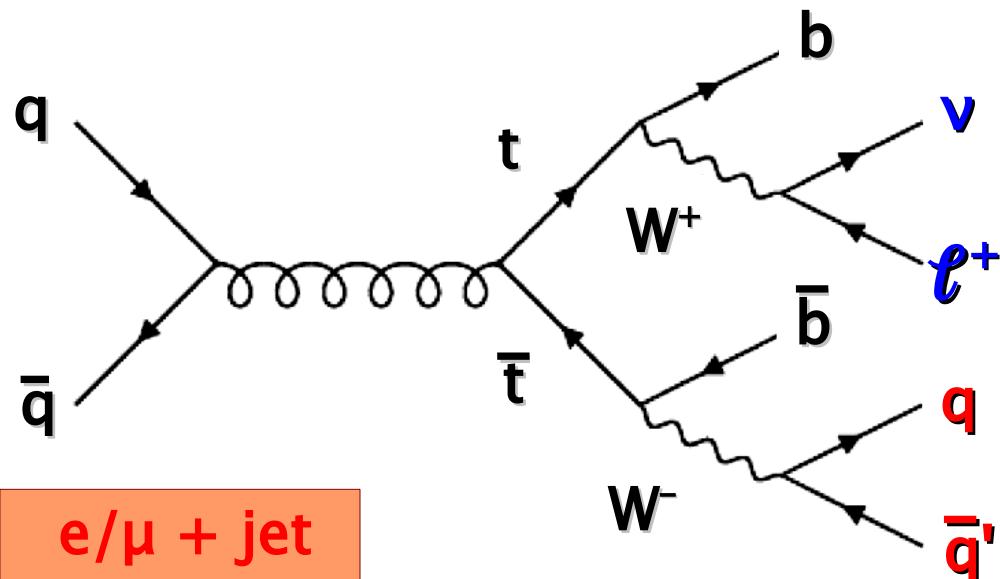
# The Top Quark Mass

- free parameter in the Standard Model
- check the self-consistency of the Standard Model in combination with W mass measurement

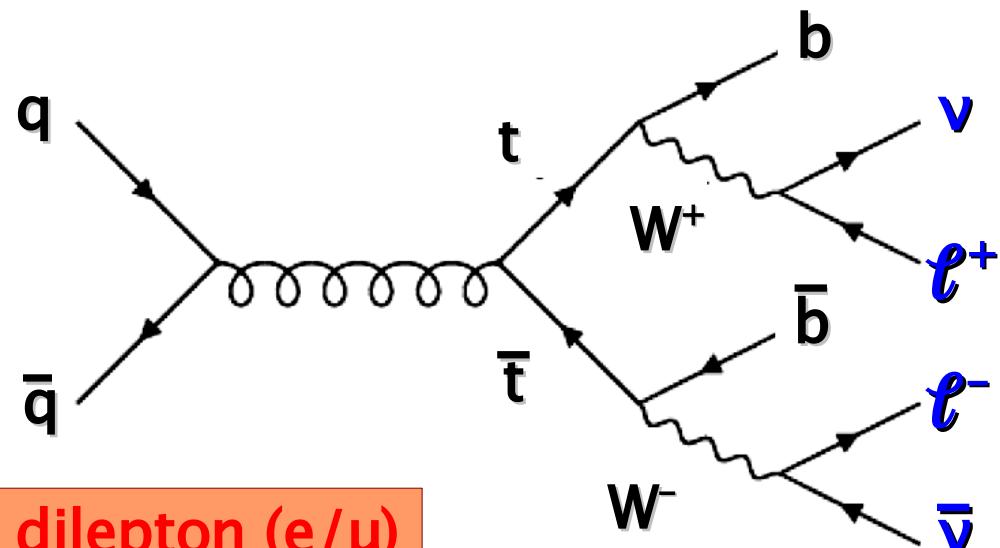


# Top anti-top signatures

**signal**



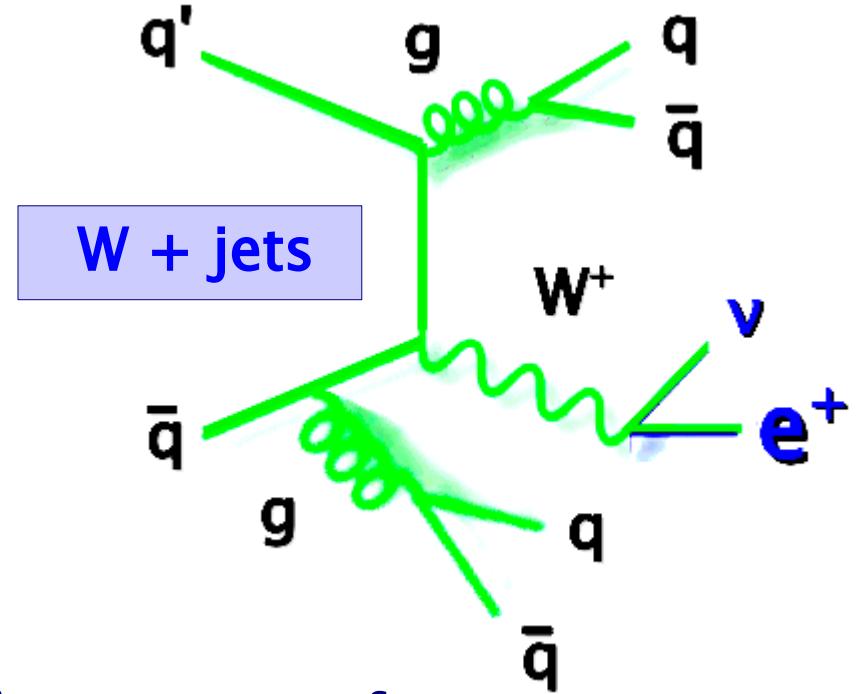
$e/\mu + \text{jet}$



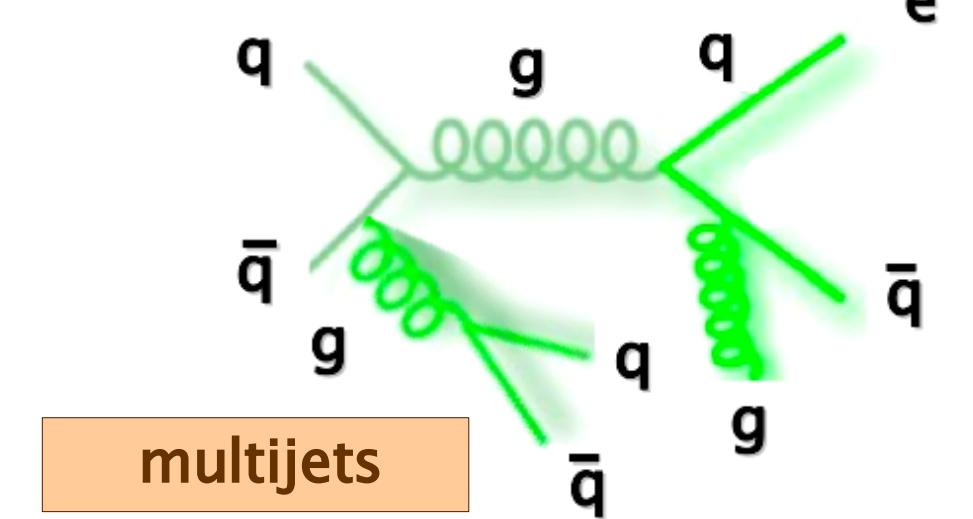
dilepton ( $e/\mu$ )

3000 times more often

**background**



$10^{10}$  times more often



multijets

# Outline

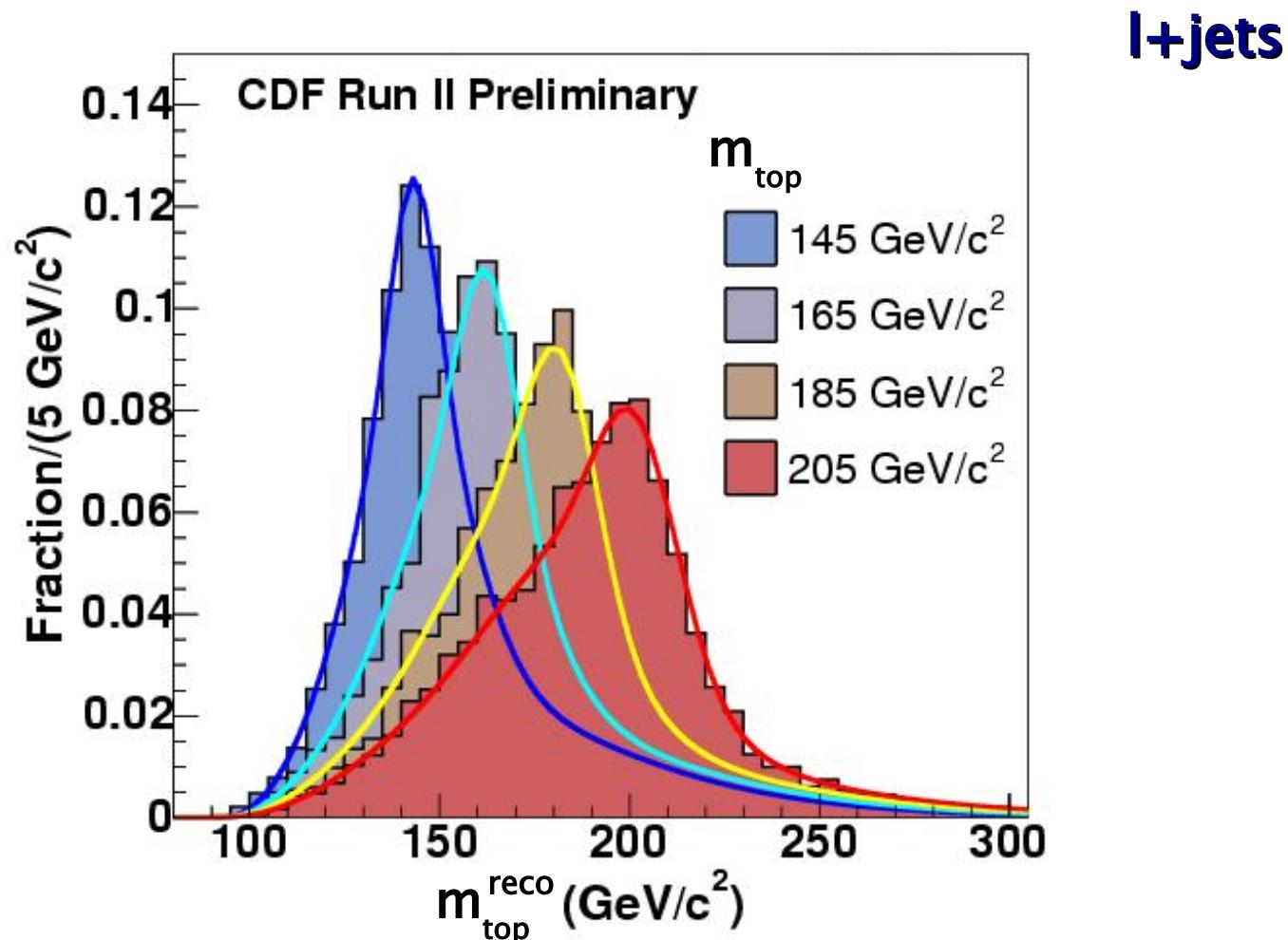
**Templates  
Matrix Elements  
Cross Section  
Summary**

# Outline

**Templates**  
**Matrix Elements**  
**Cross Section**  
**Summary**

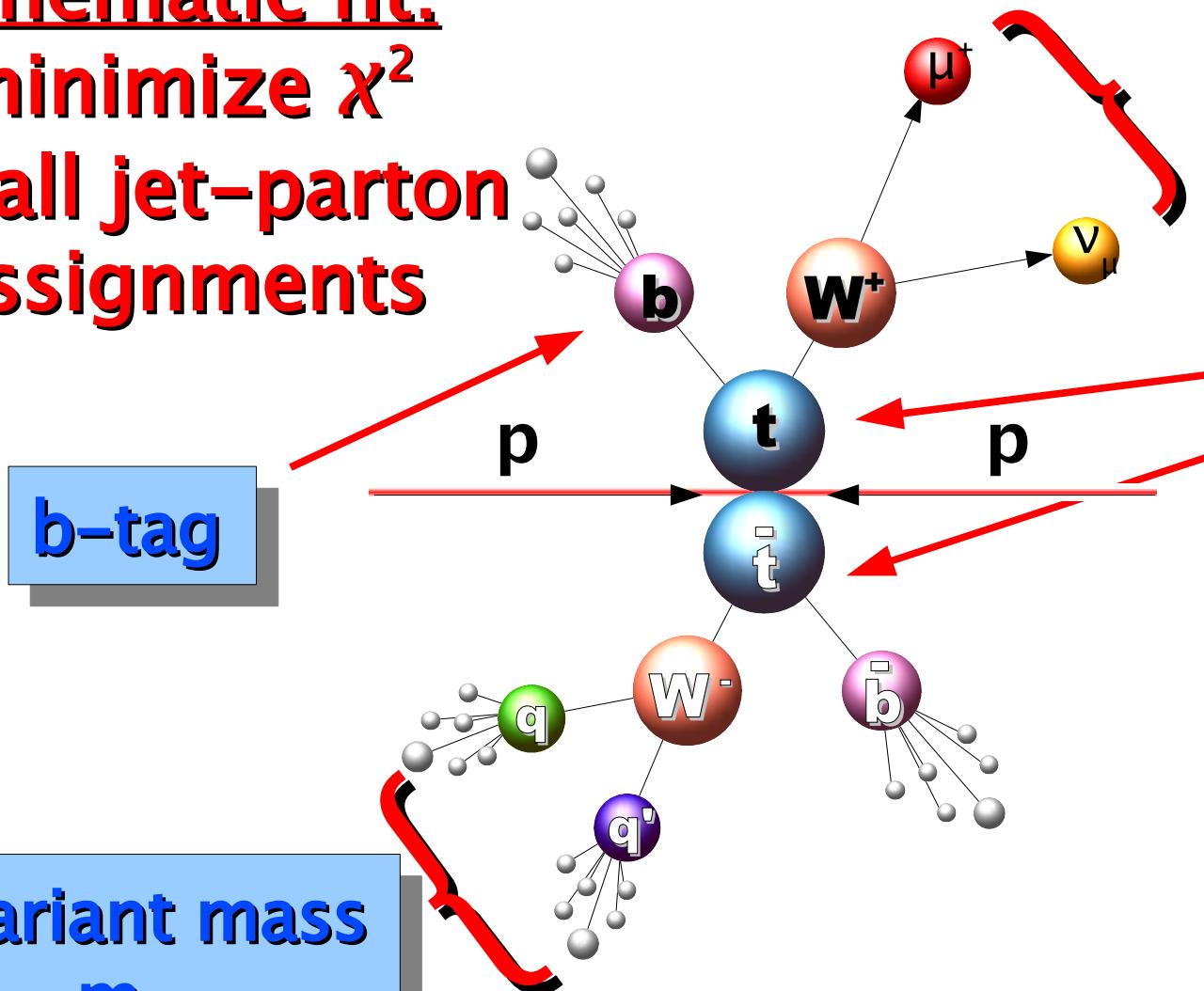
# Extraction techniques: template method

