



# **Measurement of the $B_s^0$ Lifetime and a Measurement of the Lifetime Difference in the $B_s^0$ System at DØ**

**For the DØ Collaboration**





# The Focus of B Physics Studies: CKM Matrix

**Relates quark  
mass and  
weak  
eigenstates**

$$V_{\text{CKM}} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \simeq \begin{bmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 & 1 \end{bmatrix}.$$

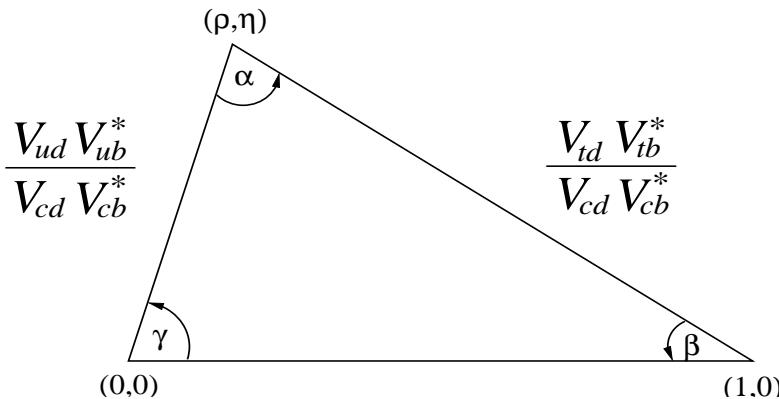
**SM: CP-violating processes solely related to one phase in CKM**

**'bd'**

**(THE unitary triangle)**

**Large effort in B physics**

**Mainly at B factories**



**'bs'**

**(A 'squashed' unitary triangle)**

$\beta \rightarrow \beta_s$

$\beta_s$  small in SM

**Checking if  $\beta_s$  is small is as important as measuring the sides and angles of THE unitary triangle**



# B<sub>s</sub> System

Schrodinger Equation:

$$i \frac{d}{dt} \begin{pmatrix} |B_s(t)\rangle \\ |\bar{B}_s(t)\rangle \end{pmatrix} = \left( M - i \frac{\Gamma}{2} \right) \begin{pmatrix} |B_s(t)\rangle \\ |\bar{B}_s(t)\rangle \end{pmatrix}$$

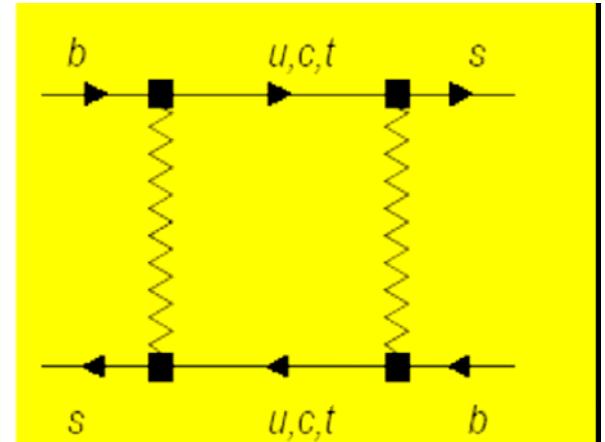
M<sub>12</sub> stems from the real part of the box diagram, dominated by top

Γ<sub>12</sub> stems from the imaginary part, dominated by charm

**Two physical states, Heavy and Light B<sub>s</sub> eigenstates, are expected to have different widths (propagate with different lifetimes)**

$$B_L = p|B_s\rangle + q|\bar{B}_s\rangle \approx cp \text{ odd}$$

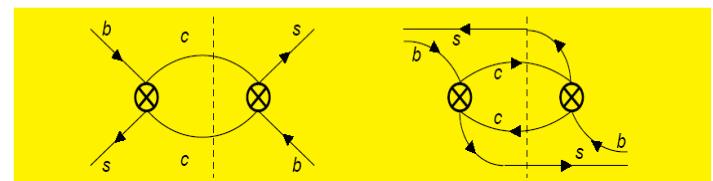
$$B_H = p|B_s\rangle - q|\bar{B}_s\rangle \approx cp \text{ even}, \quad p^2 + q^2 = 1$$



$$\Delta m = M_H - M_L \approx 2|M_{12}|$$

$$\Delta\Gamma = \Gamma_L - \Gamma_H \approx 2|\Gamma_{12}| \cos\phi$$

Γ<sub>12</sub> stems from final states common to B<sub>s</sub> and B̄<sub>s</sub>.

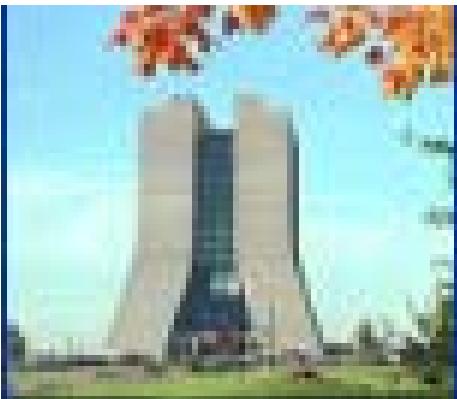


Crosses: Effective |ΔB| = 1 operators from W-exchange.

Γ<sub>12</sub> is a CKM-favored tree-level effect associated with final states containing a (c̄, c) pair.



