Measurement of direct photon pair production cross sections in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV

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We present a measurement of direct photon pair production cross sections using 4.2 fb$^{-1}$ of data collected with the D0 detector at the Fermilab Tevatron $p\bar{p}$ Collider. We measure single differential cross sections as a function of the diphoton mass, the transverse momentum of the diphoton system, the azimuthal angle between the photons, and the polar scattering angle of the photons. In addition, we measure double differential cross sections considering the last three kinematic variables in three diphoton mass bins. The results are compared with different perturbative QCD predictions and event generators.

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At a hadron collider, the direct photon pair (DPP) production with large diphoton invariant mass ($M_{\gamma\gamma}$) constitutes a large and irreducible background to searches for the Higgs boson decaying into a pair of photons, for both the Fermilab Tevatron [1] and the CERN LHC experiments [2]. DPP production is also a significant background in searches for new phenomena, such as new heavy resonances [3], extra spatial dimensions [4], or cascade decays of heavy new particles [5]. Thus, precise measurements of the diphoton differential production cross sections for various kinematic variables and their theoretical understanding are extremely important for future Higgs and new phenomena searches.

In addition, DPP production is interesting in its own right, and is used to check the validity of the predictions of perturbative quantum chromodynamics (pQCD) and soft-gluon resummation methods implemented in theoretical calculations. Measurements involving the diphoton final state have been previously carried out at fixed-target [6, 7] and collider [8–10] experiments. However,
the large integrated luminosity accumulated by the D0 experiment in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV at the Fermilab Tevatron Collider allows us to perform precise measurements of several observables in kinematic regions previously unexplored, as well as, for the first time, the measurement of double differential cross sections for this process.

The DPP events produced in $p\bar{p} \rightarrow \gamma\gamma + X$ are expected to be dominantly produced via $q\bar{q}$ scattering ($q\bar{q} \rightarrow \gamma\gamma$) and gluon-gluon fusion ($gg \rightarrow \gamma\gamma$) through a quark-loop diagram. In spite of the suppression factor of $\alpha_s^2$ for $gg \rightarrow \gamma\gamma$ as compared to $q\bar{q} \rightarrow \gamma\gamma$, the latter still gives a significant contribution in kinematic regions where the $gg$ parton luminosity is high, especially at low $M_{\gamma\gamma}$. Figure 1 shows the expected contribution to the total DPP rate from $gg \rightarrow \gamma\gamma$, as predicted by the PYTHIA [11] Monte Carlo (MC) event generator with the CTEQ6.1L parton distribution function (PDF) set [12]. In addition, direct photons may result from single or double fragmentation processes. The measured cross sections are compared to theoretical predictions from RESBOS [13], DIPHOS [14], and PYTHIA [11]. Both RESBOS and DIPHOS provide next-to-leading order (NLO) predictions in pQCD, however the $gg \rightarrow \gamma\gamma$ contribution is considered only at leading order (LO) in DIPHOS. PYTHIA is a parton shower MC event generator that includes the above processes at LO. In DIPHOS, the explicit parton-to-photon fragmentation functions are included at NLO, while in RESBOS a function approximating rate from the NLO fragmentation diagrams is introduced. Also, only in RESBOS, the effects of soft and collinear initial state gluon emissions are resummed to all orders. This is particularly important for the description of the $p_T^{\gamma\gamma}$ ($\Delta\phi_{\gamma\gamma}$) distribution, which is a delta-function at LO and diverges at NLO as $p_T^{\gamma\gamma} \rightarrow 0$ ($\Delta\phi_{\gamma\gamma} \rightarrow \pi$).