- use variables strongly correlated with  $m_{\text{top}}$
- compare data to MC with different  $m_{\text{top}}$  hypotheses



# Top mass reconstruction

constrained  
kinematic fit:  
minimize  $\chi^2$   
for all jet-parton  
assignments



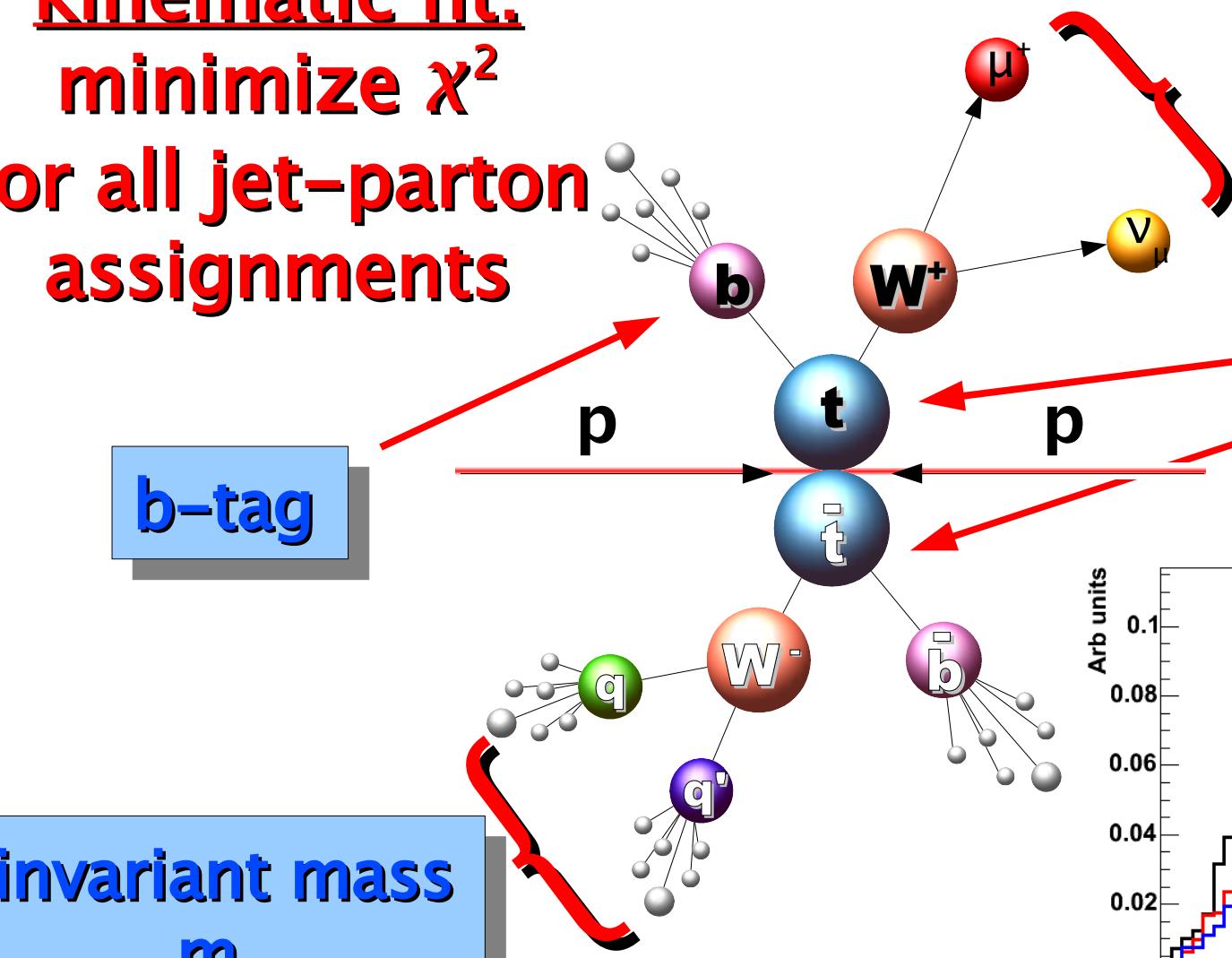
invariant mass  
 $m_W$   
(2 v solutions)

$m_{\text{top}} = m_{\text{anti-top}}$

invariant mass  
 $m_W$

# Top mass reconstruction

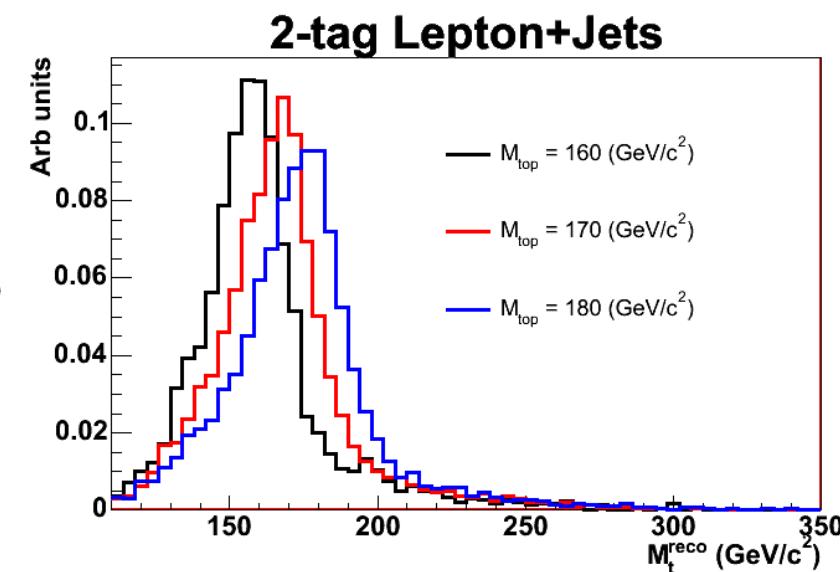
constrained  
kinematic fit:  
minimize  $\chi^2$   
for all jet-parton  
assignments



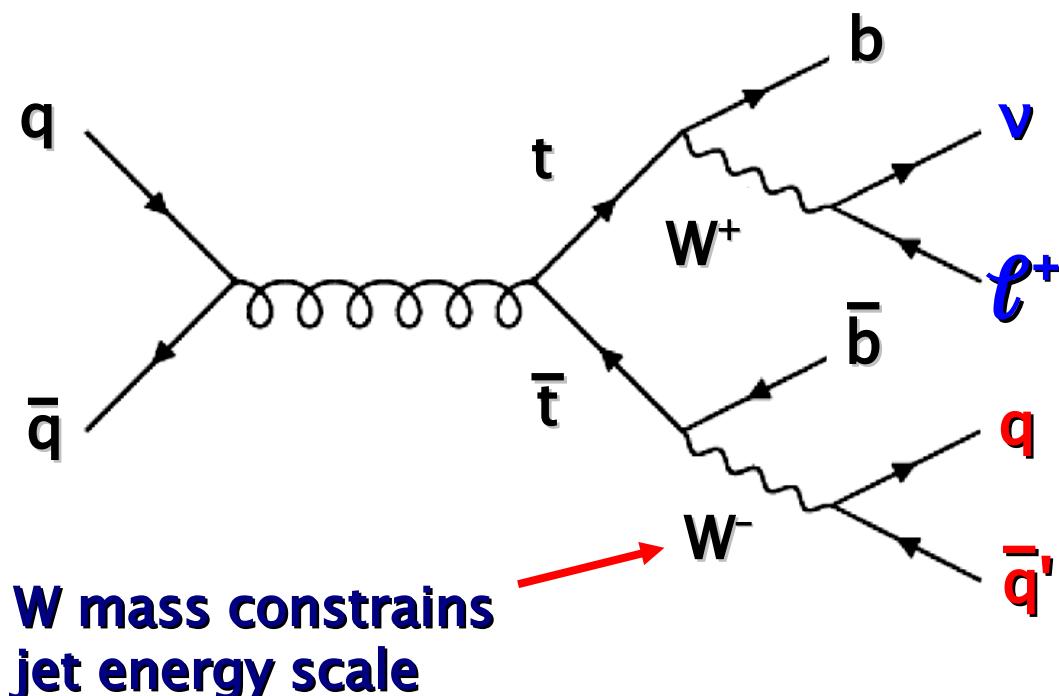
invariant mass  
 $m_W$   
(2 v solutions)