# Fermilab and the Tevatron



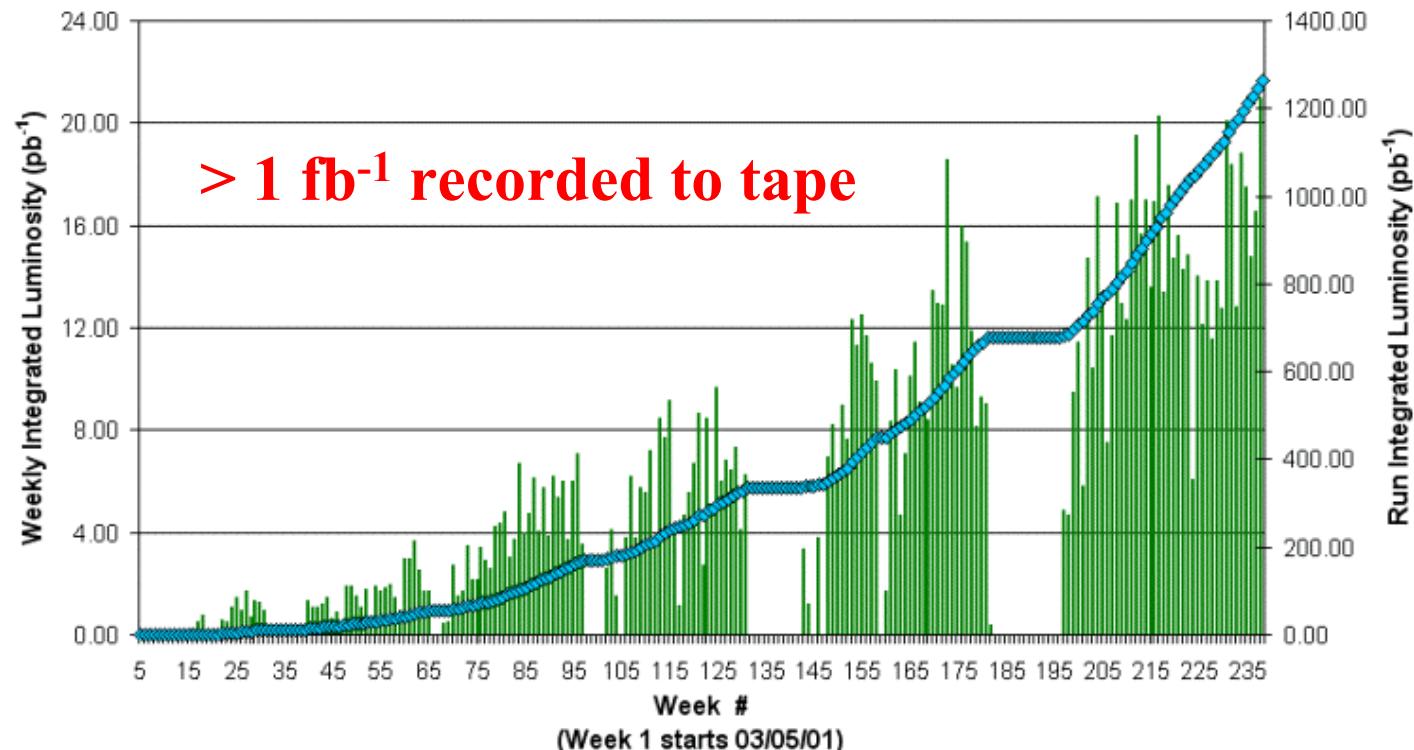
- **Tevatron is highest energy p-pbar collider in the world with CM energy of 1.96 TeV**
- **Weather is quite lovely this time of year!**



# Tevatron Performance

Green – weekly integrated luminosity  
Sky blue – run integrated luminosity

Collider Run II Integrated Luminosity



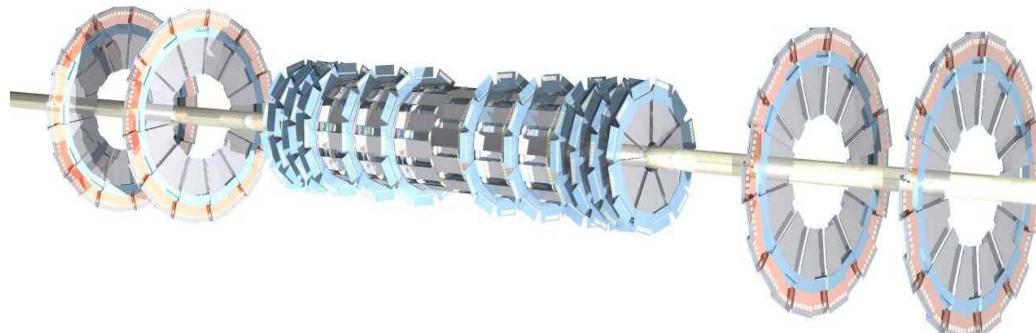
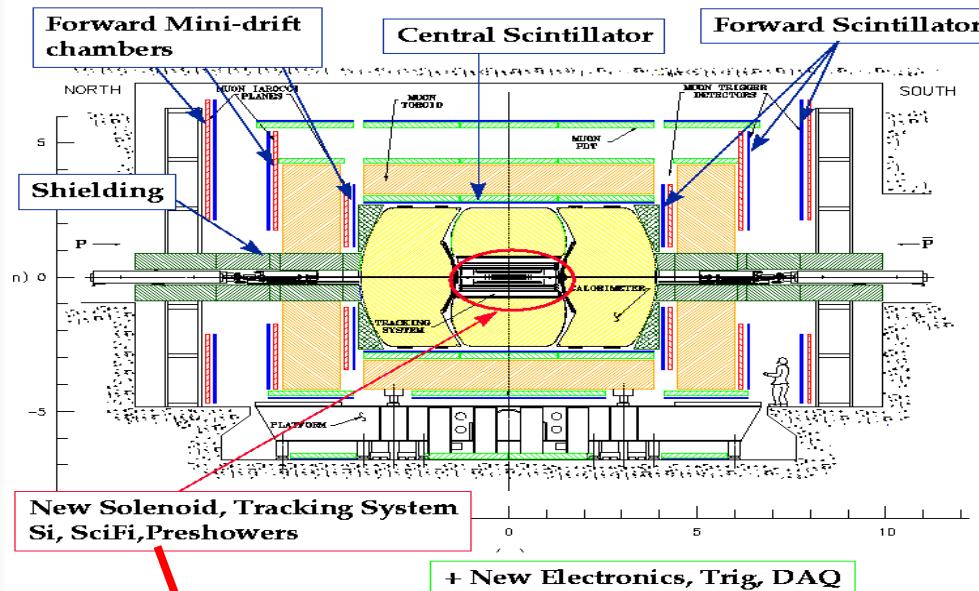
# The DØ Collaboration