The D0 detector is a general purpose detector discussed in detail elsewhere [16]. The subdetectors most relevant to this analysis are the central tracking system, composed of a silicon microstrip tracker (SMT) and a central fiber tracker (CFT) embedded in a 2 T solenoidal magnetic field, the central preshower detector (CPS), and the calorimeter. The CPS is located immediately before the inner layer of the calorimeter and is formed of approximately one radiation length of lead absorber followed by three layers of scintillating strips. The calorimeter consists of a central section with coverage in pseudorapidity of $|\eta_{\text{det}}| < 1.1$ [15], and two end calorimeters covering up to $|\eta_{\text{det}}| \approx 4.2$. The electromagnetic (EM) section of the calorimeter is segmented longitudinally into four layers (EM$i$, $i = 1, 4$), with transverse segmentation into cells of size $\Delta\eta_{\text{det}} \times \Delta\phi_{\text{det}} = 0.1 \times 0.1$ [15], except EM3 (near the EM shower maximum), where it is $0.05 \times 0.05$. The calorimeter is well-suited for a precise measurement of the energy and direction of electrons and photons, providing an energy resolution of about 3.6% at an energy of 50 GeV and an angular resolution of about 0.01 radians. The energy response of the calorimeter to photons is calibrated using electrons from $Z$ boson decays. Since electrons and photons shower differently in matter, additional corrections as a function of $\eta$ are derived using a detailed GEANT-based [17] simulation of the D0 detector response. These corrections are largest $[2.0 - 2.5] \%$ at low photon energies ($\approx 20$ GeV). The data used in this analysis were collected using a combination of triggers requiring at least two clusters of energy in the EM calorimeter with loose shower shape requirements and varying $p_T$ thresholds between 15 GeV and 25 GeV, and correspond to an integrated luminosity of $4.2 \pm 0.3 \, \text{fb}^{-1}$ [18].

Events are selected by requiring two photon candidates...
with transverse momentum $p_T > 21$ (20) GeV for the highest (next-to-highest) $p_T$ photon candidate and pseudorapidity $|\eta| < 0.9$, for which the trigger requirements are >96% efficient. The minimum $p_T$ requirements for the two photon candidates are different in order to minimize the impact of the kinematic region $p_T^\gamma \gamma \to 0$, where the NLO calculation is divergent. The photon $p_T$ is computed with respect to the reconstructed event primary vertex (PV) with the highest number of associated tracks. The PV is required to be within 60 cm of the center of the detector along the beam axis. The PV has a reconstruction efficiency of about 98% and has about 65% probability of being the correct vertex corresponding to the hard $p\bar{p} \to \gamma\gamma + X$ production.

Photon candidates are formed from clusters of calorimeter cells within a cone of radius $R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} = 0.4$ around a seed tower [16]. The final cluster energy is then recalculated from the inner core with $R = 0.2$. The photon candidates are selected by requiring: (i) $\geq 97\%$ of the cluster energy be deposited in the EM calorimeter layers; (ii) the calorimeter isolation $I = [E_{\text{cal}}(0.4) - E_{\text{EM}}(0.2)]/E_{\text{EM}}(0.2) < 0.10$, where $E_{\text{cal}}(R)/E_{\text{EM}}(R)$ is the total [EM only] energy in a cone of radius $R$; (iii) the $p_T$ scalar sum of all tracks originating from the PV in an annulus of $0.05 < R < 0.4$ around the EM cluster be $< 1.5$ GeV; and (iv) the energy-weighted EM shower width be consistent with that expected for an electromagnetic shower. To suppress electrons misidentified as photons, the EM clusters are required to not be spatially matched to significant tracker activity, either a reconstructed track or a density of hits in the SMT and CFT consistent with that of an electron [19]. In the following, this requirement will be referred to as the “track-match veto”.

To further suppress jets misidentified as photons, an artificial neural network (NN) discriminant which exploits differences in tracker activity and energy deposits in the calorimeter and in the CPS between photons and jets is defined [1]. The NN is trained using $\gamma$ and jet PYTHIA MC samples and its performance is verified using a data event sample consisting of photons radiated from charged leptons in $Z$ boson decays ($Z \to \ell^+\ell^-\gamma$, $\ell = e, \mu$) [20]. The NN output ($O_{NN}$) distributions, normalized to unit area and obtained after applying all data selection criteria, are shown in Fig. 2 for photons in data and MC and jets in MC. The $O_{NN}$ shapes for photons in data and MC are in good agreement. They exhibit a significant separation from the shape of the ONN for misidentified jets, which is validated with data on another sample in Fig. 3 (see below). Photon candidates are required to have $O_{NN} > 0.3$, which is $\approx 98\%$ efficient for photons and rejects $\approx 40\%$ of the jets misidentified as photons.

