

# Mixing and CP Violation at the Tevatron

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on behalf of the CDF and DØ Collaborations



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# Outline

- $B_s$  mixing
- D mixing: mixing interference in decay
- CP Violation:
  - $B^+ \rightarrow J/\psi K^+$ : CPV in decays
  - Semileptonic  $A_{CP}$ : CPV in mixing
  - $B_s \rightarrow J/\psi \phi$ : CPV in interference of mixing and decay
- Conclusions

(Throughout this talk, charge conjugated modes are implicitly assumed.)

# Mixing

$$|B_1\rangle = \frac{1}{\sqrt{2}} (|B^0\rangle + |\bar{B}^0\rangle) = |B_H\rangle$$

$$|B_2\rangle = \frac{1}{\sqrt{2}} (|B^0\rangle - |\bar{B}^0\rangle) = |B_L\rangle$$

Mass Eigenstates  
(and CP eigenstates  
if ignore CP violation)

Weak Eigenstates

$$\hat{H} \begin{pmatrix} B^0 \\ \bar{B}^0 \end{pmatrix} = \begin{pmatrix} M - \frac{i\Gamma}{2} & M_{12} - \frac{i\Gamma_{12}}{2} \\ M_{12}^* - \frac{i\Gamma_{12}^*}{2} & M - \frac{i\Gamma}{2} \end{pmatrix} \begin{pmatrix} B^0 \\ \bar{B}^0 \end{pmatrix}$$

- Then  $B_1$  and  $B_2$  are eigenstates with

$$\text{masses: } m_{1,2} = M \pm \frac{\Delta m}{2} \quad \text{and lifetimes: } \Gamma_{1,2} = \Gamma \pm \frac{\Delta\Gamma}{2}$$

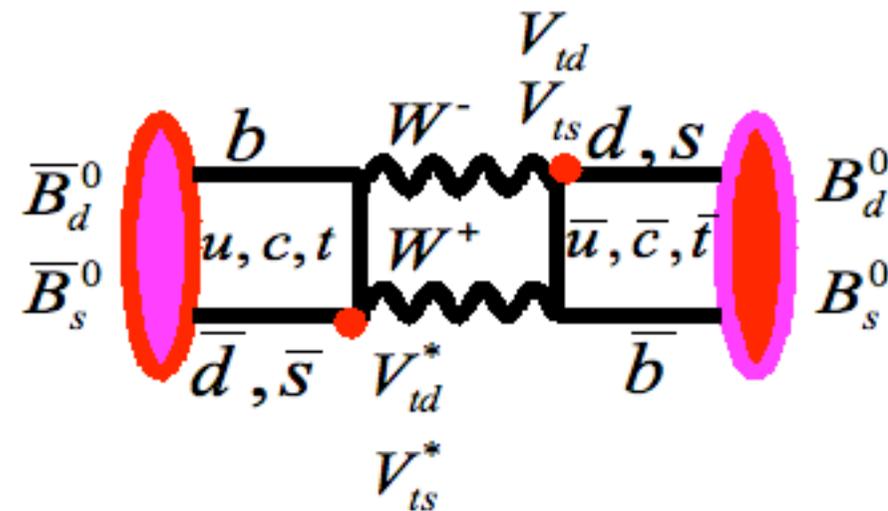
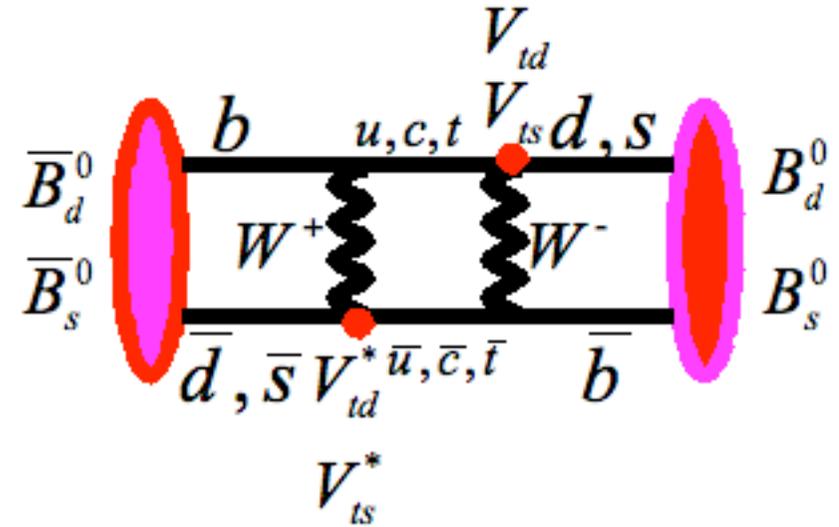
Define  $x = \Delta M/\Gamma$ ,  $y = \Delta\Gamma/2\Gamma$ , and