- 19 Countries
- 86 institutions
- ~676 physicists





# The D $\emptyset$ Detector



## Silicon Microstrip Tracker

Clean Muon ID at  $|\eta| < 2$   
Compact Central Tracker  
( $r < 55$  cm)  
Good vertex resolution,  
Modest  $p$  resolution  
 $\sigma[M(\mu\mu)] = 70$  MeV at  $J/\psi$

- axial hit resolution:  $\sim 10 \mu\text{m}$
- z hit resolution:
  - $\sim 35 \mu\text{m}$  for  $90^\circ$  stereo
  - $\sim 450 \mu\text{m}$  for  $2^\circ$  stereo



# **Measurement of the $B_s^0$ Lifetime**

**We have measured the lifetime  
in a semileptonic decay channel**



# Measure $B_s$ Lifetime Using Decays

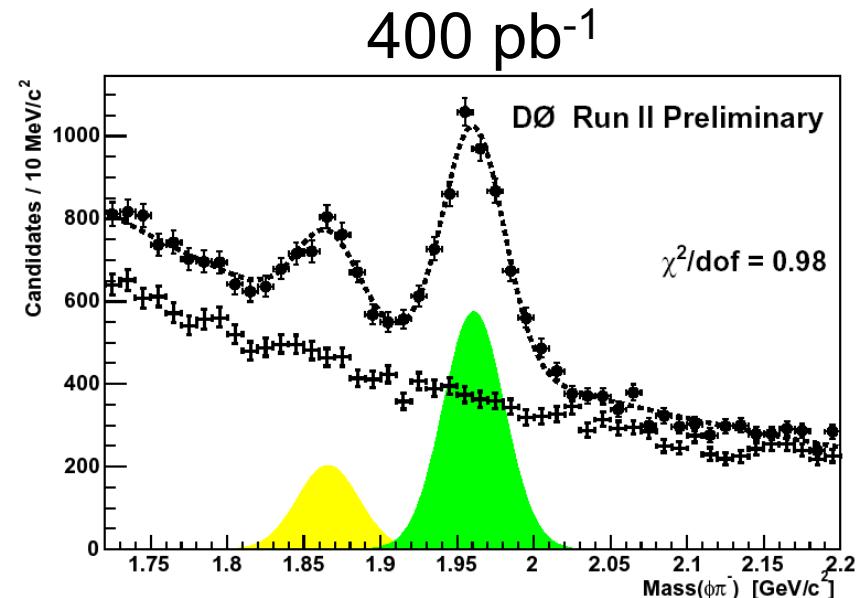
$$B_s \rightarrow D_s \mu X, D_s \rightarrow \phi \pi, \phi \rightarrow K\bar{K}$$

- Flavor-specific lifetime result used for constraining  $\Delta\Gamma/\Gamma$
- Shows we understand the systematics in  $B_s \rightarrow D_s \mu X$  decays for the  $\Delta m_s$  measurement



# Semileptonic $B_s$

- $B_s \rightarrow D_s \mu \nu X$ ,  $D_s \rightarrow \phi \pi$ ,  $\phi \rightarrow K K$
- Large data sample from muon triggers  $\sim 400 \text{ pb}^{-1}$
- Include  $B \rightarrow D_s D$ ,  $D \rightarrow \mu$  bkg (MC)
- Include charm background from gluon splitting (wide tails in ct)
- Signal channels



Sample Composition

25.4%  $B_s^0 \rightarrow D_s^- \mu^+ \nu X$   
67.7%  $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu X$   
2.4%  $B_s^0 \rightarrow D_{s0}^{*-} \mu^+ \nu X$   
4.5%  $B_s^0 \rightarrow D_{s1}^- \mu^+ \nu X$   
Total Br: 7.9 %



# Event Selection for Lifetime Analysis $B_s \rightarrow D_s \mu X$ , $D_s \rightarrow \phi \pi$ , $\phi \rightarrow K K$

## Standard selection

- Muon penetrating the toroid
- All tracks within same jet
- $\chi^2$  prob ( $D_s$ ) > 0.1%
- $\chi^2$  prob ( $B_s$ ) > 0.01%
- Helicity (D) > 0.4
- $L_{xy}$  (D) ·  $P_T$  (D) > 0
- $P_T(\mu) > 2.0$  GeV
- $P_T(K) > 1.0$  GeV
- $P_T(\pi) > 0.7$  GeV
- $P_T(D) > 3.5$  GeV
- $P_T(\mu$  w.r.t D) > 2 GeV
- $1.008 < M(\phi) < 1.032$  GeV
- $1.6 < M(D_s) < 2.3$  GeV
- $3.0 < M(B_s) < 5.0$  GeV

We make no  $L_{xy}$  cut because we are measuring the lifetime!