Finally, the two photon candidates are required to be spatially separated from each other by a distance in $\eta - \phi$ space $\Delta R > 0.4$ and to satisfy $M_{\gamma\gamma} > p_T^\gamma\gamma$. The latter requirement is satisfied by the majority ($\approx 92\%$) of DPP events and, together with the photon isolation requirements, allows significant suppression of the contribution from the fragmentation diagrams, thus restricting the data-to-theory comparison to the region where the theoretical calculations should have smaller uncertainties [13].

After imposing all requirements, 10938 events with diphoton candidates are selected in data. This sample includes instrumental background contributions from $\gamma$+jet and dijet production, where a jet is misidentified as a single photon as a result of fluctuations in the parton fragmentation into a well-isolated neutral meson ($\pi^0$ or $\eta$) decaying into a final state with two or more photons. An additional smaller background contribution results from $Z$-boson/Drell-Yan production events $Z/\gamma_{\ast} \to e^+e^-$ (ZDY) in which both electrons are misidentified as photons.

The contribution from ZDY events is estimated using the MC simulation with PYTHIA, normalized to the NNLO cross section [21]. The selection efficiencies determined from the MC simulation are corrected to those measured in the data. On average, each electron has a 2% probability of satisfying the photon selection criteria, mainly due to the inefficiency of the track-match veto requirements. The total ZDY contribution is estimated to be $161 \pm 20$ events. Backgrounds due to $\gamma$+jet and dijet events are estimated from data by using a $4 \times 4$ matrix background estimation method [1]. After applying all of the selection criteria described above, a tighter $O_{NN}$ requirement ($O_{NN} > 0.6$) is used to classify the data events into four categories, depending on whether both photon candidates, only the highest $p_T$ one, only the next-to-highest $p_T$ one, or neither of the two photon candidates pass ($p$) or fail ($f$) this requirement. The corresponding number of events (after subtraction of the estimated ZDY contribution) compose a 4-component vector $(N_{pp}, N_{pf}, N_{fp}, N_{ff})$.

![FIG. 2: Comparison of the normalized $O_{NN}$ spectra for photons from DPP MC and $Z \to \ell^+\ell^-\gamma$ data and for misidentified jets from dijet MC.](image-url)
The difference in relative efficiencies of the $O_{NN} > 0.6$ requirement between photons and jets allows estimation of the sample composition by solving a linear system of equations: \((N_{pp}, N_{pf}, N_{fp}, N_{jj})^T = E \times (N_{\gamma\gamma}, N_{\gamma j}, N_{j\gamma}, N_{jj})^T\), where \(N_{\gamma\gamma}\) (\(N_{jj}\)) is the number of DPP (dijet) events and \(N_{\gamma j}\) (\(N_{j\gamma}\)) is the number of \(\gamma + j\) events with the (next-to-)highest \(p_T\) photon candidate being a photon. The \(4 \times 4\) matrix \(E\) contains the photon \(\varepsilon_\gamma\) and jet \(\varepsilon_{\text{jet}}\) efficiencies, estimated using photon and jet MC samples and validated in data. The efficiencies are parameterized as a function of the photon candidate \(\eta\) and vary within \((90 - 95)\%\) for \(\varepsilon_\gamma\), and within \((66 - 70)\%\) for \(\varepsilon_{\text{jet}}\). The systematic uncertainty on \(\varepsilon_\gamma\) is estimated to be 1.5% from a comparison of the efficiency as a function of \(\eta\) between data and MC using samples of electrons from Z boson decays and photons from radiative Z boson decays. In order to estimate the systematic uncertainty on \(\varepsilon_{\text{jet}}\), two independent control data samples enriched in jets misidentified as photons are selected, either by inverting the photon isolation variable \((I > 0.07)\), or by requiring at least one track in a cone of \(R < 0.05\) around the photon, while keeping the remaining photon selection criteria unchanged. In both cases the agreement with the MC prediction for \(\varepsilon_{\text{jet}}\) is found to be within 10%, which is taken as the systematic uncertainty. Figure 3 compares the shape of the \(O_{NN}\) distribution between data and MC for jets misidentified as photons selected by requiring \(I > 0.07\). The MC simulation is found to provide a fair description of the shape of this distribution. The total number of DPP events is found to be \(N_{\gamma\gamma} = 7307 \pm 312\) (stat.), corresponding to an average DPP purity of \(\approx 67\%\). Following this procedure, the number of DPP events is estimated in each bin of the four kinematic variables considered \((M_{\gamma\gamma}, p_T^{\gamma\gamma}, \Delta\phi_{\gamma\gamma}, \text{and } |\cos \theta^*|)\). The largest kinematic dependence of the DPP purity is in terms of \(M_{\gamma\gamma}\), with a variation between \(\approx 60\%\) at \(M_{\gamma\gamma} \approx 40\) GeV and close to 100% for \(M_{\gamma\gamma} > 200\) GeV. As a function of the other kinematic variables, the DPP purity varies in the \((60 - 70)\%\) range. The relative systematic uncertainty on the purity results from the systematic uncertainties on \(\varepsilon_\gamma\) and \(\varepsilon_{\text{jet}}\), and typically varies within \((11 - 15)\%\). As a cross-check, the DPP purity was also estimated via a fit to the two-dimensional distribution in data of \(O_{NN,\gamma\gamma}\) versus \(O_{NN,j\gamma}\) using templates constructed from photons and jets in MC. The result was found to be in good agreement with that from the \(4 \times 4\) matrix method.