$$m_{\text{top}} = m_{\text{anti-top}}$$

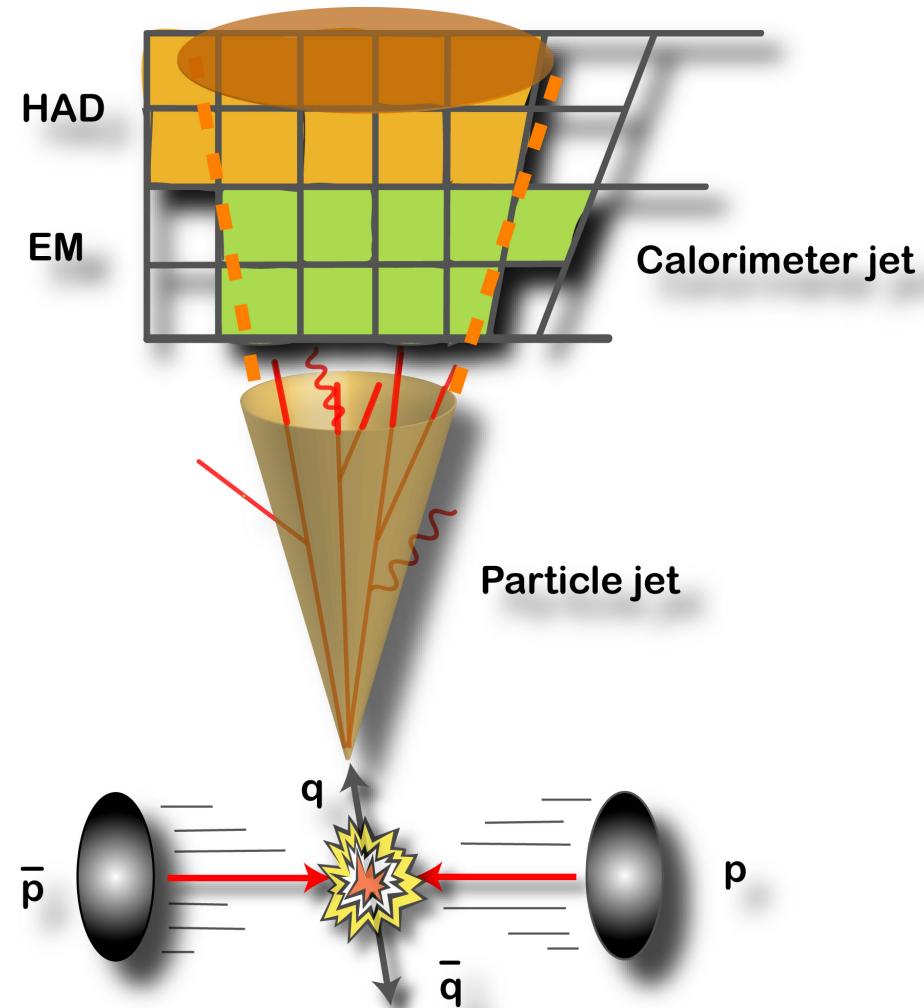
invariant mass  
 $m_W$



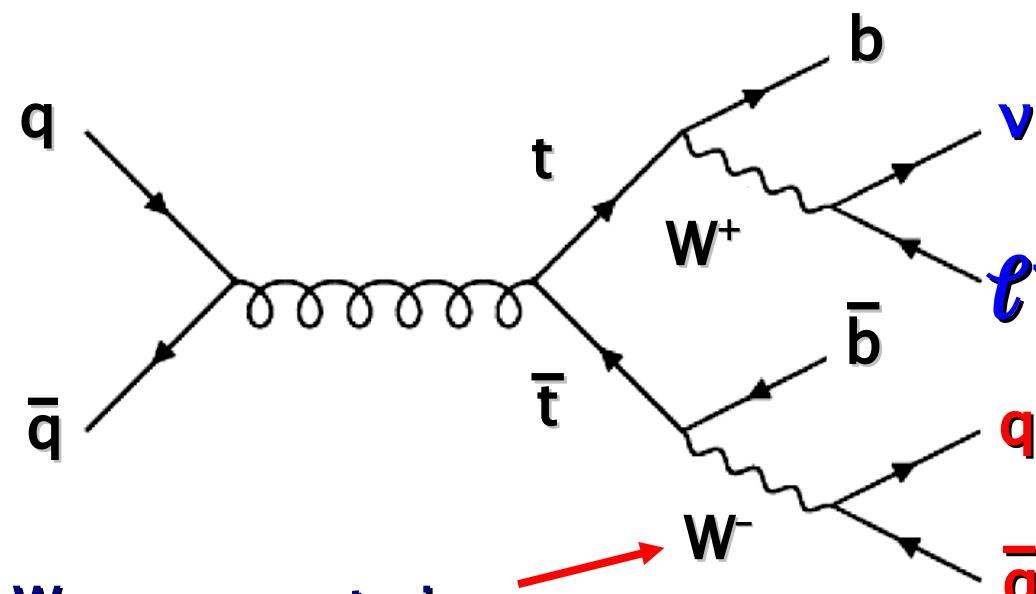
# Main systematics: jet energy scale



jet energy scale:  
translate jet into parton energy

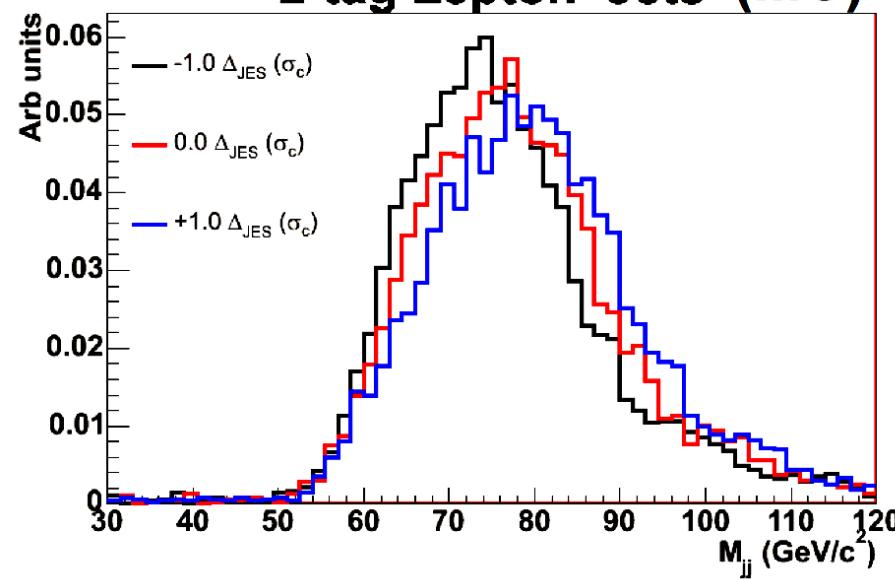


# Main systematics: jet energy scale

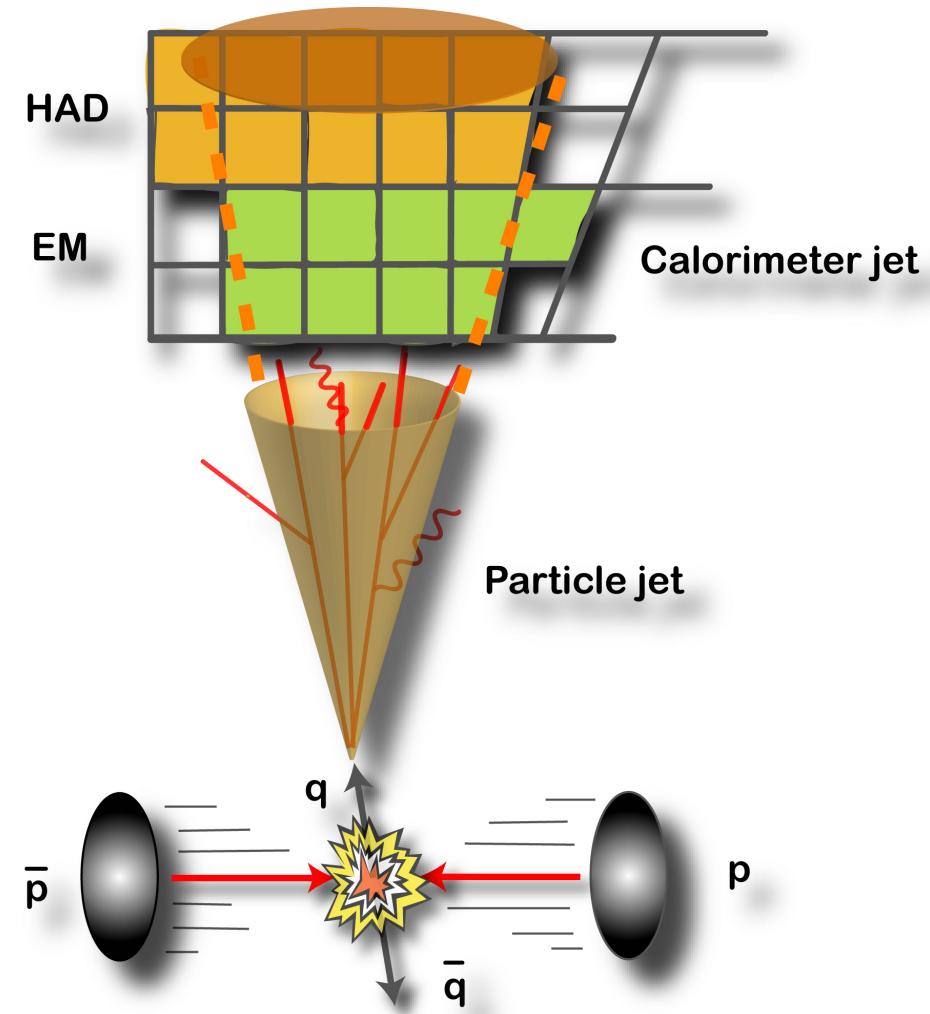


**W mass constrains  
jet energy scale**

**2-tag Lepton+Jets (MC)**



**jet energy scale:  
translate jet into parton energy**

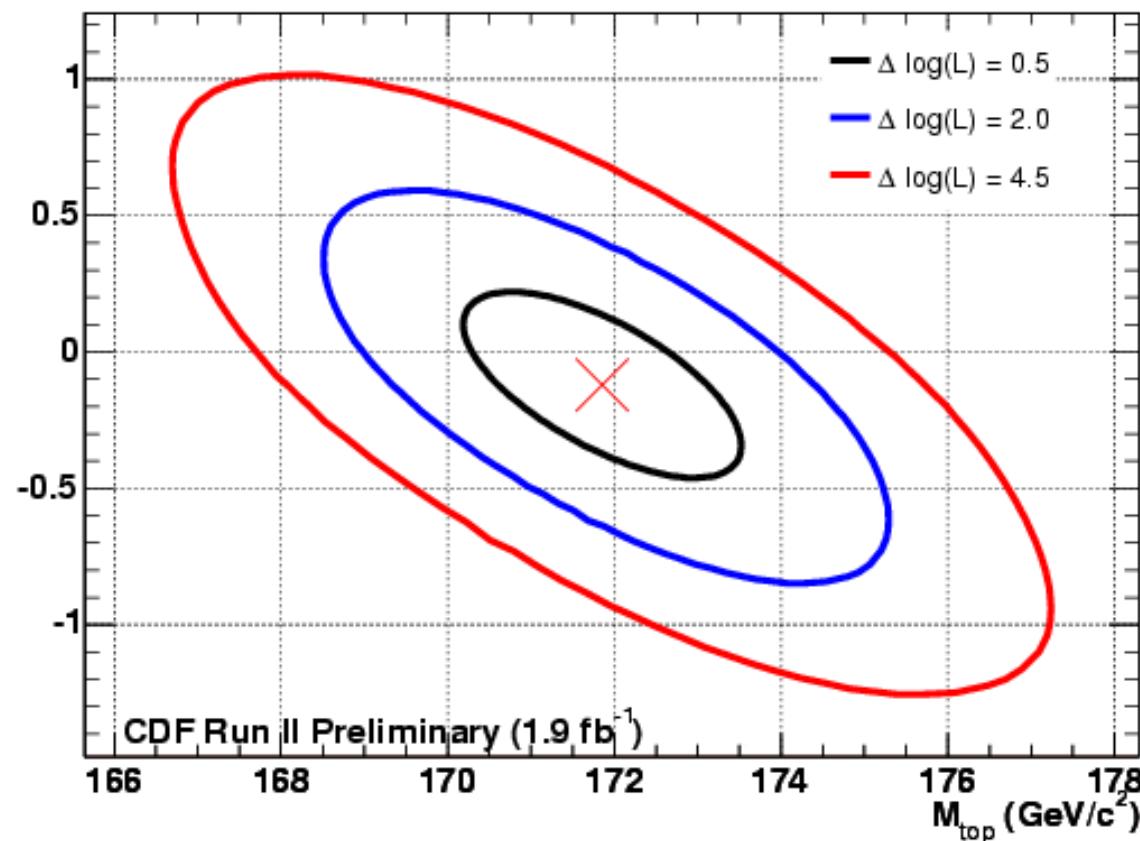


# Results

1.9 fb<sup>-1</sup>

- Probability density functions with Kernel Density Estimates
- maximum Likelihood fit using signal and background pdfs

$\Delta$  jet  
energy  
scale



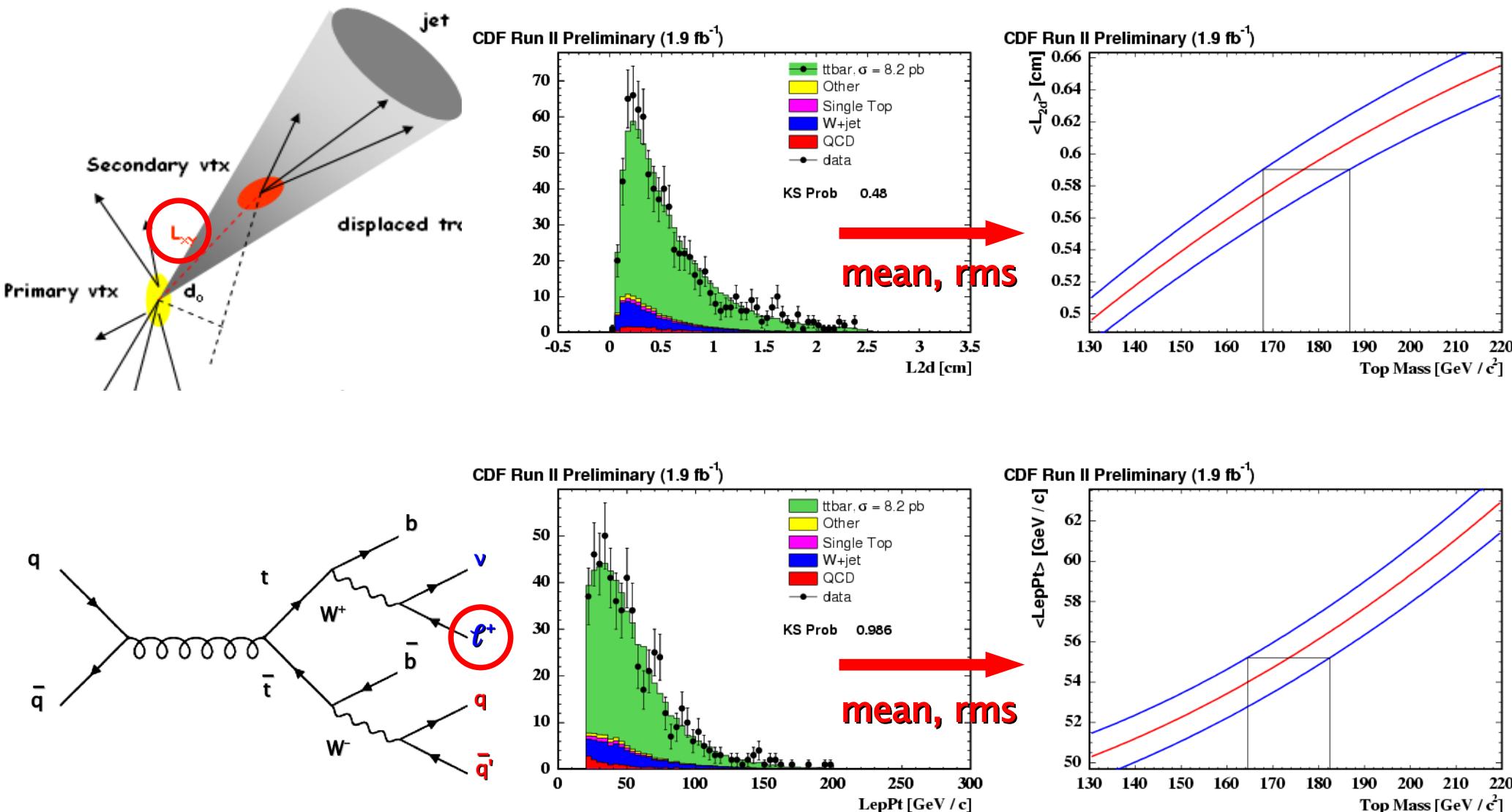
- l+jets/dilepton combined



$$m_{\text{top}} = 171.9 \pm 1.7 \text{ (stat+JES)} \pm 1.0 \text{ (syst)} \text{ GeV} \quad \pm 1.1\%$$

# Alternative template method

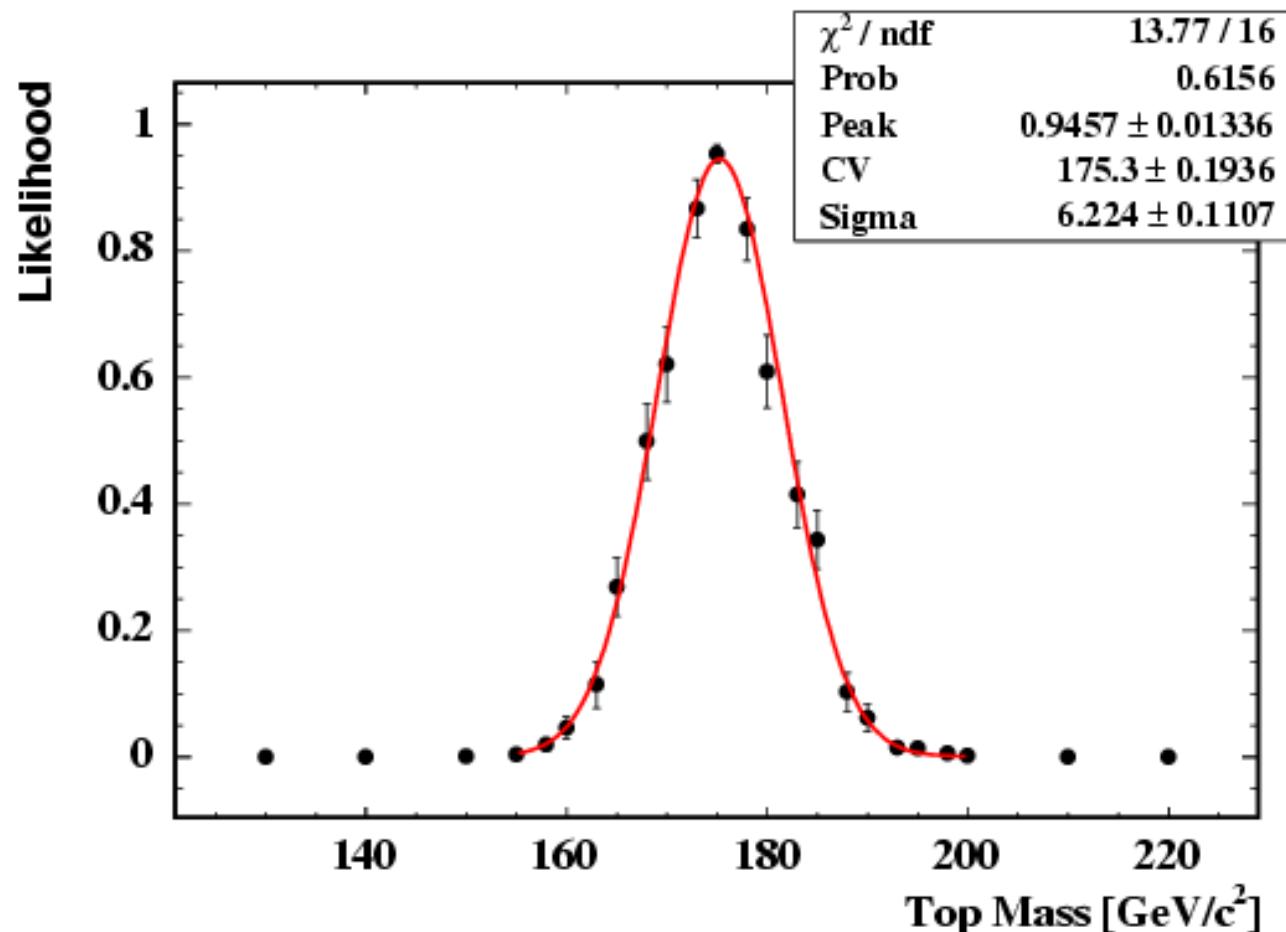
- Quantities with minimal dependence on jet energy scale