# B<sub>s</sub> Semileptonic Lifetime Fit

Unbinned maximum likelihood fitting components:

- Signal lifetime
- Background lifetimes
- Signal fraction from D<sub>s</sub> mass peak
- Momentum resolution, for each decay mode and type j, K<sub>j</sub>
- ct resolution scale factor
- 10 parameters

$$L = \prod_i^{N_s} [f_{sig} F_{sig}^i + (1 - f_{sig}) F_{bg}^i] \prod_j^{N_B} F_{bg}^j$$

$$c\tau = L_{xy} \frac{m(B_s)}{P_T(D_s \mu)} \times K$$

$$F_{sig}^i = \int dK H(K) \left[ \frac{K}{c\tau} e^{-K\lambda_j/c\tau} \otimes G \right]$$

$$F_{bg}^j = (1 - f_+ - f_{++} - f_-) G$$

$$+ f_+ \frac{e^{-\lambda_j/\lambda^+}}{\lambda^+} (\lambda_j \geq 0)$$

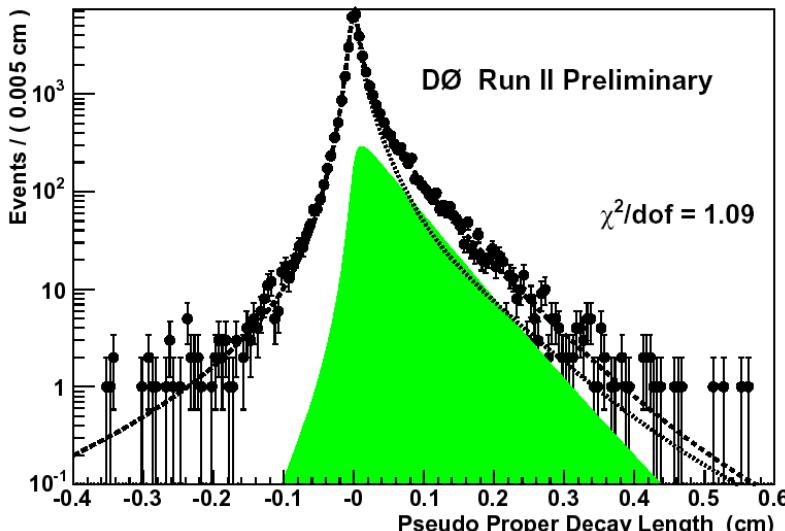
$$+ f_{++} \frac{e^{-\lambda_j/\lambda^{++}}}{\lambda^{++}} (\lambda_j \geq 0)$$

$$+ f_- \frac{e^{-\lambda_j/\lambda^-}}{\lambda^-} (\lambda_j < 0)$$



# B<sub>s</sub> Semileptonic Lifetime: Results

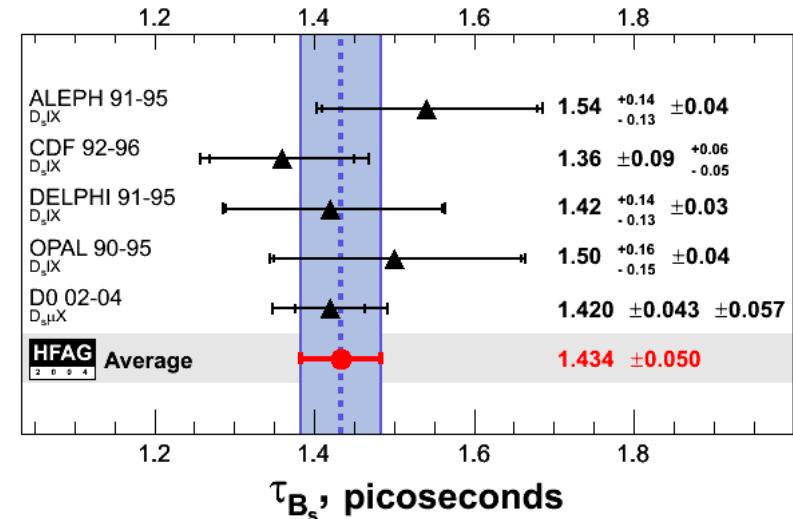
400 pb<sup>-1</sup>



Green: signal

Dotted line: background

$$\tau = 1.420 \pm 0.043 \text{ (stat)} \pm 0.057 \text{ (syst) ps}$$



World's best  
single measurement !

PDG World Average:  $1.442 \pm 0.066$  ps



# Lifetime Difference in the $B_s^0$ System



# Untagged $B_s$ Decay

$B_s \rightarrow J/\psi \phi$ ,  
Pseudoscalar  $\rightarrow$  Vector Vector decay

Three waves: S, P, D, or  $A_0$ ,  $A_{||}$ ,  $A_{\perp}$

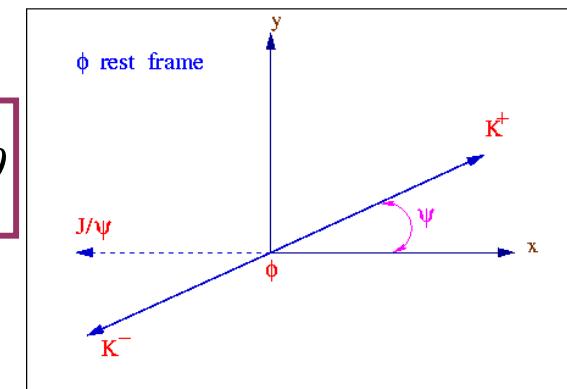
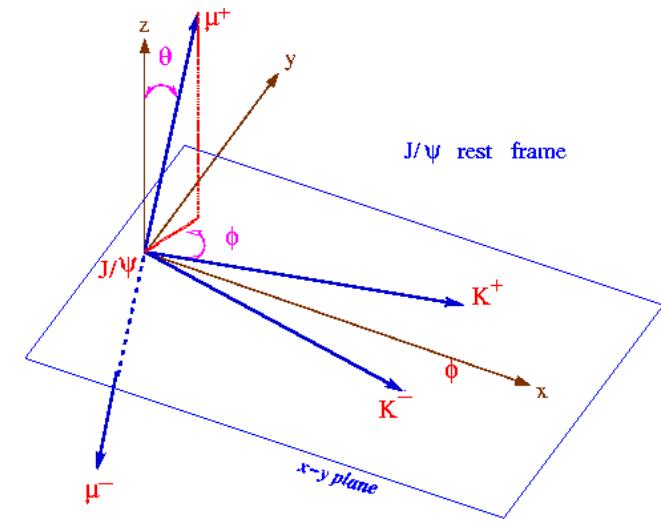
Both CP-even and CP-odd present, but well separated in transversity