The estimated number of DPP events per bin is corrected for the DPP event selection efficiency and acceptance. The selection efficiency is calculated using DPP events generated with RESBOS and processed through a GEANT-based simulation of the D0 detector. In order to accurately model the effects of multiple \(p\bar{p}\) interactions and detector noise, data events from random \(p\bar{p}\) crossings with a similar instantaneous luminosity spectrum as considered in the data analysis are overlaid on the MC events. These MC events are then processed using the same reconstruction code as for the data. Small differences between data and MC in the per-photon selection efficiencies are corrected for with suitable scale factors derived using control samples of electrons from Z boson decays, as well as photons from the radiative Z boson decays. The overall DPP selection efficiency after applying all selection criteria is estimated as a function of the variable of interest. In the case of \(p_T^{\gamma\gamma}, \Delta\phi_{\gamma\gamma}, \text{and } |\cos \theta^*|\), it is about 64% with a \((2 - 3)\%\) variation across the bins, while for \(M_{\gamma\gamma}\), the efficiency grows from about 60% at \(30 < M_{\gamma\gamma} < 50\) GeV to 69% at \(M_{\gamma\gamma} > 200\) GeV. The total relative systematic uncertainty on the DPP selection efficiency is \(4.3\%\), dominated by the track-match veto and photon \(O_{NN}\) selections. The acceptance is calculated using DPP events generated with RESBOS and is driven by the selections in \(W_{\text{det}} (|W_{\text{det}}| < 0.9\), applied to avoid edge effects in the central calorimeter region used for the measurement) and \(\phi_{\text{det}}\) (to avoid periodic calorimeter module boundaries [16] that bias the EM cluster energy and position measurements), PV misidentification, photon energy scale, and bin-to-bin migration effects due to the finite energy and angular resolution of the EM calorimeter. The overall DPP acceptance varies within \((45 - 64)\%\) with a relative systematic uncertainty of \((4 - 7)\%\).