# Results

1.9 fb<sup>-1</sup>

- Likelihood fit for data using mean values of both variables



$$m_{\text{top}} = 176.7 \pm 6.2 \text{ (stat)} \pm 3.0 \text{ (syst) GeV}$$

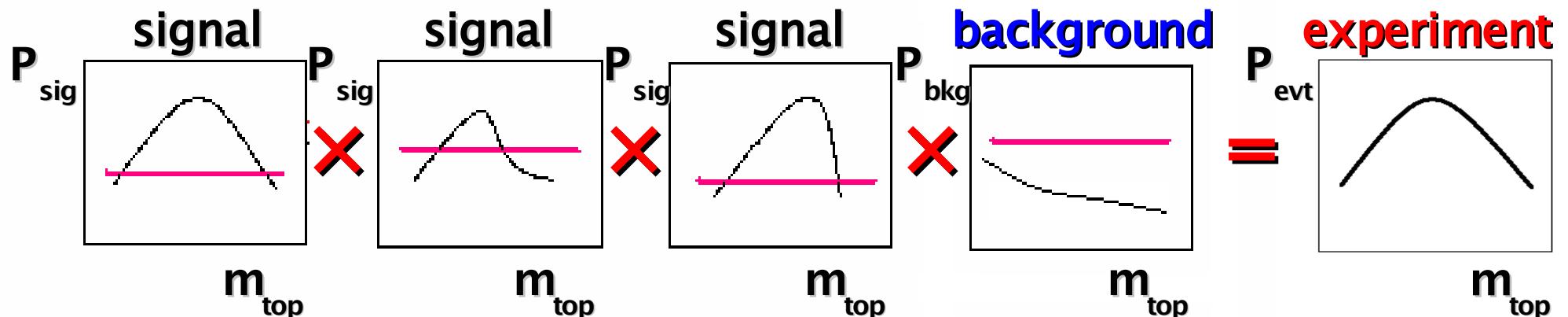
 $\pm 3.9\%$

# Outline

**Templates  
Matrix Elements  
Cross Section  
Summary**

# Extraction techniques: matrix element

- probability densities for every event as function of  $m_{top}$



$$P_{sig}(x; m_{top}, JES) = \underbrace{Acc(x)}_{\text{Acceptance}} \times \frac{1}{\sigma} \underbrace{\int d^n \sigma(y; m_{top}) dq_1 dq_2 f(q_1) f(q_2)}_{\text{LO-Matrix element x phase space}} \underbrace{W(x, y; JES)}_{\text{PDF's}}$$

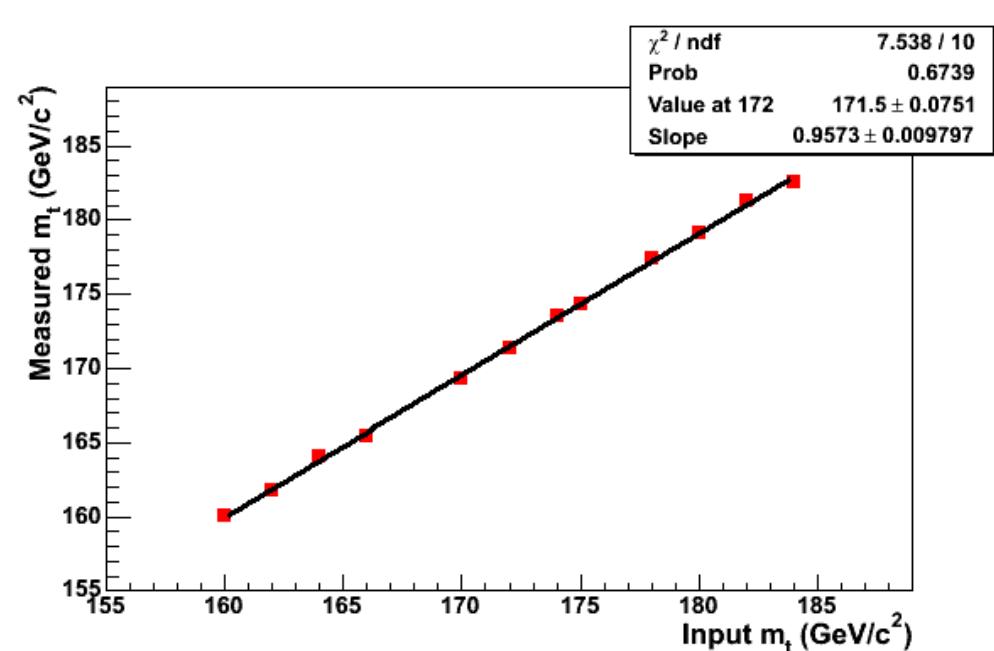
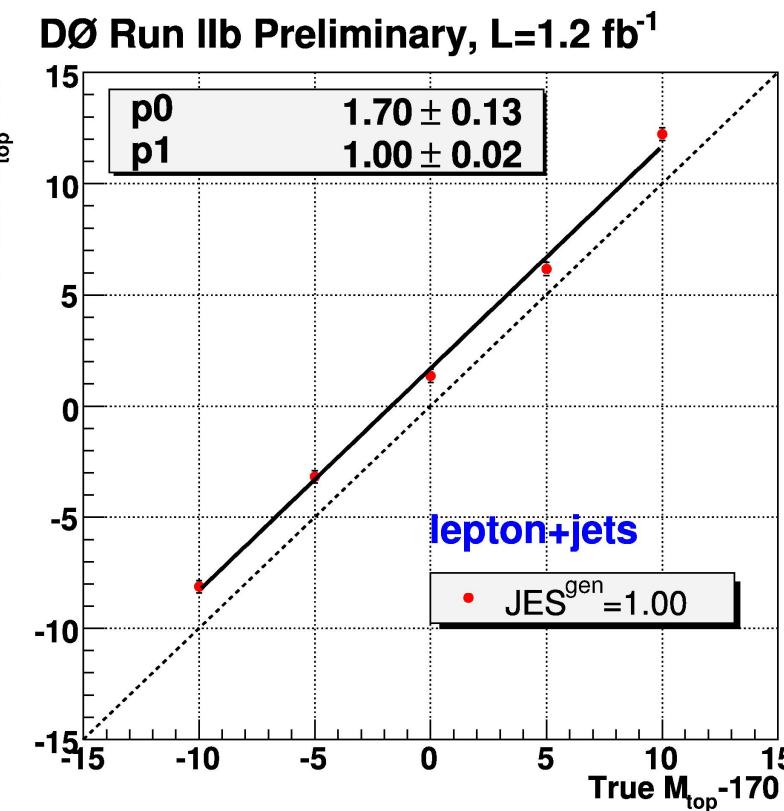
Acceptance  
(selection,  
trigger,...)
LO-Matrix element  
x phase space
PDF's
Transfer Functions  
(Probability to measure  
x when y was produced)

- maximum Likelihood fit:

$$L(x_1, \dots, x_n; m_{top}, JES, f_{top}) = \prod_{i=1}^n P_{evt}(x_i; m_{top}, JES, f_{top})$$

# Calibration: ensemble tests

- pseudo experiments: compare measured mass with generated
- correct for differences: calibration curve



- rely on MC simulations (ALPGEN, PYTHIA) in detail...

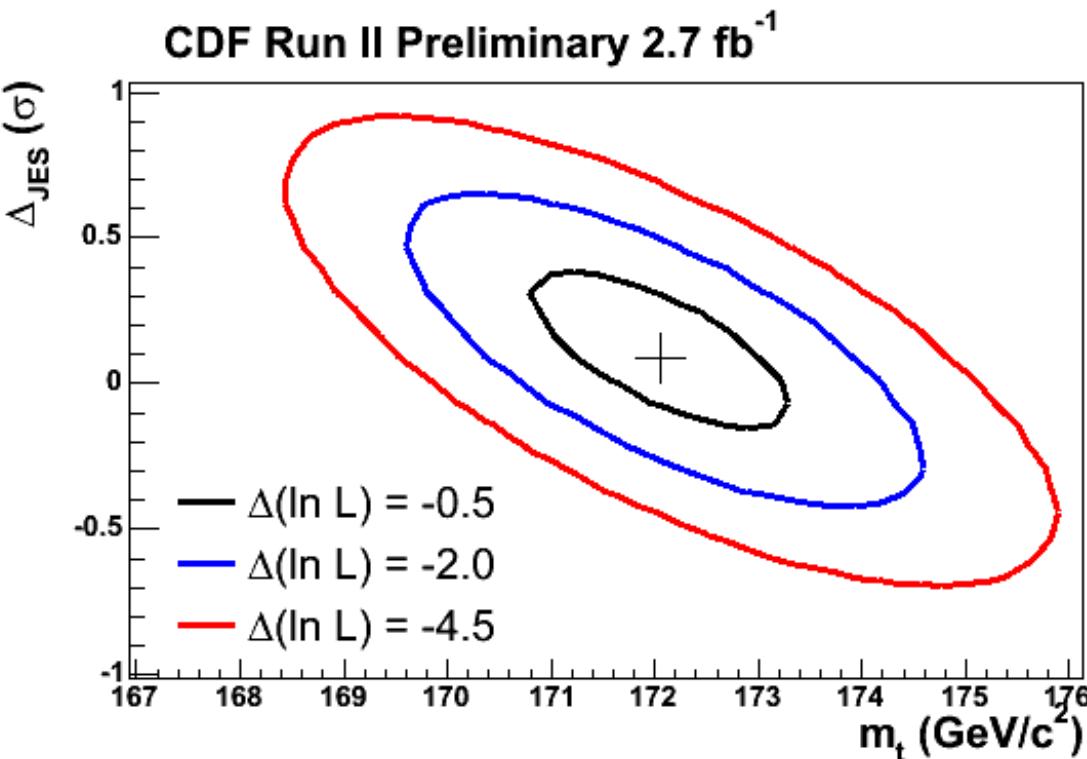
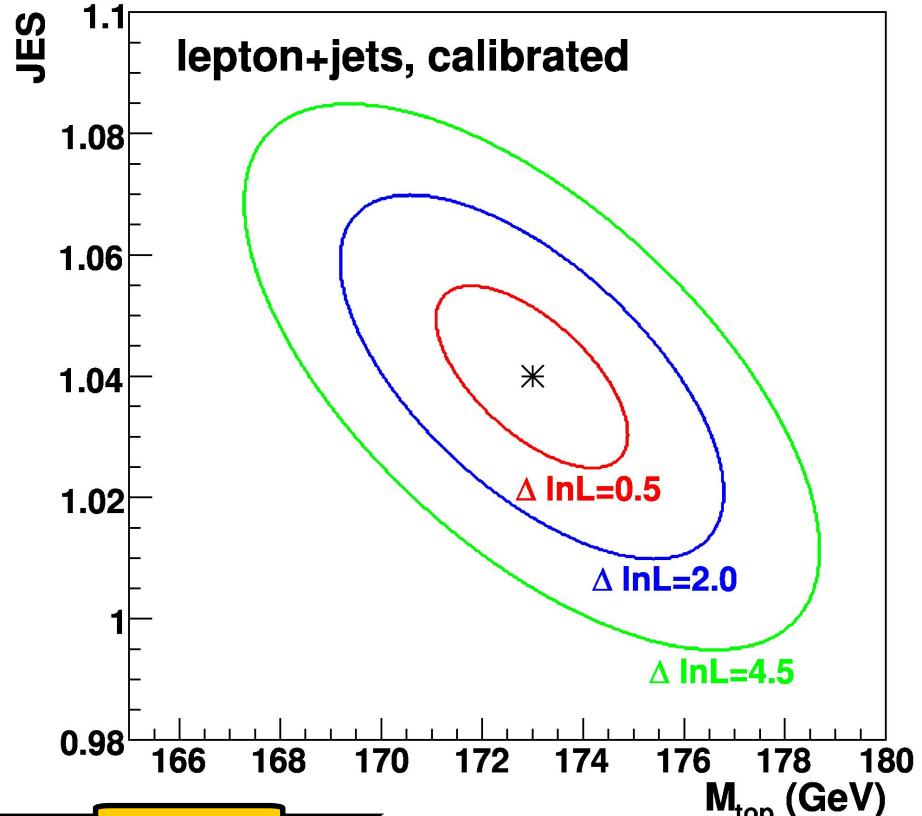


# Results



DØ Run IIb Preliminary,  $L=1.2 \text{ fb}^{-1}$

2.7  $\text{fb}^{-1}$



$$m_{\text{top}} = 172.2 \pm 1.0 \text{ (stat)} \pm 1.4 \text{ (syst)} \text{ GeV}$$

**$\pm 1.0\%$**

$$m_{\text{top}} = 172.2 \pm 1.0 \text{ (stat)} \pm 1.3 \text{ (syst)} \text{ GeV}$$

**$\pm 1.0\%$**

# Systematics apart from simultaneous JES



Source	Uncertainty on top mass ( $\text{GeV}/c^2$ )
Signal modeling	$\pm 0.40$
Background modeling	$\pm 0.08$
$W$ heavy flavor factor	$\pm 0.07$
$b$ fragmentation function	$\pm 0.10$
PDF uncertainty	$\pm 0.24$
Residual JES uncertainty	$\pm 0.03$
Relative $b$ /light Jet Energy Scale	$\pm 0.82$
$b$ -tagging efficiency	$\pm 0.16$
Trigger efficiency	$\pm 0.09$
Jet energy resolution	$\pm 0.30$
Multijet background	$\pm 0.20$
MC calibration	$\pm 0.14$
Total	$\pm 1.0$

Systematic source	Systematic uncertainty ( $\text{GeV}/c^2$ )
Calibration	0.1
MC generator	0.5
ISR and FSR	0.3
Residual JES	0.5
$b$ -JES	0.4
Lepton $P_T$	0.2
Pileup	0.1
PDFs	0.2
Background	0.4
Total	1.0

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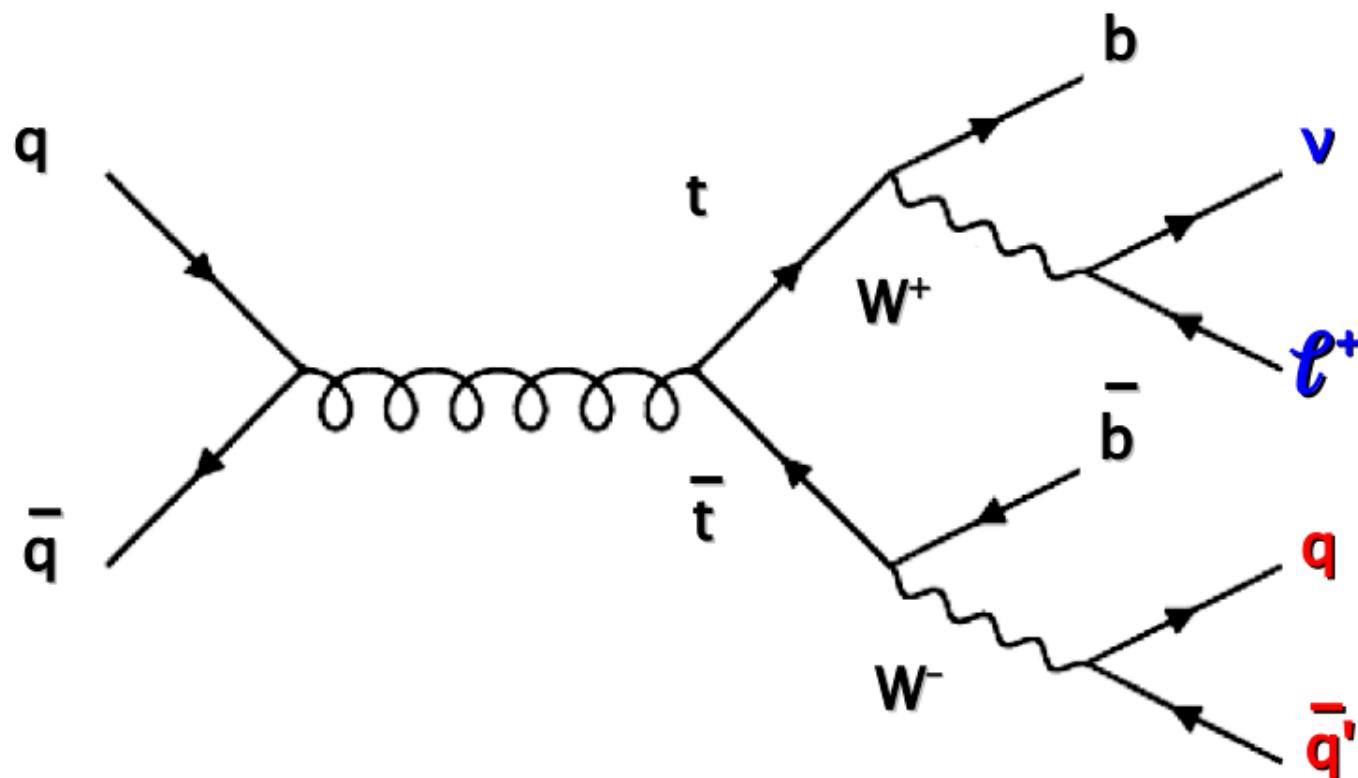
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- work together to get uniform treatment where possible