$$x' = x \cos\delta + y \sin\delta, \quad y' = -x \sin\delta + y \cos\delta$$

( $\delta$  is a strong phase)

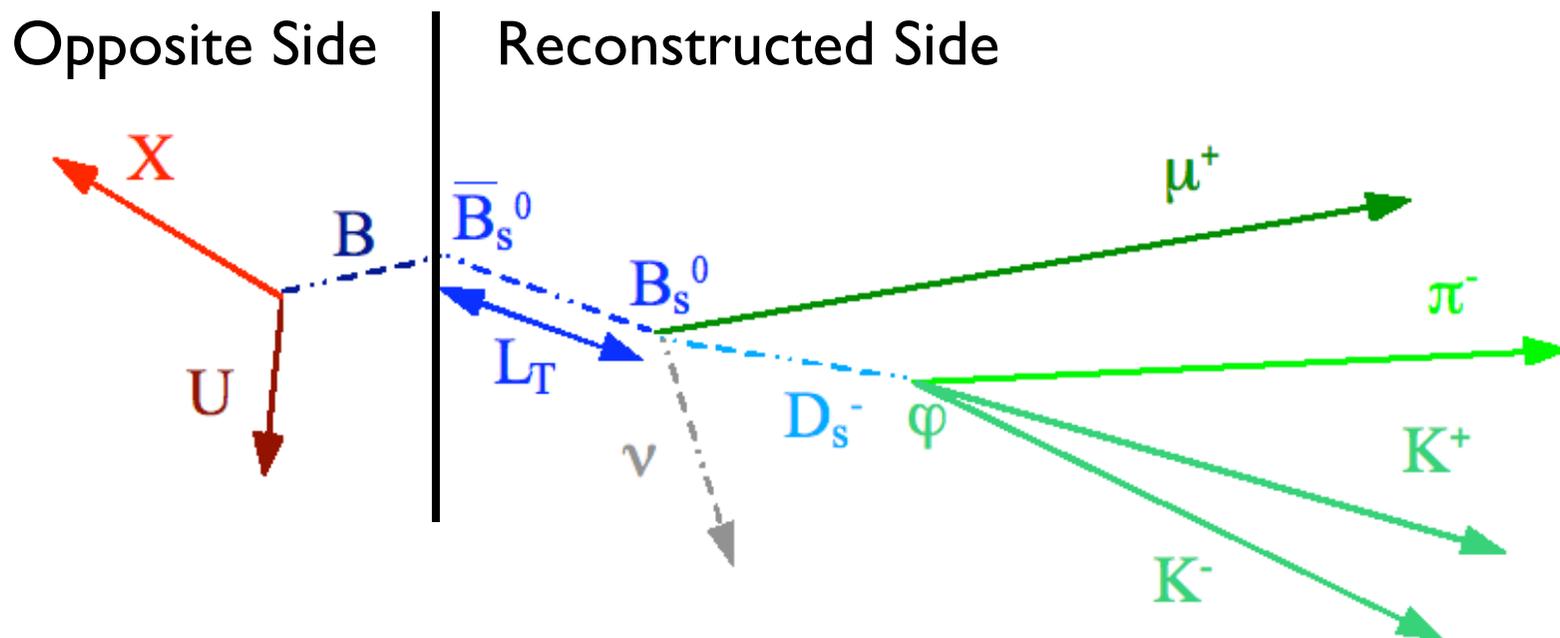
# Feynman Diagrams (B)