The differential cross sections \(\frac{d\sigma}{dM_{\gamma\gamma}}, \frac{d\sigma}{dp_T^{\gamma\gamma}}, \frac{d\sigma}{d\Delta\phi_{\gamma\gamma}}, \text{and } \frac{d\sigma}{d|\cos \theta^*|}\) are obtained from the number of data events corrected for the background contribution, divided by the trigger, vertex and diphoton selection efficiencies, acceptance, integrated luminosity, and the bin width for each kinematic variable. The measured differential cross sections, compared to the theoretical predictions from RESBOS, are presented in Table I. The average value for each variable in a bin was estimated using RESBOS. The statistical uncertainty \(\delta_{\text{stat}}\) corresponds to the statistical precision on \(N_{\gamma\gamma}\) estimated in the \(4 \times 4\) matrix method, which can be sizable when values of \(\varepsilon_\gamma\) and \(\varepsilon_{\text{jet}}\) are numerically close.
Figure 4 shows a comparison of the measured differential cross sections to the theoretical predictions from RESBOS, DIPHOX, and PYTHIA. Systematic uncertainties in the measured cross sections have large (> 90%) bin-to-bin correlations. There is a common 7.4% normalization uncertainty, resulting from the photon selection criteria (4.3%) and luminosity measurement (6.1%), that is not shown on the data points. The predictions from RESBOS and DIPHOX are computed using the CTEQ6.6M PDF set [12], the DSS set of fragmentation functions [22], and setting renormalization \( \mu_R \), factorization \( \mu_F \), and fragmentation \( \mu_f \) scales as \( \mu_R = \mu_F = \mu_f = M_{\gamma\gamma} \).

The uncertainty due to the scale choice is estimated by simultaneous variation by a factor of two of all scales relative to the default choice and found to be about 10% for \( M_{\gamma\gamma} \) and \( |\cos \theta^*| \) and up to (15 – 20)% for high \( p_T^{\gamma} \) and low \( \Delta \phi_{\gamma\gamma} \). The PDF uncertainty is estimated using DIPHOX and the 44 eigenvectors provided with the CTEQ6.6M PDF set [12] and found to be within (3 – 6)% for all four cross sections. The predictions from PYTHIA are computed with “Tune A” [11], which uses the CTEQ5L PDF set. All theoretical predictions are obtained using diphoton event selection criteria equivalent to those applied in the experimental analysis. In particular, the photon isolation is required to be \( E_T^{\text{iso}} = E_T^{\text{ph}}(0.4) - E_T^{\gamma} \) < 2.5 GeV, where \( E_T^{\text{tot}}(0.4) \) is the total transverse energy within a cone of radius \( R = 0.4 \) centered on the photon, and \( E_T^{\gamma} \) is the photon transverse energy. For RESBOS and DIPHOX, \( E_T^{\text{tot}} \) is computed at the parton level, whereas in the case of PYTHIA, it is computed at the particle level. This requirement suppresses the contributions from photons produced in the fragmentation processes and leads to a more consistent comparison with the experimental result. Studies performed using DIPHOX indicate that the contribution to the overall cross section from one- and two-fragmentation processes does not exceed 16% and significantly drops at large \( M_{\gamma\gamma} \), \( p_T^{\gamma} \) and small \( \Delta \phi_{\gamma\gamma} \) to (1–3)%.

In order to allow a direct comparison to the data, the NLO QCD cross sections obtained with RESBOS and DIPHOX are further corrected for contributions from multiple parton interactions and hadronization, both of which affect the efficiency of the isolation requirement. These corrections are estimated using DPP events simulated in PYTHIA using Tunes A and S0 [11]. The corrections vary within (4.0 – 5.5)% as a function of the measured kinematic variables and are consistent for both tunes within 0.5%.

The results obtained show that none of the theoretical predictions considered is able to describe the data well in all kinematic regions of the four variables. RESBOS shows the best agreement with data, although systematic discrepancies are observed at low \( M_{\gamma\gamma} \), high \( p_T^{\gamma} \), and low \( \Delta \phi_{\gamma\gamma} \). However, the agreement between RESBOS and data is fair at intermediate \( M_{\gamma\gamma} \) (50 – 80 GeV), and good at high \( M_{\gamma\gamma} \) (> 80 GeV). The large discrepancy between RESBOS and DIPHOX in some regions of the phase space is due to absence of all-order soft-gluon resummation and accounting \( gg \to \gamma \gamma \) contribution just at LO in DIPHOX.