# Top mass interpretation

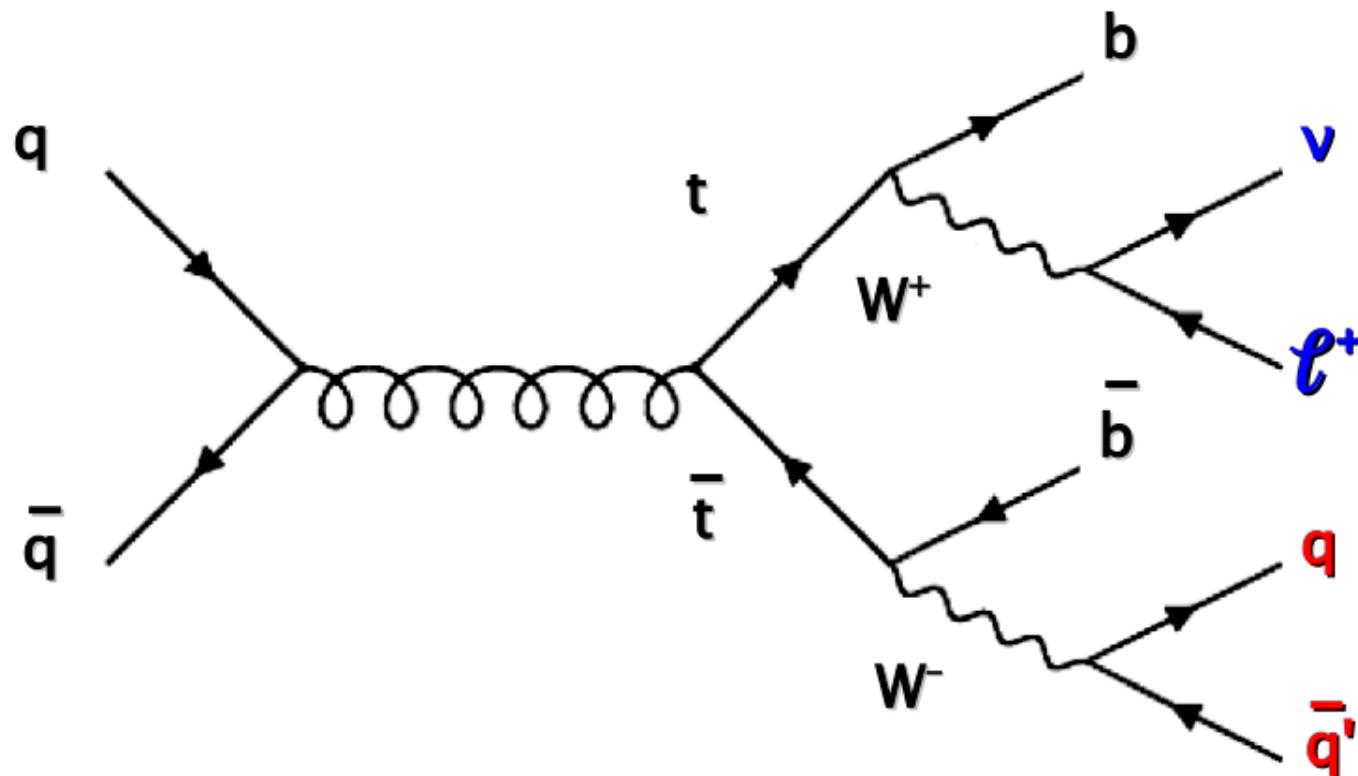
**the concept of quark mass is convention-dependent!**



# Top mass interpretation

**the concept of quark mass is convention-dependent!**

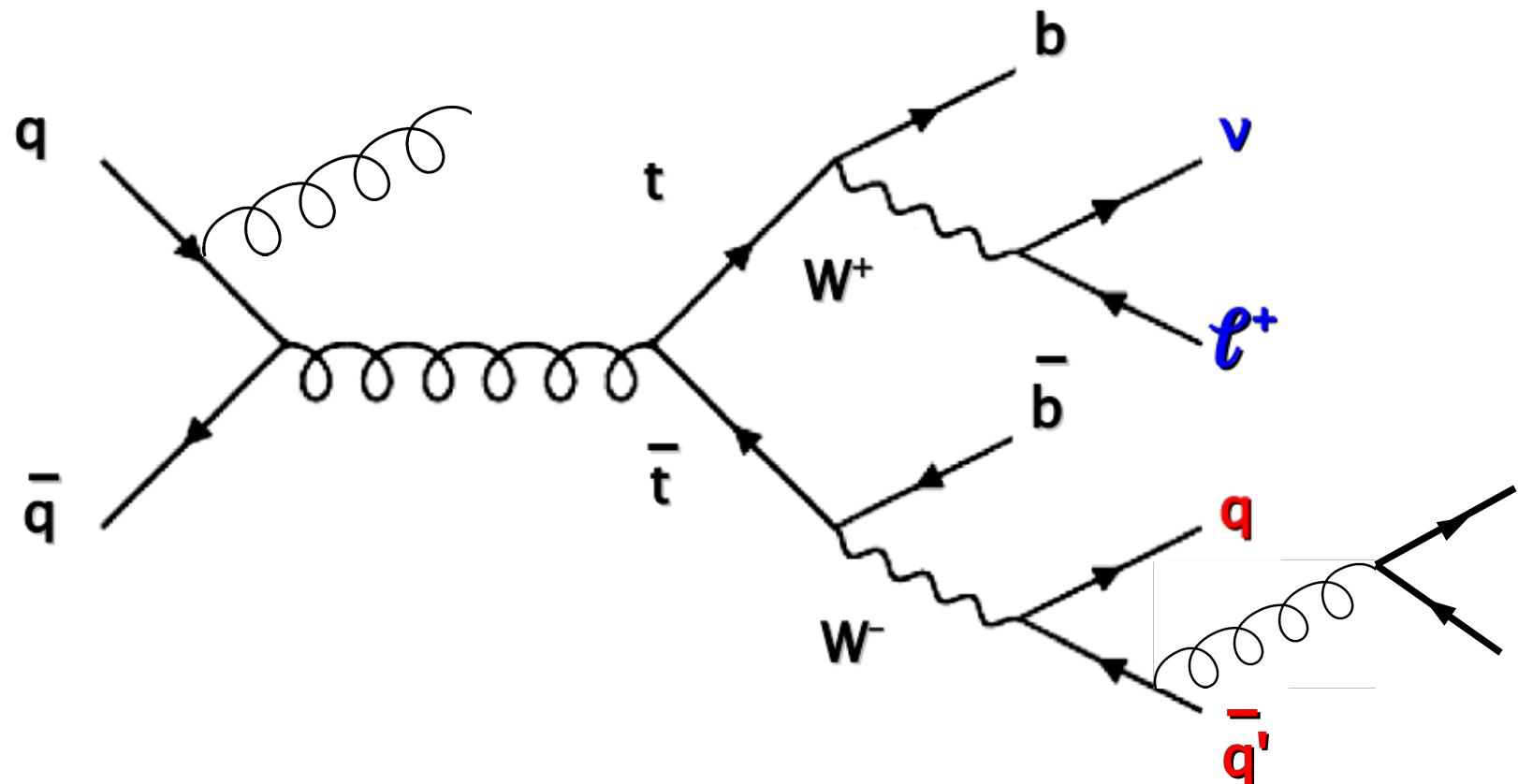
- matrix element in LO QCD



# Top mass interpretation

**the concept of quark mass is convention-dependent!**

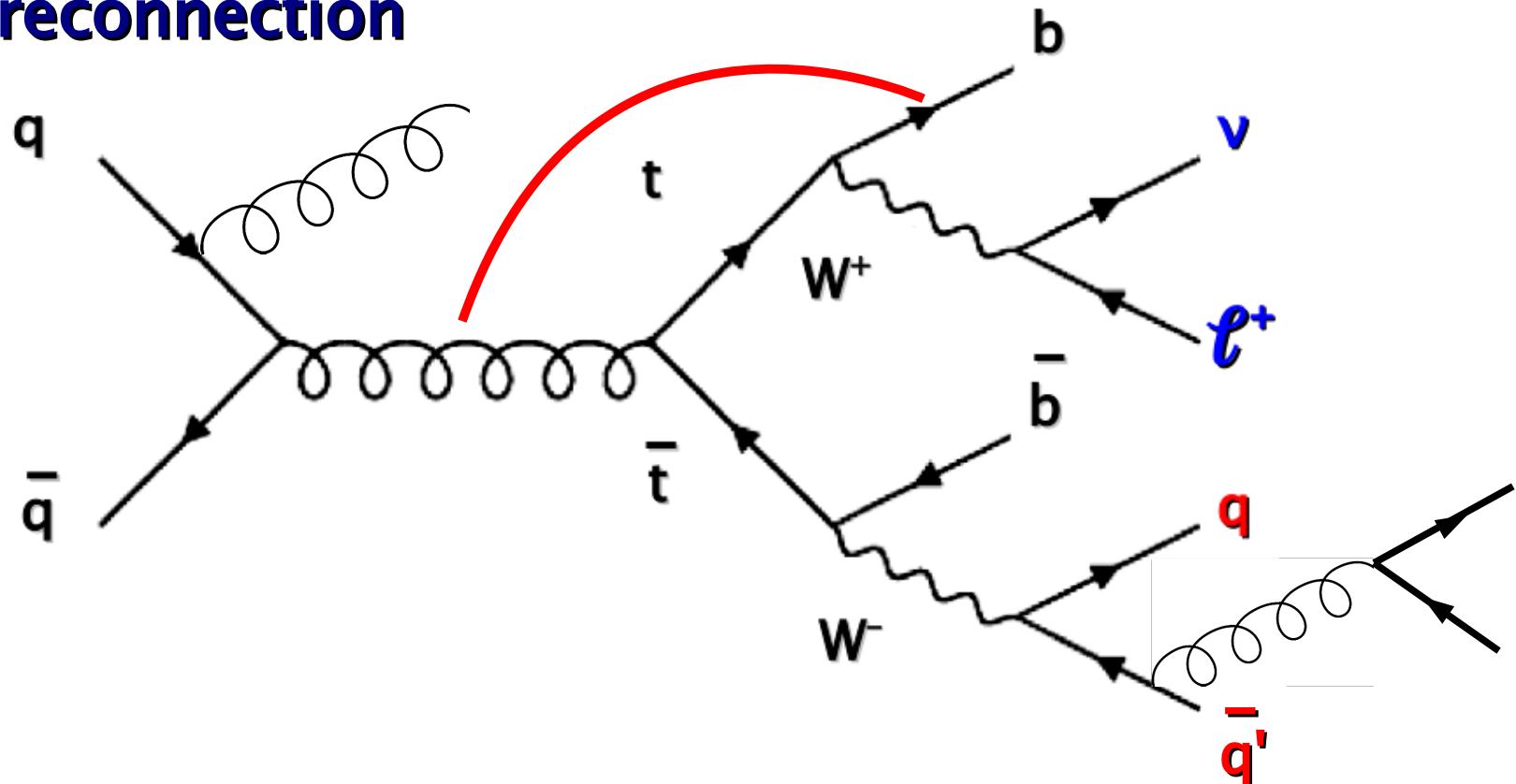
- matrix element in LO QCD
- parton showers



# Top mass interpretation

**the concept of quark mass is convention-dependent!**

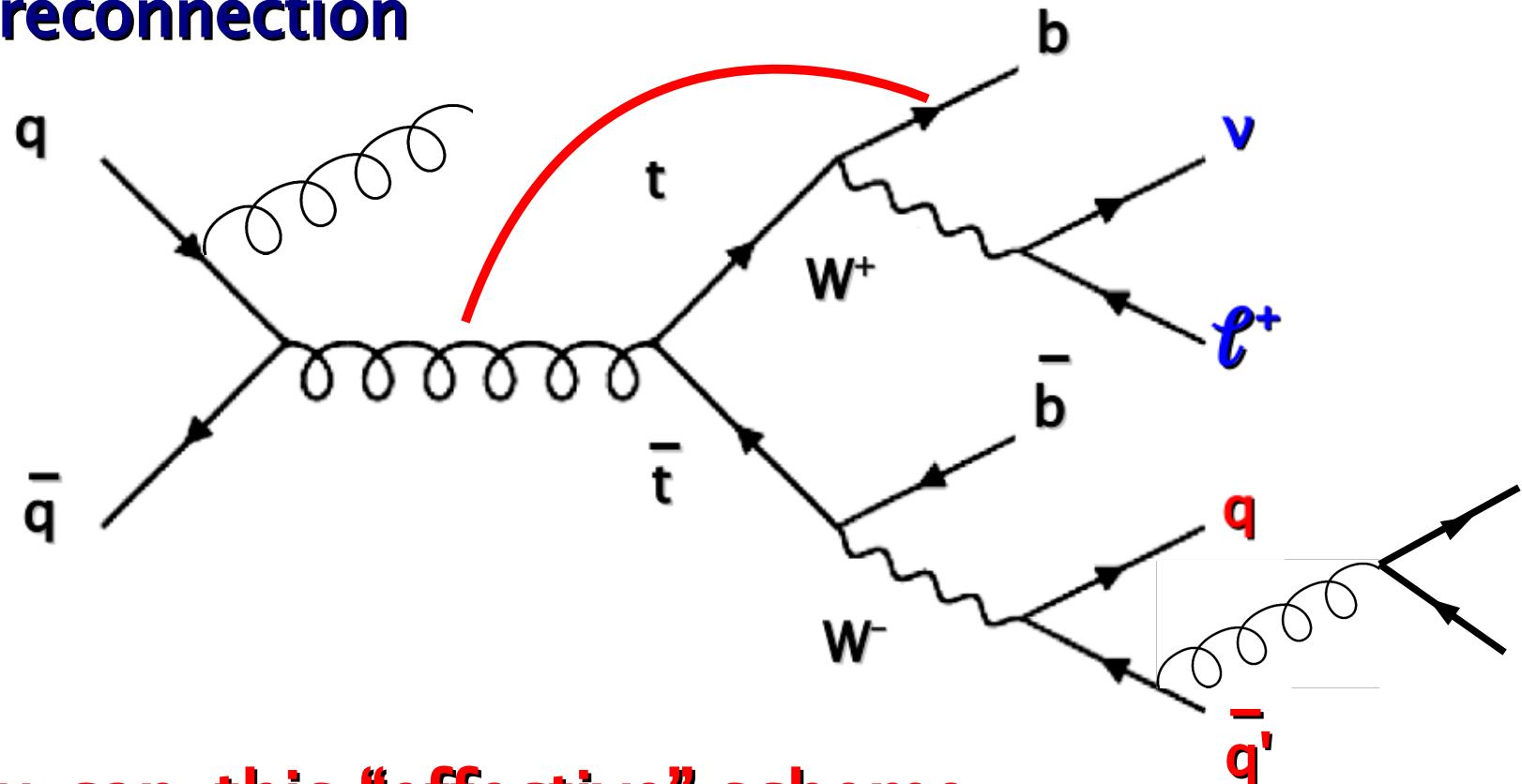
- matrix element in LO QCD
- parton showers
- color reconnection



# Top mass interpretation

**the concept of quark mass is convention-dependent!**

- matrix element in LO QCD
- parton showers
- color reconnection



⇒ how can this “effective” scheme  
translated to a renormalisation scheme?