S, D (Parity, CP even) :  
linear combination of  $A_0$ ,  $A_{||}$   
P (Parity, CP odd) :  $A_{\perp}$

$$\frac{d\Gamma(t)}{d\cos\theta} \propto \left( |A_0(t)|^2 + |A_{||}(t)|^2 \right) \frac{3}{8} \left( 1 + \cos^2 \theta \right) + |A_{\perp}(t)|^2 \left| \frac{3}{4} \sin^2 \theta \right|^2$$

Integral for flat efficiency in  $\phi, \psi$

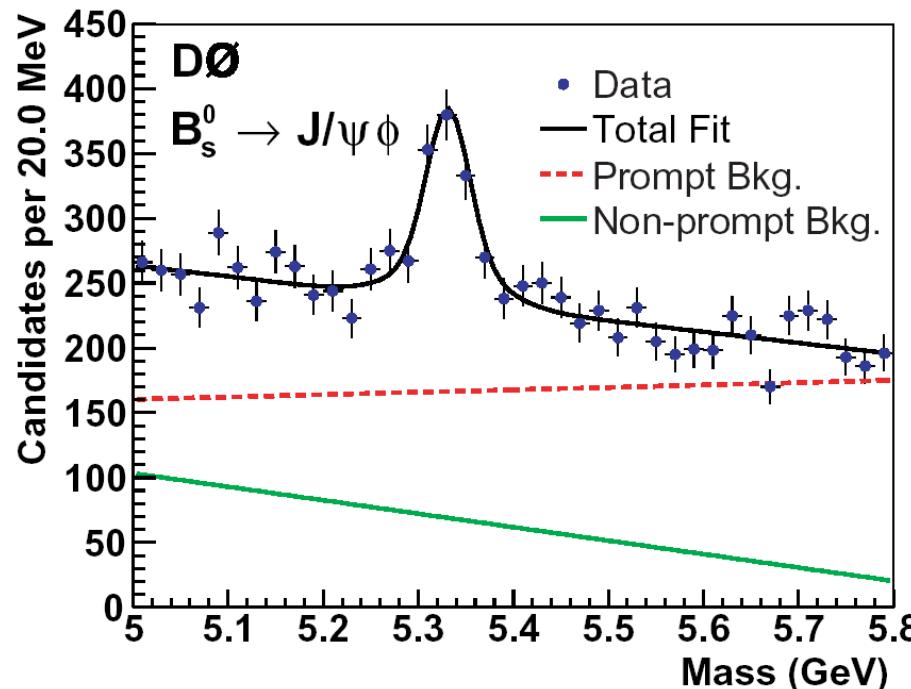
$\cos\theta = \text{transversity}$





# $B_s$ Lifetime Difference

- We measure TWO distinct lifetimes by fitting the time evolution and transversity distribution in untagged  $B_s \rightarrow J/\psi \phi$  decays
- If CP is conserved, they can be interpreted as the lifetimes of the two  $B_s$  mass eigenstates.



hep-ex/0507084



# Maximum Likelihood Fit

$$\mathcal{L} = \prod_{i=1}^N [f_{sig} \mathcal{F}_{sig}^i + (1 - f_{sig}) \mathcal{F}_{bck}^i]$$

Simultaneous fit to mass, proper decay length and transversity using an unbinned maximum log-likelihood method

- 19 parameters:**
- 1  $f_{sig}$  signal fraction
  - 2 signal mass, width
  - 1  $R_\perp$  CP-odd fraction at  $t = 0$
  - 1  $c\tau = c / \bar{\Gamma}$ ,  $\bar{\Gamma} = (\Gamma_L + \Gamma_H) / 2$
  - 1  $\Delta\Gamma / \bar{\Gamma}$
  
  - 2 bkg slope in mass ( 1 prompt, 1 long-lived )
  - 1  $\sigma (ct)$  scale
  - 6 bkg ct shape
  - 4 bkg transversity ( 2 prompt + 2 long-lived )