<table>
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<th>( \langle p_T^{\gamma} \rangle ) (GeV)</th>
<th>( \Delta \phi_{\gamma\gamma} ) (rad)</th>
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<td>120 – 150</td>
<td>132.9</td>
<td>3.65 × 10^{-3}</td>
<td>120 +16/14</td>
<td>4.52 × 10^{-3}</td>
<td></td>
</tr>
<tr>
<td>150 – 200</td>
<td>170.7</td>
<td>1.67 × 10^{-3}</td>
<td>150 +16/14</td>
<td>1.74 × 10^{-3}</td>
<td></td>
</tr>
<tr>
<td>200 – 350</td>
<td>248.8</td>
<td>3.30 × 10^{-4}</td>
<td>200 +16/14</td>
<td>3.53 × 10^{-4}</td>
<td></td>
</tr>
</tbody>
</table>

Further insight on the dependence of the \( p_T^{\gamma} \), \( \Delta \phi_{\gamma\gamma} \), and \( |\cos \theta^*| \) kinematic distributions on the mass scale can be gained through the measurement of double differential cross sections. For this purpose, the differential cross sections as functions of \( p_T^{\gamma\gamma} \), \( \Delta \phi_{\gamma\gamma} \), and \( |\cos \theta^*| \) are
measured in three $M_{\gamma\gamma}$ bins: 30 – 50 GeV, 50 – 80 GeV and 80 – 350 GeV. The results are presented in Tables II – IV, corresponding to each of the three $M_{\gamma\gamma}$ intervals. Each table is split into three sub-tables, showing results separately for $d^2\sigma/dM_{\gamma\gamma}dp_T^{\gamma\gamma}$, $d^2\sigma/dM_{\gamma\gamma}d\Delta\phi_{\gamma\gamma}$, and $d^2\sigma/dM_{\gamma\gamma}d|\cos \theta^*|$. The measured cross sections for the $p_T^{\gamma\gamma}$, $\Delta\phi_{\gamma\gamma}$, and $|\cos \theta^*|$ variables in the three mass bins are shown in Figs. 5 – 7 and compared to the theoretical predictions. These results confirm that the largest discrepancies between data and RESBOS for each of the kinematic variables originate from the lowest $M_{\gamma\gamma}$ region ($M_{\gamma\gamma} < 50$ GeV). As shown in Fig. 1, this is the region where the contribution from $gg \to \gamma\gamma$ is expected to be largest. The discrepancies between data and RESBOS are reduced in the intermediate $M_{\gamma\gamma}$ region (50 – 80 GeV), and a quite satisfactory description of all kinematic variables is achieved for the $M_{\gamma\gamma} > 80$ GeV region, the relevant region for the Higgs boson and new phenomena searches. However, it should be pointed out that at the Tevatron, DPP production at high masses is strongly dominated by $q\bar{q}$ annihilation, in contrast with the LHC, where the contribution from $gg$ and $qg$ initiated process will be significant. It remains to be seen whether the addition of NNLO corrections to RESBOS, as done in [23], will improve the description of the high $p_T^{\gamma\gamma}$ (low $\Delta\phi_{\gamma\gamma}$) spectrum at low $M_{\gamma\gamma}$.

FIG. 4: The measured differential diphoton production cross sections as functions of (a) $M_{\gamma\gamma}$, (b) $p_T^{\gamma\gamma}$, (c) $\Delta\phi_{\gamma\gamma}$, and (d) $|\cos \theta^*|$. The data are compared to the theoretical predictions from RESBOS, DIPHOX, and PYTHIA. The predictions from RESBOS, and DIPHOX use the CTEQ6.6M PDF set [12] and renormalization, factorization, and fragmentation scales $\mu_R = \mu_F = \mu_t = M_{\gamma\gamma}$, while PYTHIA uses the Tune A settings. Theoretical predictions are obtained using the following selections: two photons with $p_T > 21(20)$ GeV, $|\eta| < 0.9$, 30 < $M_{\gamma\gamma} <$ 350 GeV, $M_{\gamma\gamma} > 50$ GeV, $50 < \Delta\phi_{\gamma\gamma} < 90$, $\Delta\phi_{\gamma\gamma} > 350$, $\Delta\phi_{\gamma\gamma} > 0.4$, $\Delta\phi_{\gamma\gamma} > 0.5\pi$, and $E_T^{\text{iso}} < 2.5$ GeV. The ratio of differential cross sections between data and RESBOS are displayed as black points with uncertainties in the bottom plots. The inner line for the uncertainties in data points shows the statistical uncertainty, while the outer line shows the total (statistical and systematic added in quadrature) uncertainty after removing the 7.4% normalization uncertainty. The solid (dashed) line shows the ratio of the predictions from DIPHOX (PYTHIA) to those from RESBOS. In the bottom plots, the scale uncertainties are shown by dash-dotted lines and the PDF uncertainties by shaded regions.
FIG. 5: The measured double differential diphoton production cross sections as functions of (a) $p_T^\gamma$, (b) $\Delta \phi_{\gamma\gamma}$, and (c) $|\cos \theta^*|$ for $30 < M_{\gamma\gamma} < 50$ GeV. The notations for points, lines and shaded regions are the same as in Fig. 4.