# Outline

**Templates  
Matrix Elements  
Cross Section  
Summary**

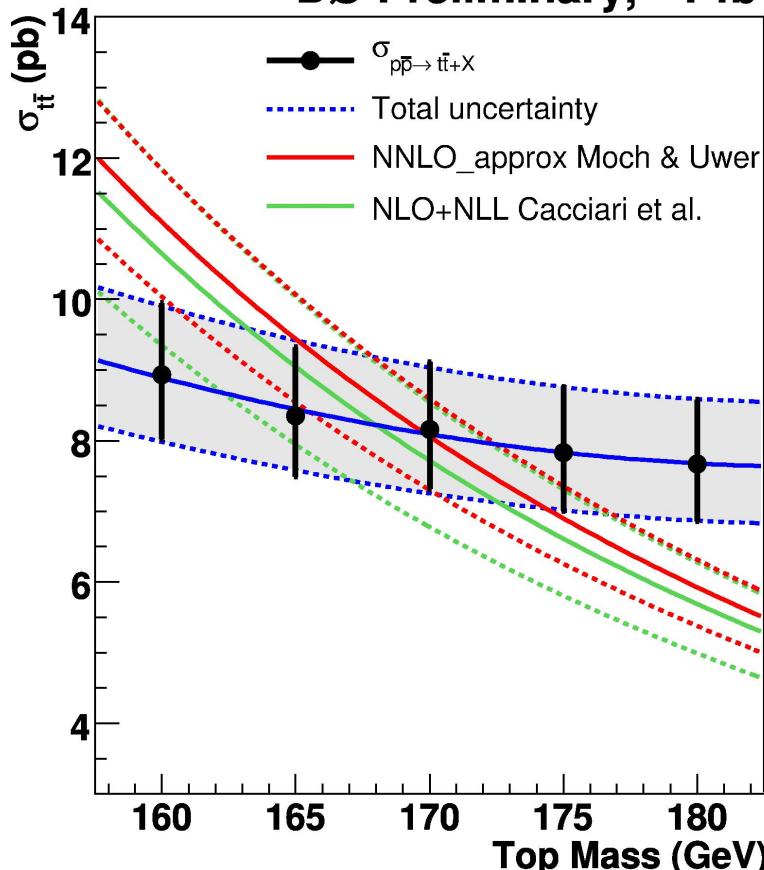
# Top mass from cross section measurement



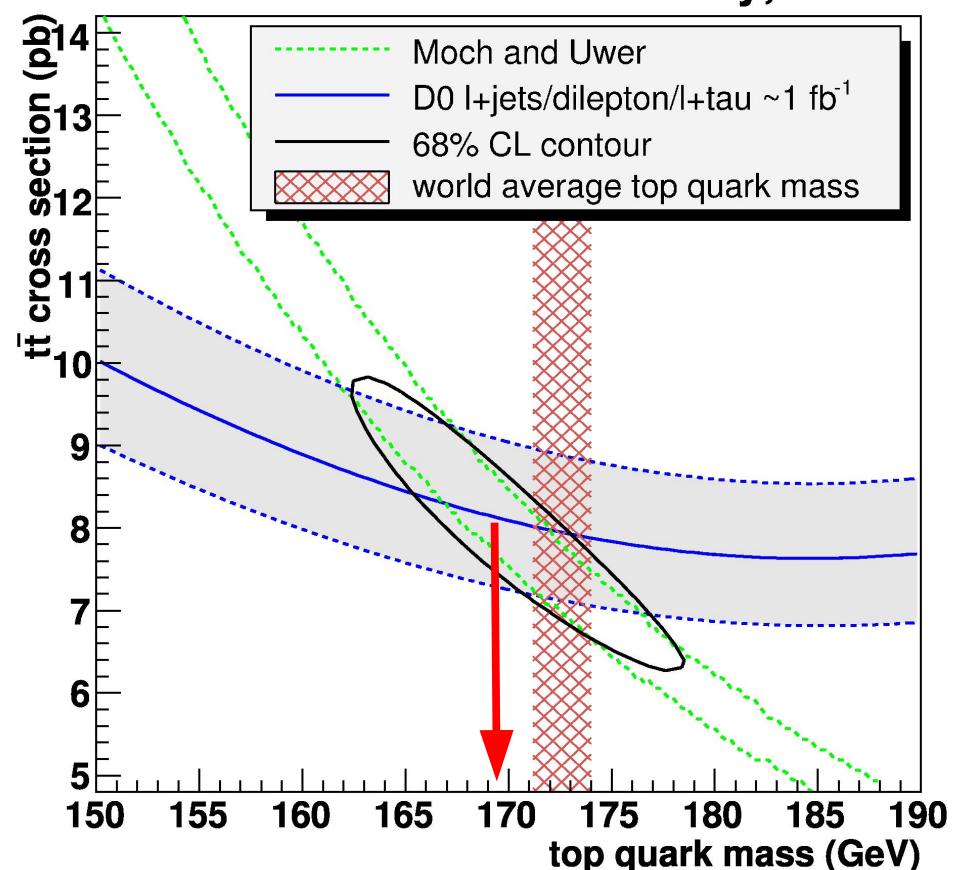
- lepton+jets/dilepton/lepton+tau combination

1.0  $\text{fb}^{-1}$

DØ Preliminary,  $\sim 1 \text{ fb}^{-1}$



DØ Preliminary,  $\sim 1 \text{ fb}^{-1}$



pole mass

$M_{\text{top}} = 169.6 \pm 5.5 \text{ GeV}$  with NNLO<sub>approx</sub>

$\pm 3.2\%$

# Outline

**Templates  
Matrix Elements  
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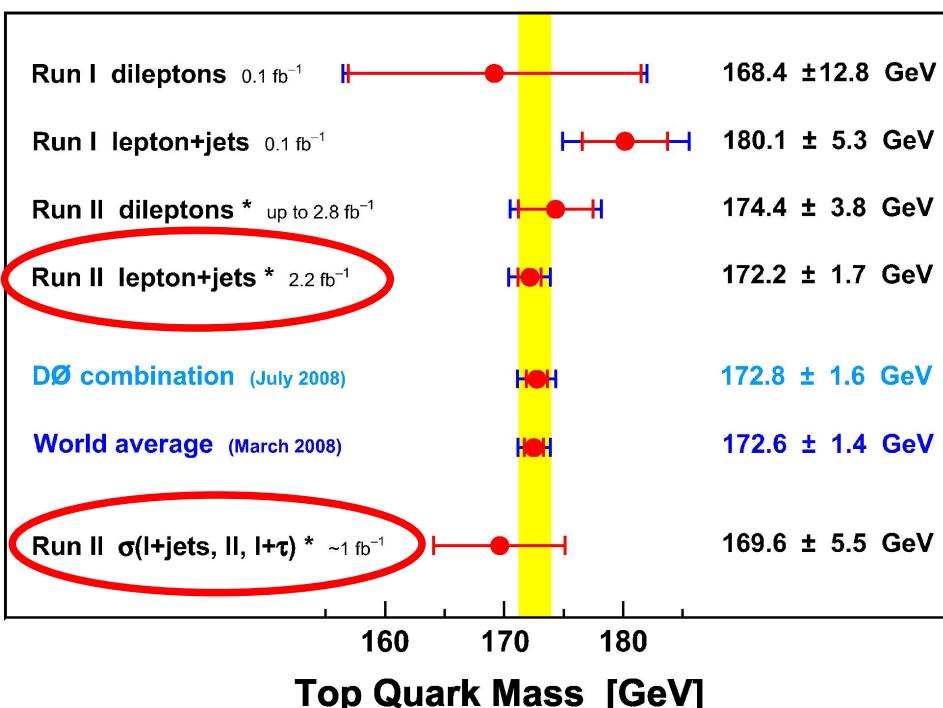
# Summary