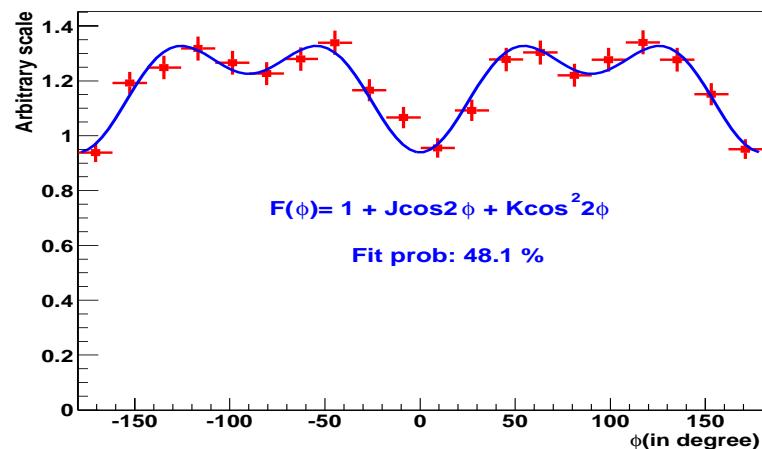
# Untagged $B_s$ Decay Rate in Time, Angles

$$\begin{aligned}
 \frac{d^3 \Gamma \rightarrow J/\psi (\rightarrow l^+ l^-) \phi (\rightarrow K^+ K^-)}{dcos\theta \, d\phi \, dcose\psi \, dt} \propto & \frac{9}{16\pi} \left[ 2|A_0(0)|^2 e^{-\Gamma_L t} \cos^2\psi (1 + \sin^2\theta \cos^2\phi) \right. \\
 & + \sin^2\psi \left\{ |A_{||}(0)|^2 e^{-\Gamma_L t} (1 + \sin^2\theta \sin^2\phi) + |A_{\perp}(0)|^2 e^{-\Gamma_H t} \sin^2\theta \right\} \\
 & + \frac{1}{\sqrt{2}} \sin 2\psi \left\{ |A_0(0)||A_{\perp}(0)| \cos(\delta_2 - \delta_1) e^{-\Gamma_L t} \sin^2\theta \sin^2 2\phi \right\} \\
 & + \left\{ \frac{1}{\sqrt{2}} |A_0(0)||A_{\perp}(0)| \cos \delta_2 \sin 2\psi \sin 2\theta \cos \phi \right\} \frac{1}{2} (e^{-\Gamma_H t} + e^{-\Gamma_L t}) \delta \phi \\
 & \left. - \left\{ \frac{1}{\sqrt{2}} |A_{||}(0)||A_{\perp}(0)| \cos \delta_1 \sin^2 \psi \sin 2\theta \sin \phi \right\} \frac{1}{2} (e^{-\Gamma_H t} + e^{-\Gamma_L t}) \delta \phi \right] H(\cos \psi) F(\phi) G(\cos \theta)
 \end{aligned}$$

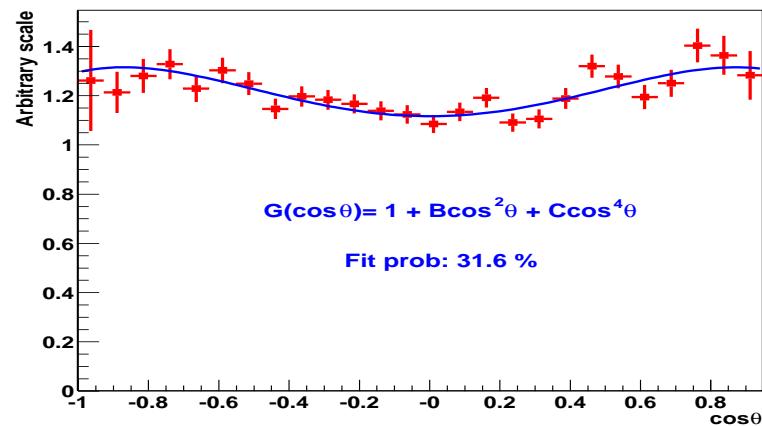


# Detector Acceptance (MC)

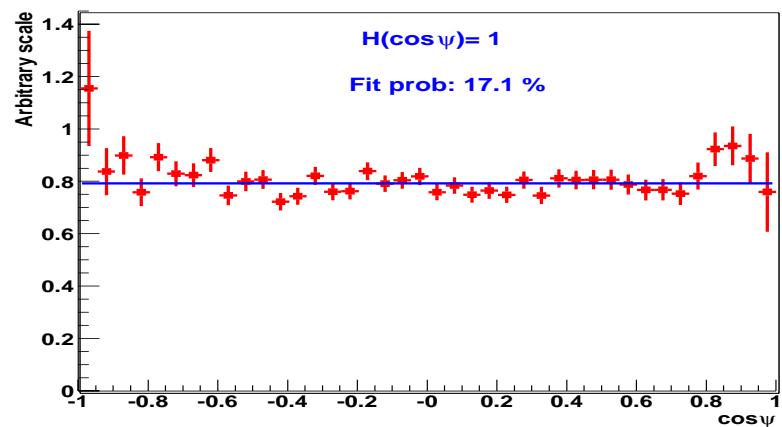
$$F(\phi) = 1 + J \cos(2\phi) + K \cos^2(2\phi)$$



$$G(\cos \theta) = 1 + B \cos^2 \theta + C \cos^4 \theta$$



$$H(\cos \psi) \text{ flat distribution}$$





# 3 Angles → 1 Angle

Inserting  $H(\cos\psi) = 1$ , and  $F(\phi) = 1 + J \cos(2\phi) + K \cos^2(2\phi)$ , and integrating over  $\cos\psi$  and  $\phi$ , we obtain a 1-angle time evolution:

$$\frac{d^3 \Gamma \rightarrow J/\psi (\rightarrow l^+ l^-) \phi (\rightarrow K^+ K^-)}{d \cos\theta dt} = N \pi \left[ (|A_0(0)|^2 + |A_{||}(0)|^2) e^{-\Gamma_L t} (1 + \cos^2\theta) \right.$$

$$+ \frac{K}{2} \left\{ (|A_0(0)|^2 + |A_{||}(0)|^2) e^{-\Gamma_L t} (1 + \cos^2\theta) \right. + 2 |A_\perp(0)|^2 e^{-\Gamma_H t} \sin^2\theta \Big\}$$