FIG. 6: The measured double differential diphoton production cross sections as functions of (a) $p_T^\gamma$, (b) $\Delta \phi_{\gamma\gamma}$, and (c) $|\cos \theta^*|$ for $50 < M_{\gamma\gamma} < 80$ GeV. The notations for points, lines and shaded regions are the same as in Fig. 4.

FIG. 7: The measured double differential diphoton production cross sections as functions of (a) $p_T^\gamma$, (b) $\Delta \phi_{\gamma\gamma}$, and (c) $|\cos \theta^*|$ for $80 < M_{\gamma\gamma} < 350$ GeV. The notations for points, lines and shaded regions are the same as in Fig. 4.
In summary, we have presented measurements of single and double differential cross sections for DPP production in \( p\bar{p} \) collisions at \( \sqrt{s} = 1.96 \) TeV. This analysis uses 4.2 fb\(^{-1}\) of D0 data, representing a twenty-fold increase in statistics relative to the last published Tevatron results \([10]\). The measured cross sections are compared to predictions from RESBOS, DIPHOX and PYTHIA, showing the necessity of including higher order corrections beyond NLO as well as the resummation to all orders of soft and collinear initial state gluons. These results allow the tuning of the theoretical predictions for this process, which is of great relevance for improving the sensitivity of searches for the Higgs boson and other new phenomena at the Tevatron and the LHC.

**TABLE II:** The measured double differential cross sections in bins of \( p_T^{\gamma\gamma} \), \( \Delta \phi_{\gamma\gamma} \), and \( |\cos \theta'| \), in the region 30 < \( M_{\gamma\gamma} \) < 50 GeV. The columns \( \delta_{\text{stat}} \) and \( \delta_{\text{sysyst}} \) represent the statistical and systematic uncertainties, respectively. Also shown are the predictions from RESBOS.

| \( p_T^{\gamma\gamma} \) (GeV) | \( \Delta \phi_{\gamma\gamma} \) (rad) | \( |\cos \theta'| \) | \( d^2\sigma / dM_{\gamma\gamma} dp_T^{\gamma\gamma} \) (pb/GeV\(^2\)) | Data | \( \delta_{\text{stat}} \) (%) | \( \delta_{\text{sysyst}} \) (%) | RESBOS |
|----------------|----------------|----------|----------------|-------|----------------|----------------|----------|
| 0.0 – 5.0      | 2.4            | 1.98     | 5.11 x 10\(^{-3}\) | 15    | +17/–14        | 4.64 x 10\(^{-3}\) | 17        |
| 5.0 – 10.0     | 7.0            | 2.17     | 3.65 x 10\(^{-3}\) | 18    | +16/–14        | 2.35 x 10\(^{-3}\) | 18        |
| 10.0 – 15.0    | 12.2           | 2.17     | 8.17 x 10\(^{-3}\) | 19    | +16/–14        | 8.72 x 10\(^{-3}\) | 18        |
| 15.0 – 50.0    | 23.4           | 3.58     | 1.57 x 10\(^{-3}\) | 19    | +16/–14        | 1.67 x 10\(^{-3}\) | 18        |