**DØ**

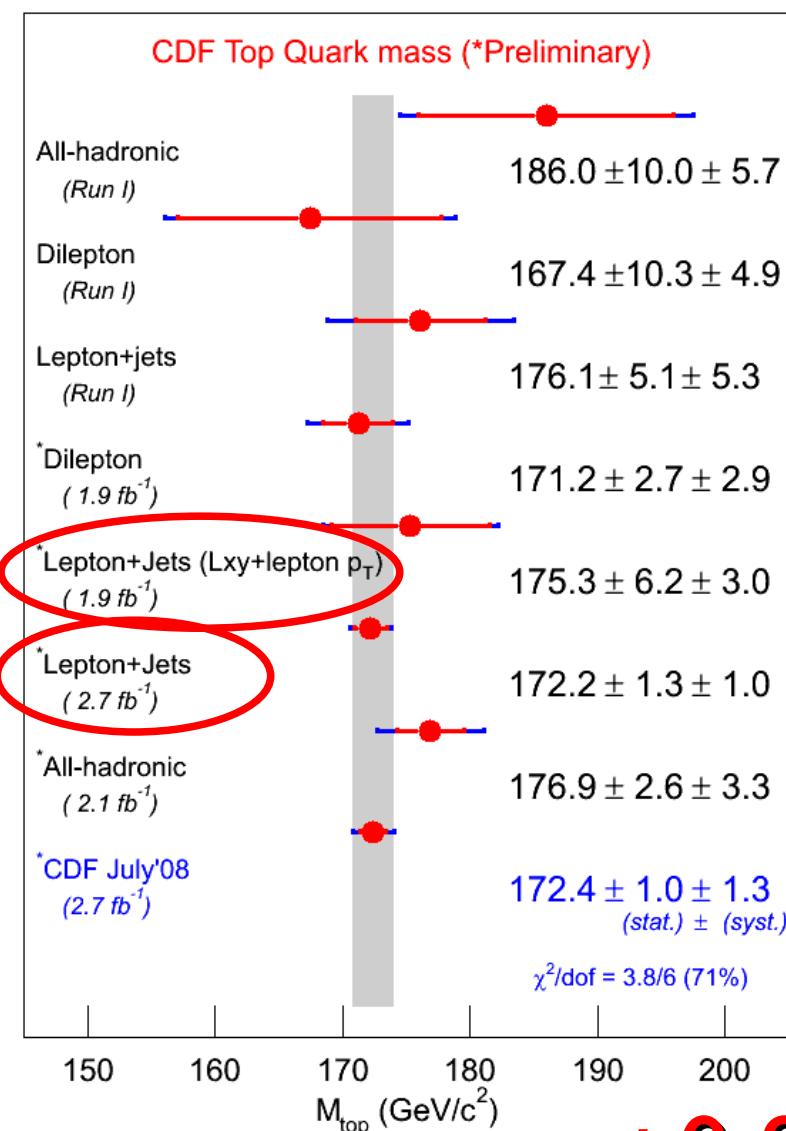
\* = preliminary

Summer 2008



**$\pm 0.92\%$**

- ideogram method



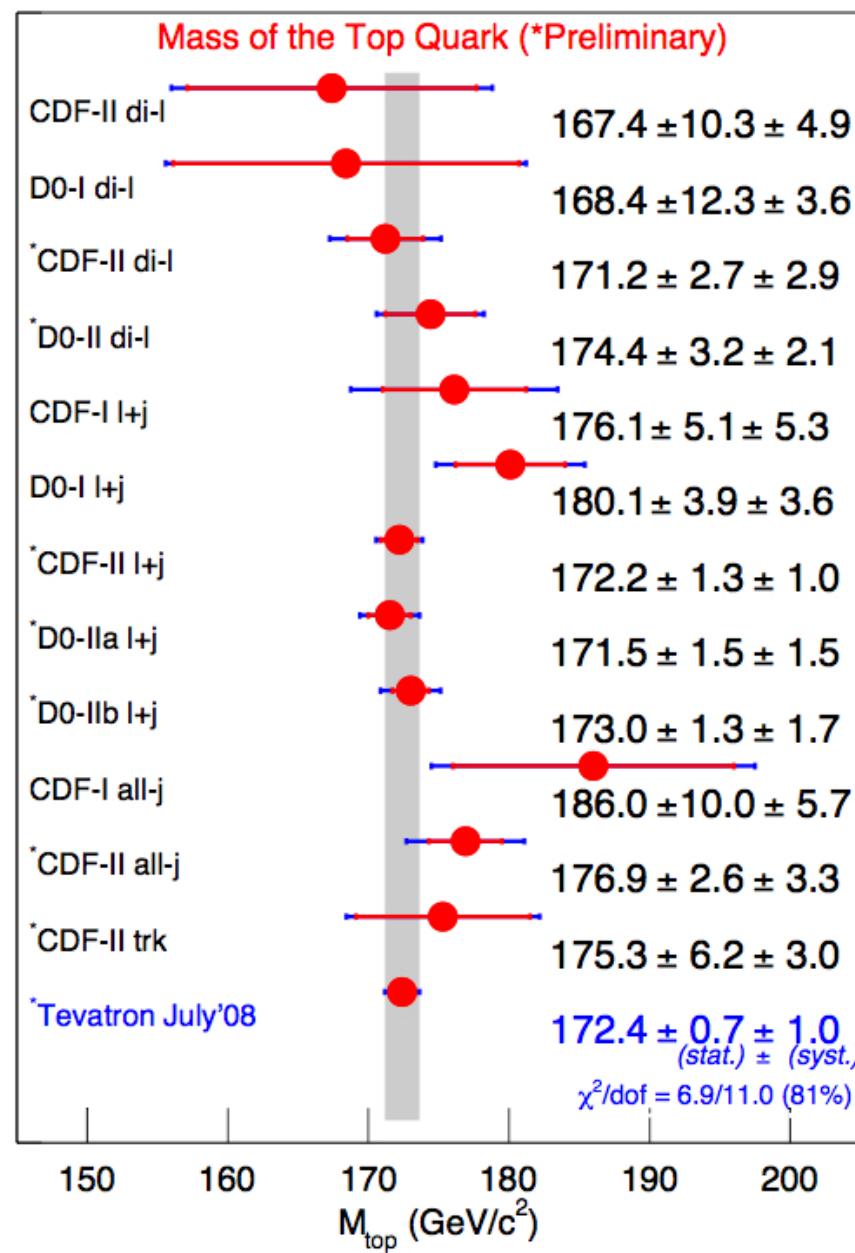
**$\pm 0.95\%$**

- template

- dynamical likelihood



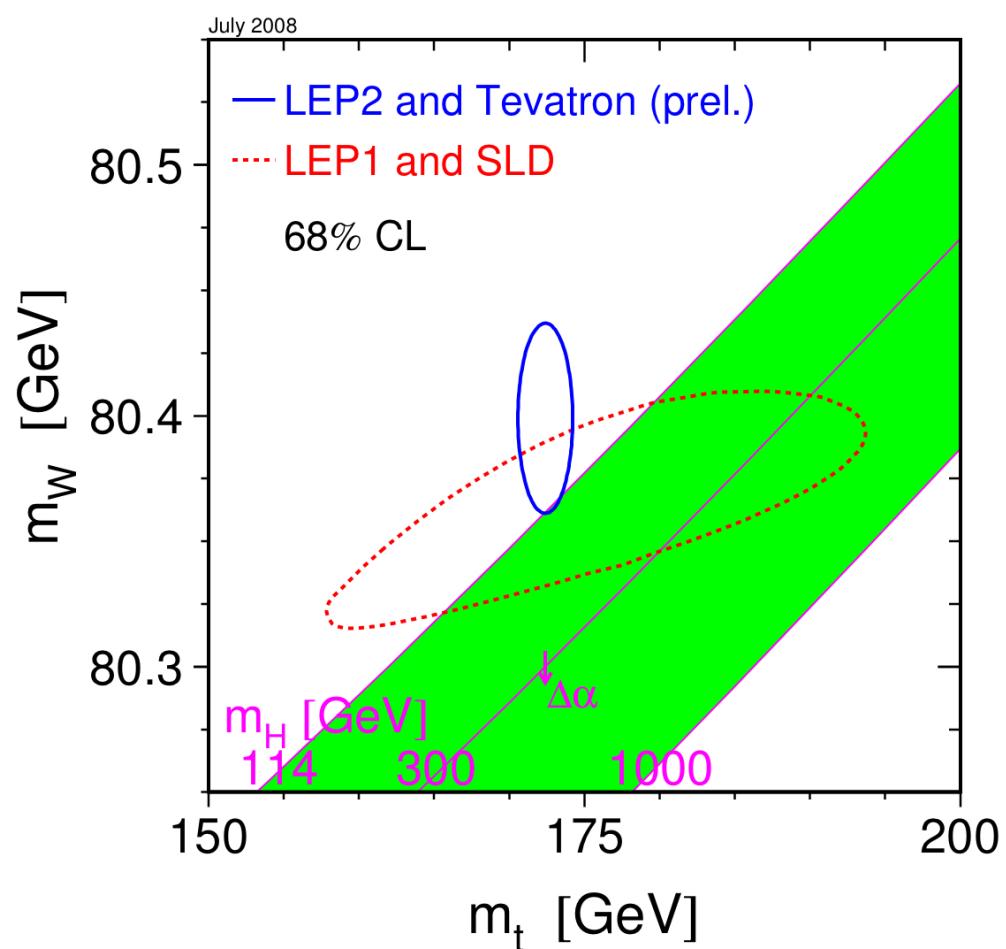
# Tevatron Combination: July 2008



• up to

2.8 fb<sup>-1</sup>

$$M_{\text{top}} = 172.4 \pm 1.2 \text{ GeV} \pm 0.7\%$$



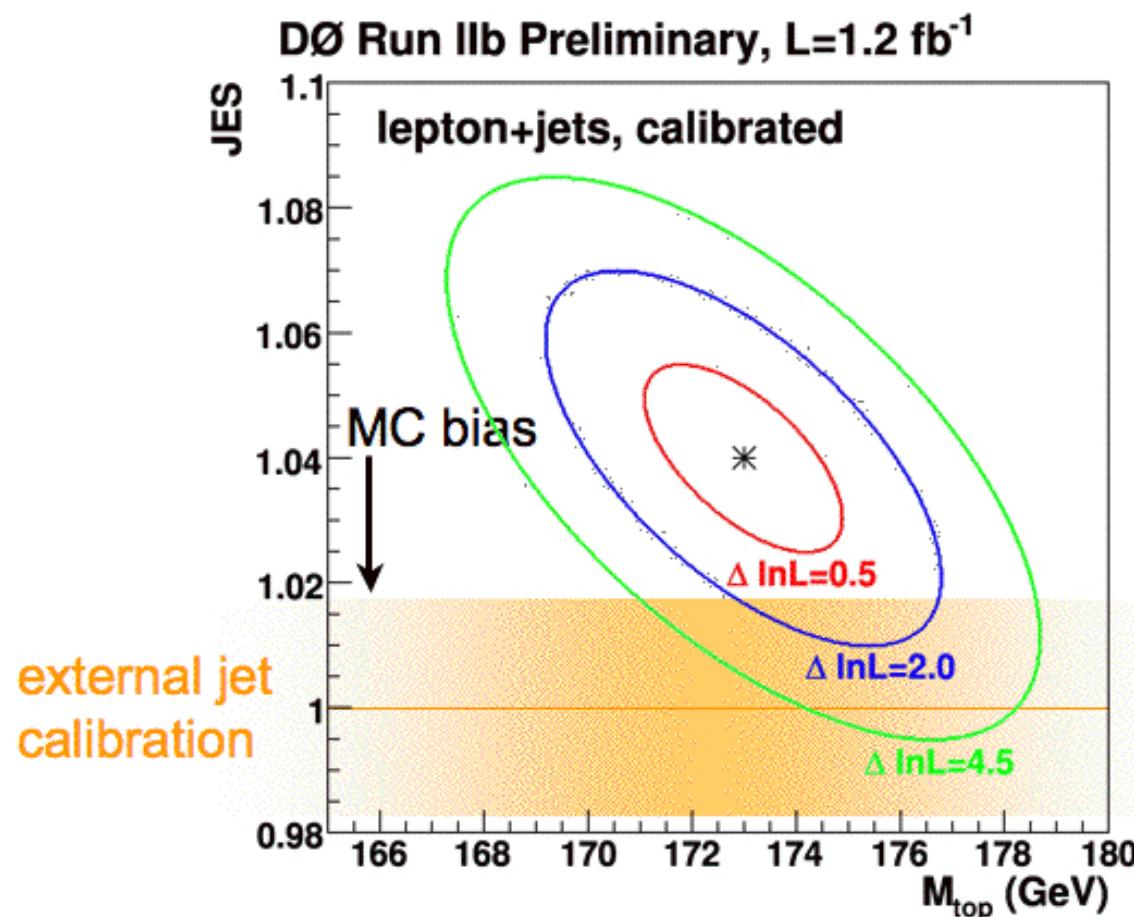
# Conclusions

## main challenges for the future:

- CDF & DØ:  
better understanding of systematics
- Theory & experiment:  
better understanding on theoretical uncertainties  
and interpretation of top quark mass

# Backup

# Results

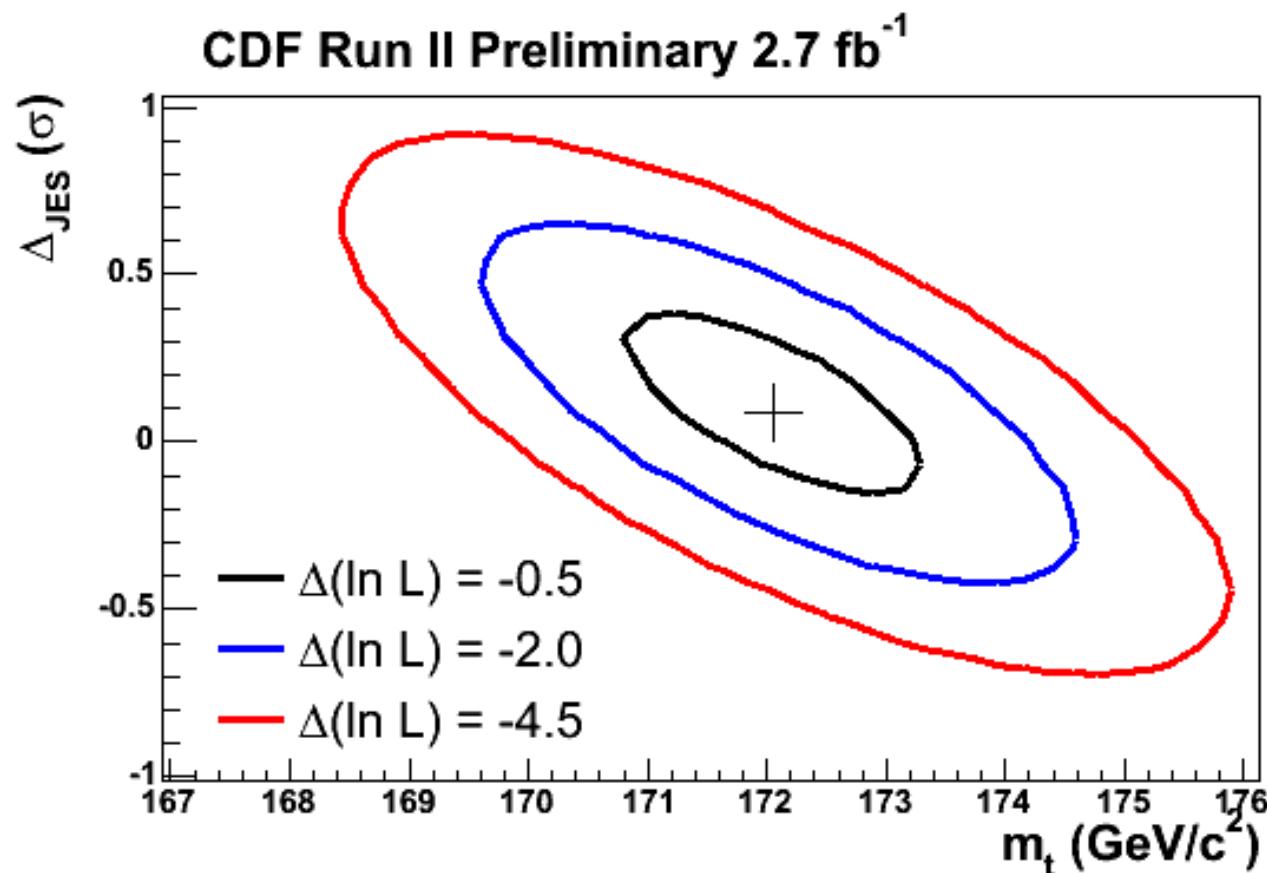


**$\pm 1.0\%$**

$m_{\text{top}} = 172.2 \pm 1.0 \text{ (stat)} \pm 1.4 \text{ (syst)} \text{ GeV}$

$2.2 \text{ fb}^{-1}$

# Results

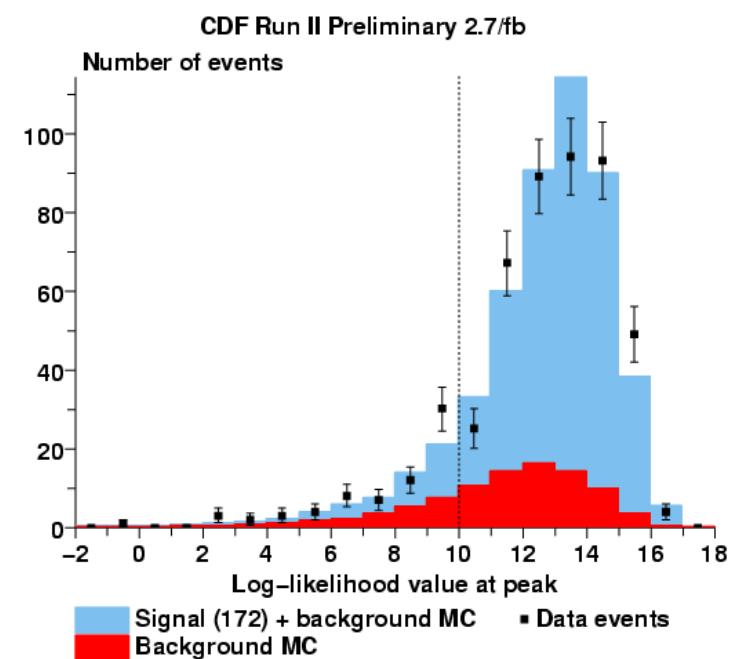
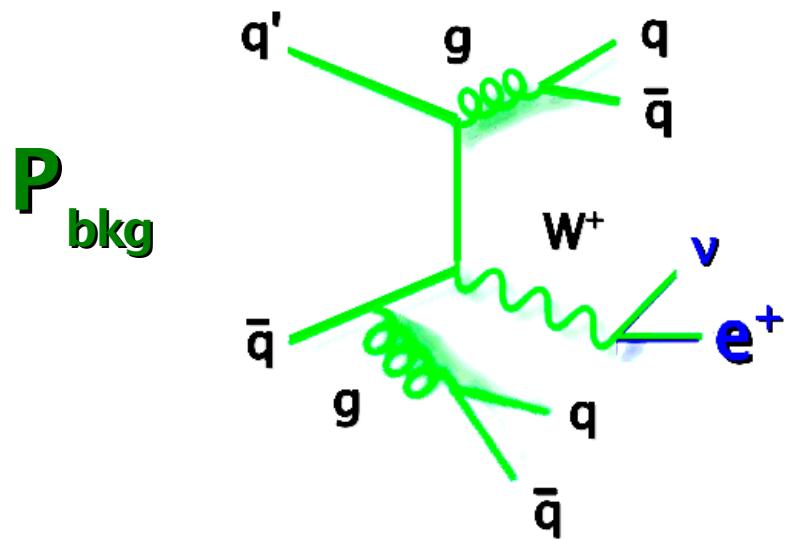
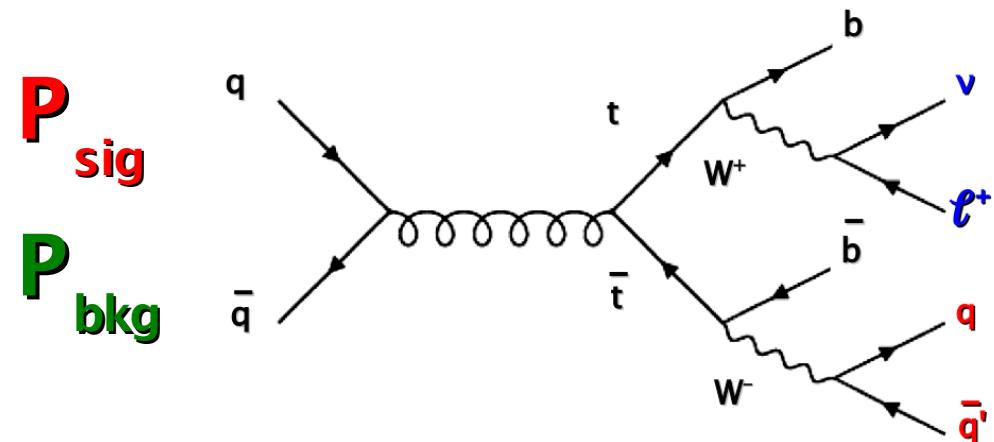
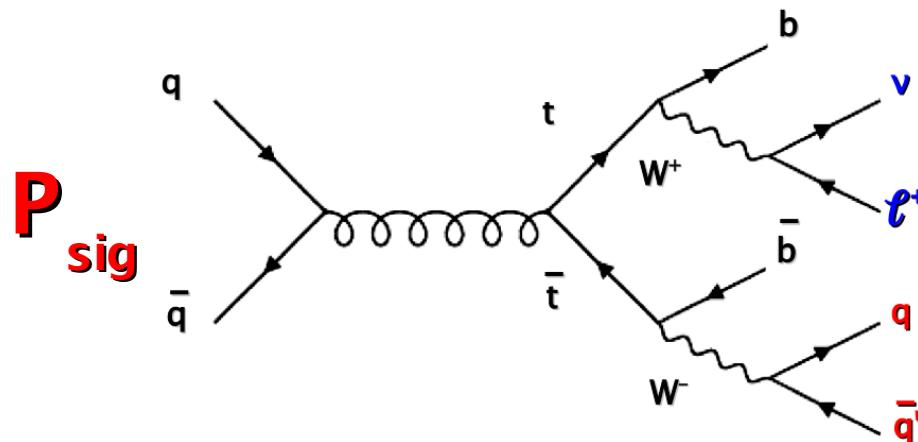