$$\left. - \frac{J}{2} (|A_0(0)|^2 - |A_{||}(0)|^2) e^{-\Gamma_L t} \sin^2\theta \right. + 2 |A_\perp(0)|^2 e^{-\Gamma_H t} \sin^2\theta \Big] G(\cos\theta)$$

$$|A_0(0)|^2 + |A_{||}(0)|^2 + |A_\perp(0)|^2 = 1$$

defining,  $R_\perp = |A_\perp(0)|^2$



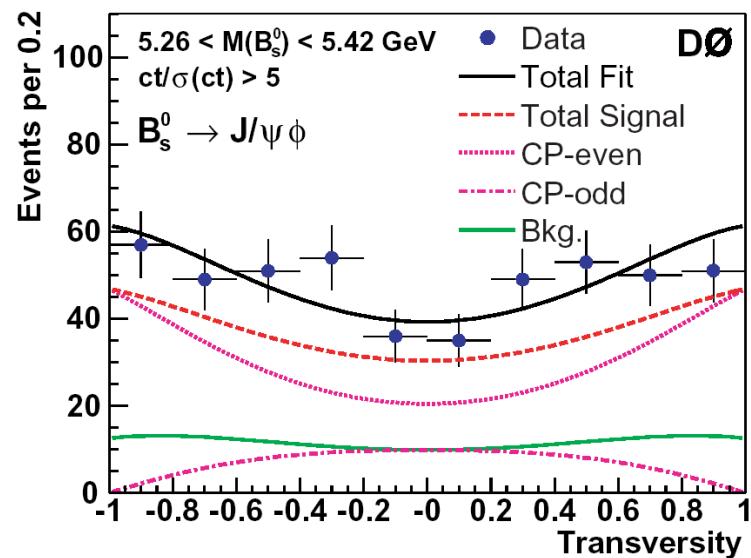
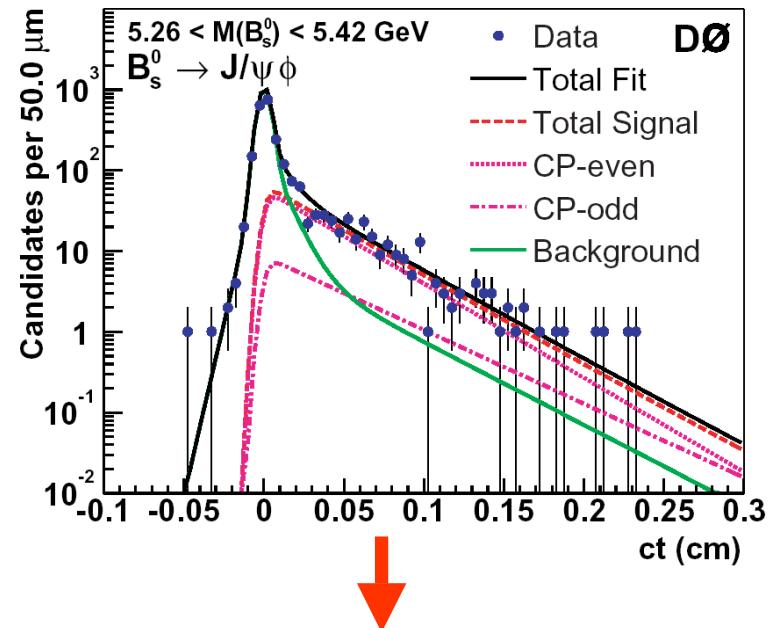
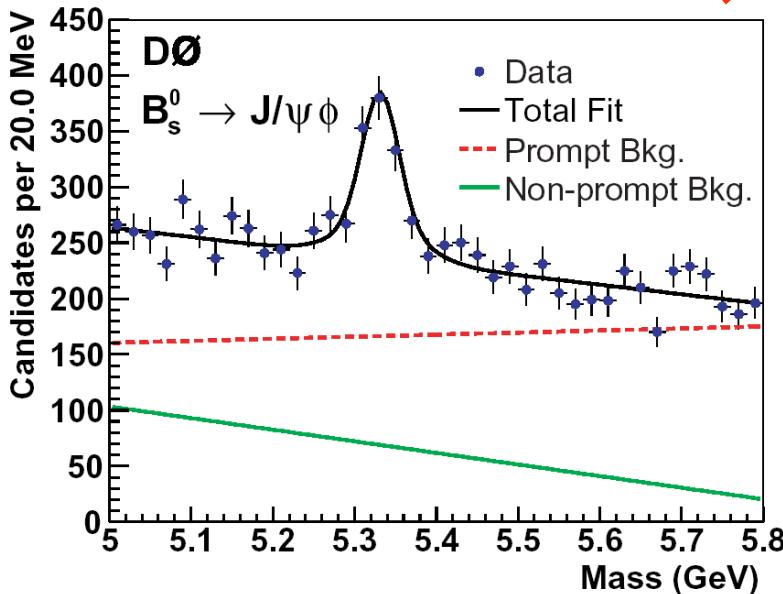
# $\Delta\Gamma$ Result

$$\bar{\tau}(B_s^0) = 1.39^{+0.13}_{-0.14} \pm 0.08 \text{ ps}$$

$$\frac{\Delta\Gamma}{\Gamma} = 0.21^{+0.27}_{-0.40} \pm 0.20$$

$$R_{\perp} = 0.17 \pm 0.10 \pm 0.02$$

Accepted by PRL !