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**TABLE III:** The measured double differential cross sections in bins of \( p_T^{\gamma\gamma} \), \( \Delta \phi_{\gamma\gamma} \), and \( |\cos \theta'| \), in the region 50 < \( M_{\gamma\gamma} \) < 80 GeV. The notations are the same as in Table II.

| \( p_T^{\gamma\gamma} \) (GeV) | \( \Delta \phi_{\gamma\gamma} \) (rad) | \( |\cos \theta'| \) | \( d^2\sigma / dM_{\gamma\gamma} dp_T^{\gamma\gamma} \) (pb/GeV\(^2\)) | Data | \( \delta_{\text{stat}} \) (%) | \( \delta_{\text{sysyst}} \) (%) | RESBOS |
|----------------|----------------|----------|----------------|-------|----------------|----------------|----------|
| 5.0 – 10.0     | 7.3            | 4.92     | 9.12 x 10\(^{-3}\) | 12    | +16/–14        | 4.06 x 10\(^{-3}\) | 19        |
| 10.0 – 15.0    | 12.3           | 2.93     | 9.12 x 10\(^{-3}\) | 14    | +16/–14        | 2.33 x 10\(^{-3}\) | 19        |
| 15.0 – 20.0    | 17.3           | 1.86     | 9.12 x 10\(^{-3}\) | 18    | +16/–14        | 1.29 x 10\(^{-3}\) | 19        |
| 20.0 – 30.0    | 24.1           | 8.22     | 9.12 x 10\(^{-3}\) | 18    | +16/–14        | 5.81 x 10\(^{-4}\) | 18        |
| 30.0 – 80.0    | 39.8           | 1.34     | 9.12 x 10\(^{-3}\) | 17    | +16/–14        | 6.81 x 10\(^{-5}\) | 18        |

**TABLE IV:** The measured double differential cross sections in bins of \( p_T^{\gamma\gamma} \), \( \Delta \phi_{\gamma\gamma} \), and \( |\cos \theta'| \), in the region 80 < \( M_{\gamma\gamma} \) < 350 GeV. The notations are the same as in Table II.

| \( p_T^{\gamma\gamma} \) (GeV) | \( \Delta \phi_{\gamma\gamma} \) (rad) | \( |\cos \theta'| \) | \( d^2\sigma / dM_{\gamma\gamma} dp_T^{\gamma\gamma} \) (pb/GeV\(^2\)) | Data | \( \delta_{\text{stat}} \) (%) | \( \delta_{\text{sysyst}} \) (%) | RESBOS |
|----------------|----------------|----------|----------------|-------|----------------|----------------|----------|
| 1.57 – 2.20    | 1.98           | 6.19     | 9.12 x 10\(^{-3}\) | 25    | +16/–14        | 2.99 x 10\(^{-3}\) | 19        |
| 2.20 – 2.51    | 2.38           | 1.94     | 9.12 x 10\(^{-3}\) | 20    | +16/–14        | 1.16 x 10\(^{-2}\) | 19        |
| 2.51 – 2.67    | 2.60           | 4.49     | 9.12 x 10\(^{-3}\) | 20    | +16/–14        | 2.56 x 10\(^{-3}\) | 19        |
| 2.67 – 2.83    | 2.76           | 6.64     | 9.12 x 10\(^{-3}\) | 16    | +16/–14        | 4.87 x 10\(^{-2}\) | 19        |
| 2.83 – 2.98    | 2.92           | 1.18     | 9.12 x 10\(^{-3}\) | 14    | +16/–14        | 1.04 x 10\(^{-3}\) | 20        |
| 2.98 – 3.14    | 3.07           | 2.30     | 9.12 x 10\(^{-3}\) | 10    | +16/–14        | 2.47 x 10\(^{-3}\) | 19        |
[15] The polar angle $\theta$ and the azimuthal angle $\phi$ are defined with respect to the positive $z$ axis, which is along the proton beam direction. Pseudorapidity is defined as $\eta = -\ln[tan(\theta/2)]$. Also, $\eta_{\text{det}}$ and $\phi_{\text{det}}$ are the pseudorapidity and the azimuthal angle measured with respect to the center of the detector.