**±1.0%**

$m_{\text{top}} = 172.2 \pm 1.0 \text{ (stat)} \pm 1.3 \text{ (syst)} \text{ GeV}$

$2.7 \text{ fb}^{-1}$

# Matrix element method comparisons



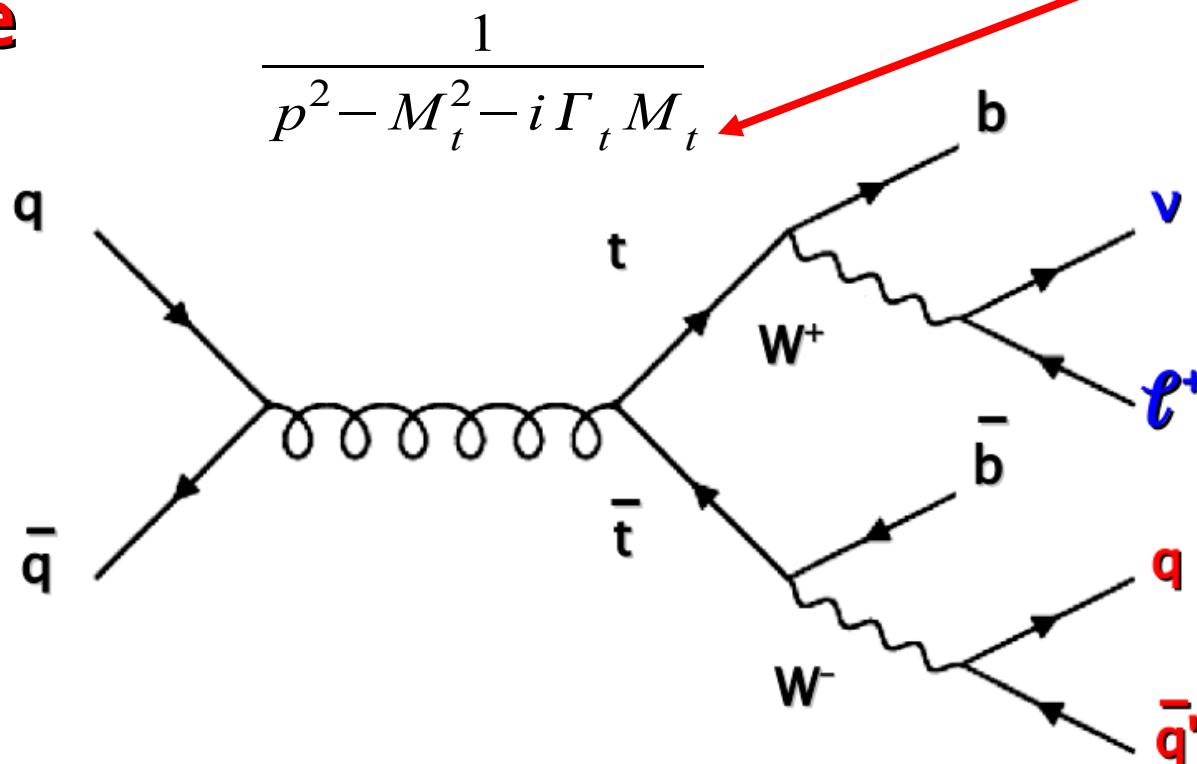
# Differences in top mass definitions

hep-ph/0001002

$\overline{\text{MS}}$  scheme

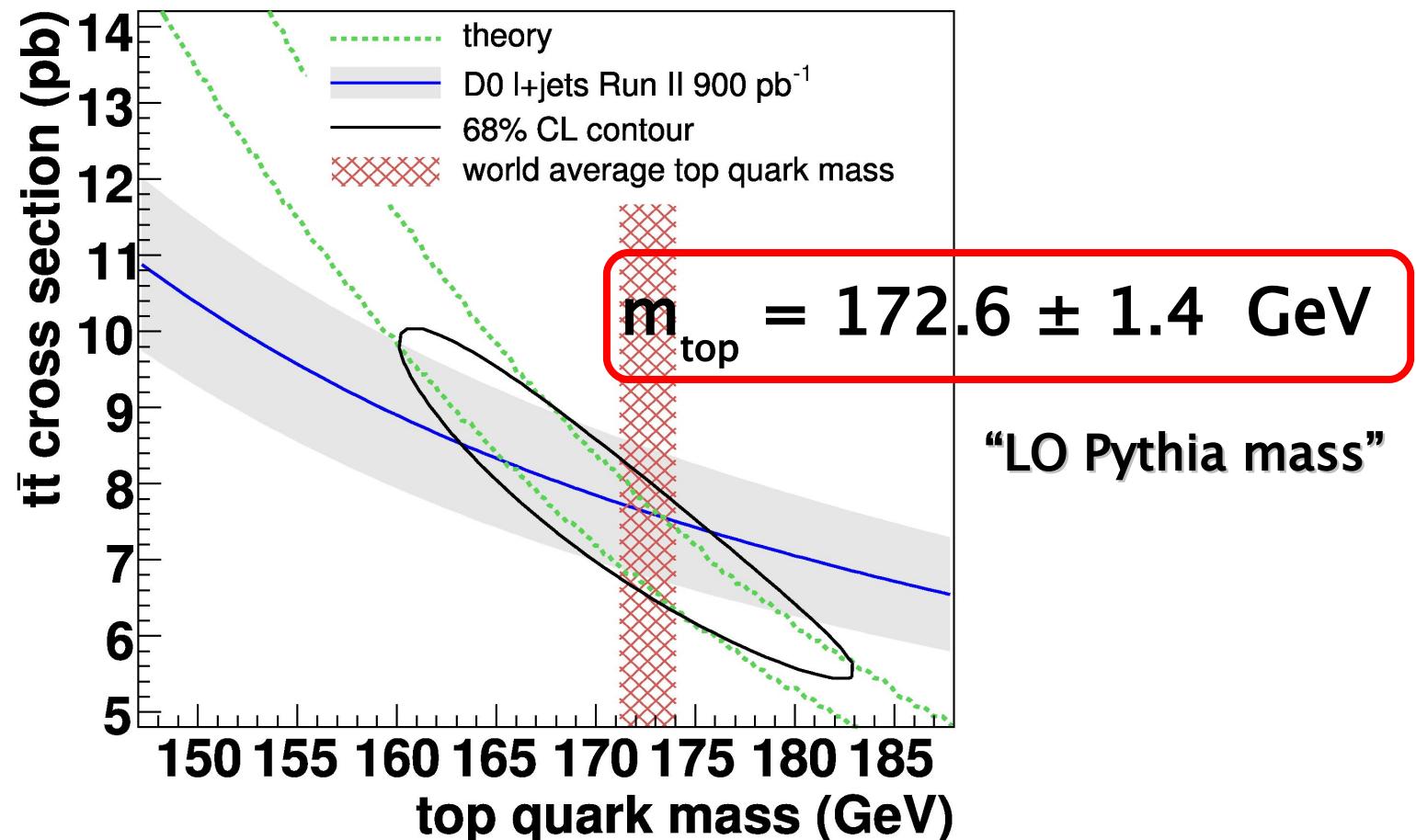
$$\overline{m}_t \equiv m_t^{\overline{\text{MS}}} (m_t) = \frac{M_t}{1 + \frac{4}{3\pi} \alpha_s(M_t)}$$

pole mass



⇒ difference between  $\overline{\text{MS}}$  and pole mass is  $\approx 7 \text{ GeV...}$

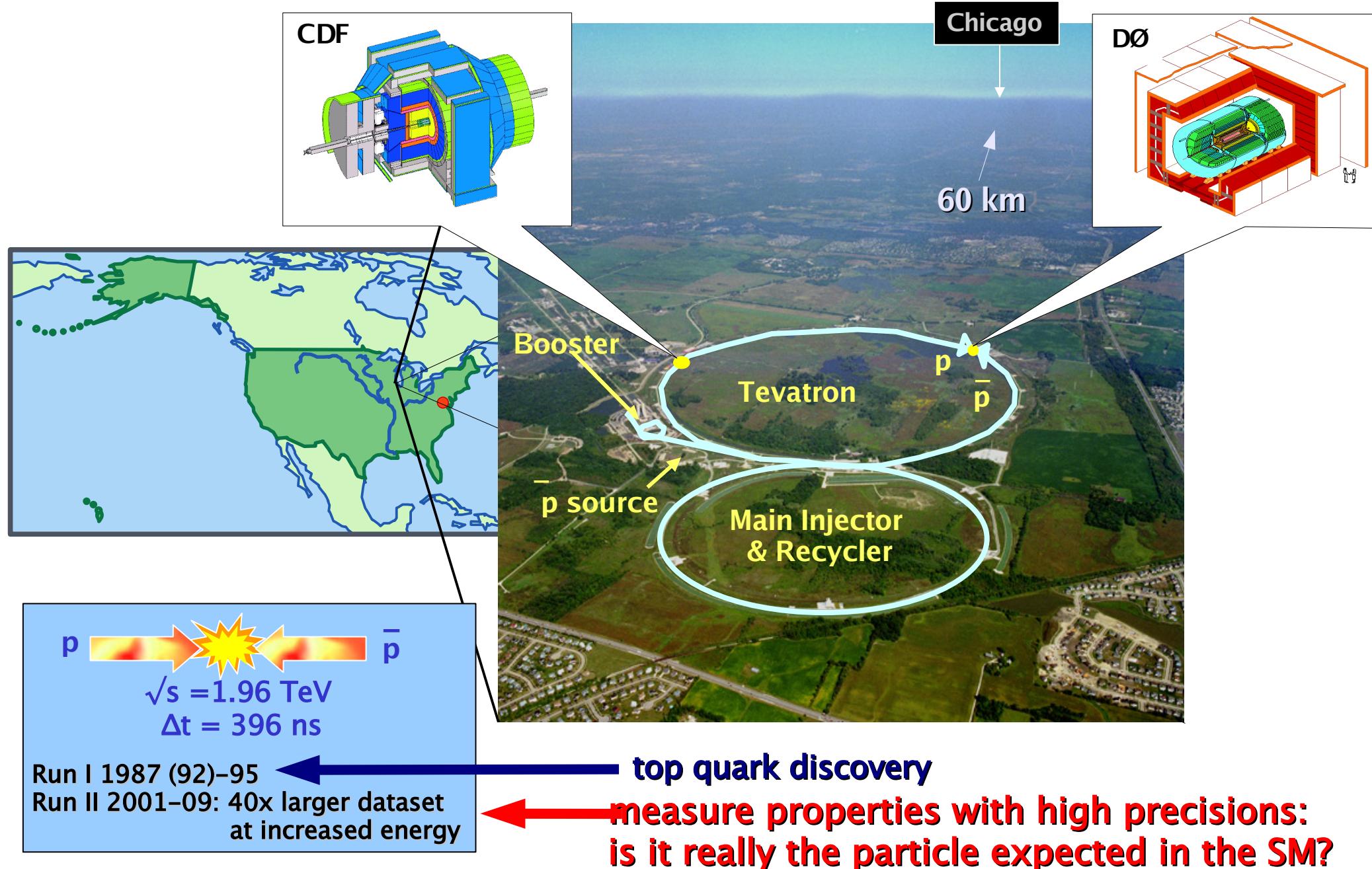
# Top mass from cross section measurement



$$M_{\text{top}} = 170 \pm 7 \text{ GeV}$$

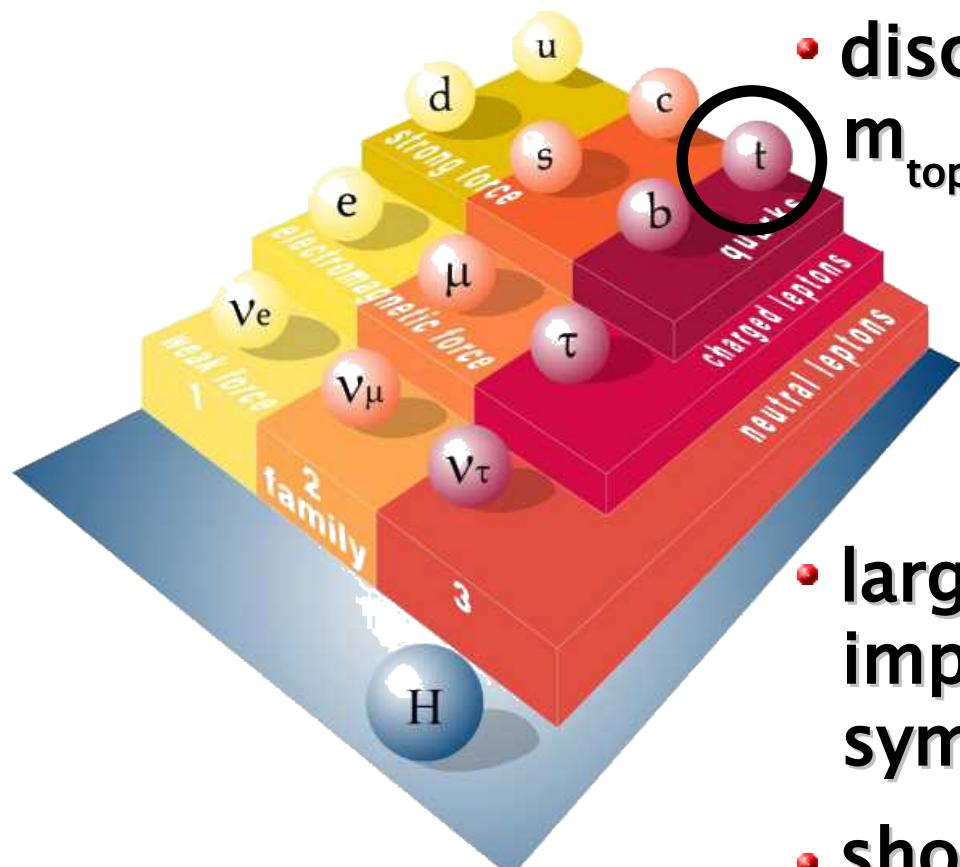
pole mass

# The Tevatron at FERMILAB: $p\bar{p}$ Collisions



# The Top Quark

- needed as isospin partner of bottom quark
- discovered in 1995 by CDF and DØ:  
 $m_{top} \sim$  gold atom



- large coupling to Higgs boson  $\sim 1$ :  
important role in electroweak symmetry breaking?
- short lifetime:  $\tau \sim 5 \cdot 10^{-25} s \ll \Lambda_{QCD}^{-1}$ :  
decays before fragmenting  
→ observe “naked” quark