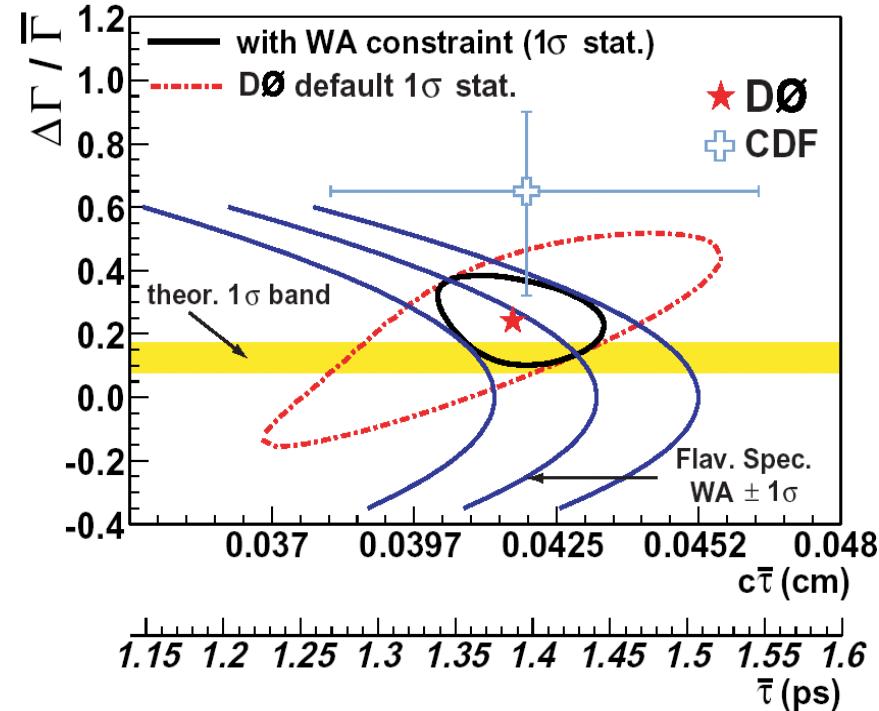




# $\Delta\Gamma$ Comparisons

- D0 and CDF  $\Delta\Gamma/\Gamma$  results are consistent
- D0 result is close to the theory prediction of  $0.12 \pm 0.05$

Including systematic errors:

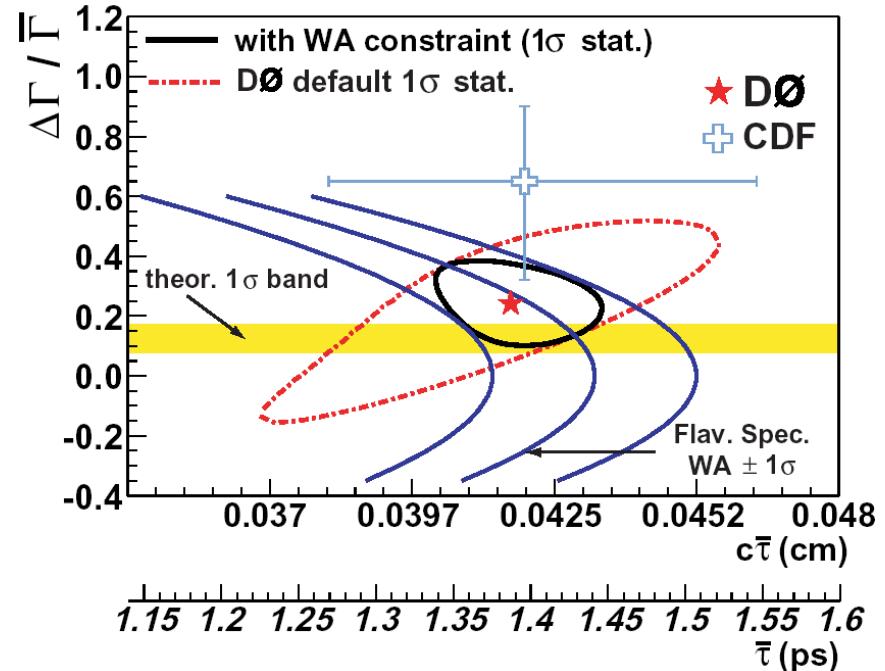


Experiment	$R_{\perp}$	$\Delta\Gamma/\Gamma$	$\bar{\tau}(ps)$	$\tau_L$	$\tau_H$
Aleph					$1.27 \pm 0.34$
CDF RunII	$0.125 \pm 0.08$	$0.65^{+0.25}_{-0.33}$	$1.40^{+0.15}_{-0.13}$	$1.05^{+0.16}_{-0.13}$	$2.07^{+0.58}_{-0.46}$
D0 RunII	$0.17 \pm 0.10$	$0.21^{+0.33}_{-0.45}$	$1.39^{+0.15}_{-0.16}$	$1.23^{+0.16}_{-0.13}$	$1.52^{+0.39}_{-0.43}$



# Constraint from Semileptonic Measurements

WA semileptonic (flavor specific) measurements provide an independent relation of  $\Delta\Gamma$  and  $\Gamma$ , leading to a significant improvement to  $\Delta\Gamma$



A single-lifetime fit applied to flavor specific final state measures  $\Gamma_{fs} = 1/\tau_{fs}$ :

$$\rightarrow \begin{aligned} \Gamma_{fs} &= \bar{\Gamma} \left( \frac{1 - (\Delta\Gamma / 2\bar{\Gamma})^2}{1 + (\Delta\Gamma / 2\bar{\Gamma})^2} \right) \\ \bar{\tau}_{fs} &= 1.43 \pm 0.05 \text{ ps} \\ \Rightarrow \frac{\Delta\Gamma}{\Gamma} &= 0.23 \quad {}^{+ 0.16}_{- 0.17} \end{aligned}$$



# $\Delta\Gamma/\Gamma$ Projections