- Processes (dominantly) mediated by box diagrams
- Since  $V_{tb}$  is large, diagrams with top quarks dominant
- In  $M_{12}$ , mass comes in as  $m_{\text{top}}^2/m_W^2$
- High oscillation frequency was the first experimental indication of large top quark mass (1987)
- Sensitive to new heavy particles in loops



$\bullet \Delta m_d \propto |V_{tb}^* V_{td}|^2$ 
 $\bullet \Delta m_s \propto |V_{tb}^* V_{ts}|^2$

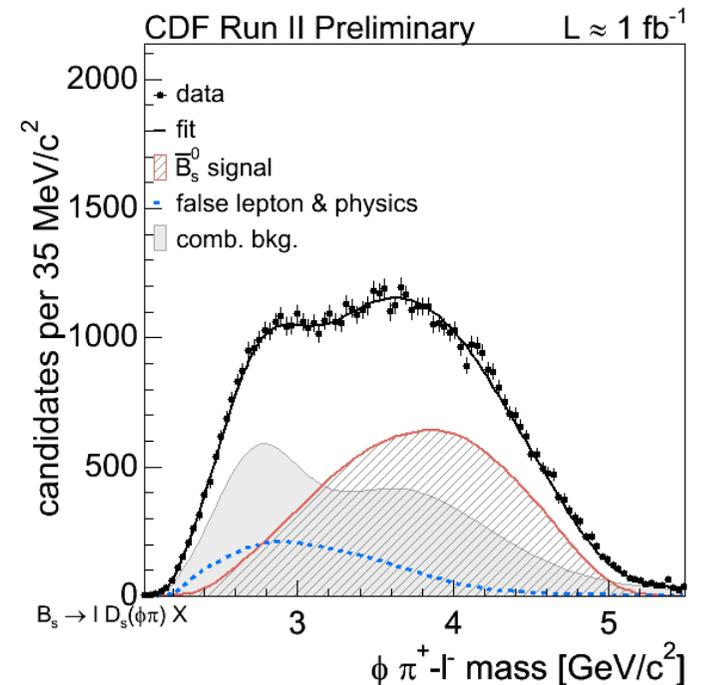
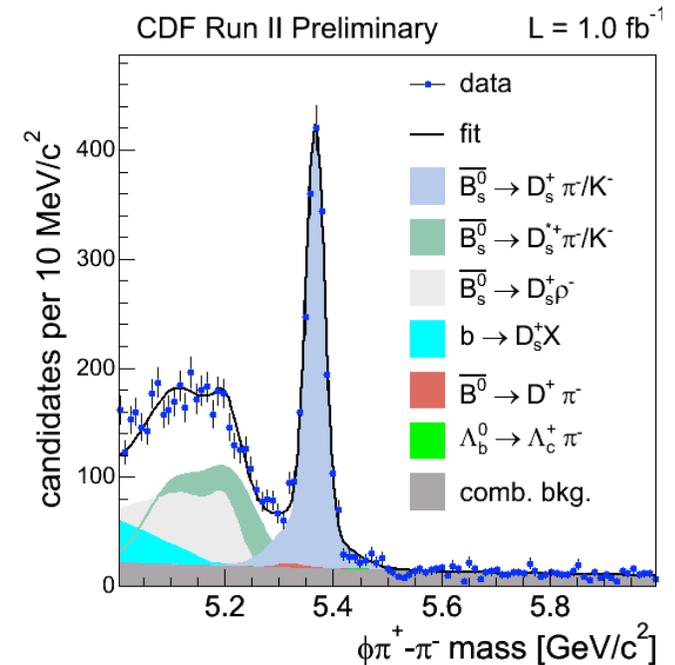
# Analysis Strategy



- Reconstruct  $B_s$  decay on one side, flavor at decay time is given by charges of decay products, measure momentum and (transverse) decay length  $L_T$  (to determine proper lifetime)
- Tag flavor at production using either “opposite side” b-hadron (most b’s are pair-produced), or “same side” hadron from fragmentation (for  $B_s$ , in principle a K)

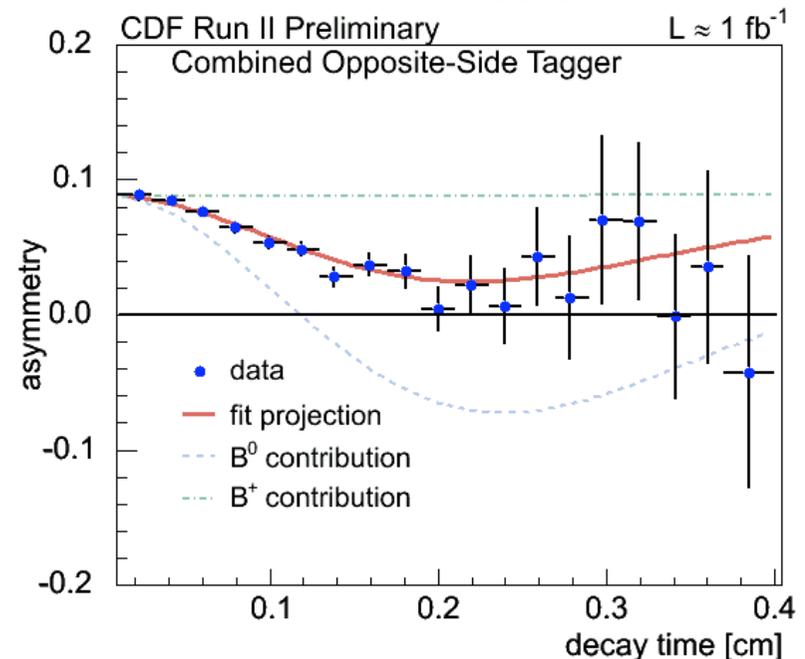
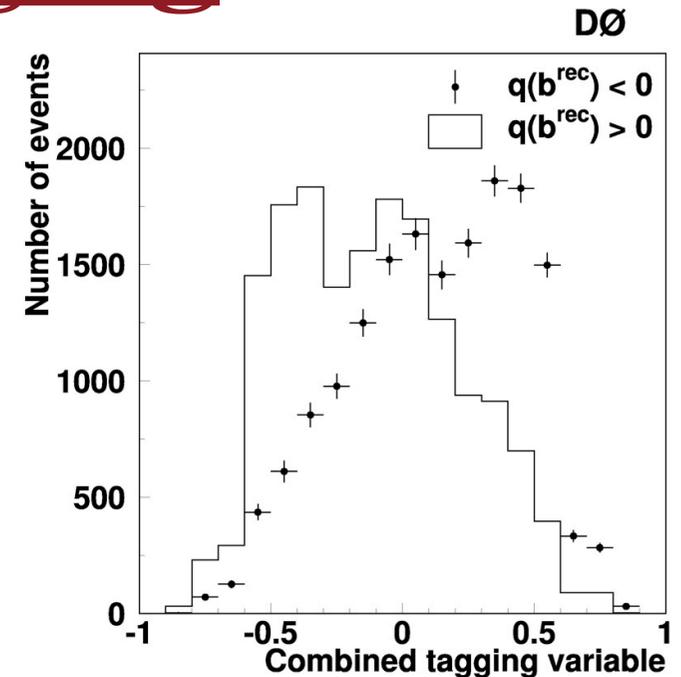
# Reconstruction

- Look for  $B_s \rightarrow D_s X$ 
  - X can be leptons, 1 or 3 pions
  - Consider multiple  $D_s$  decay channels
- Use NN (CDF) / likelihood (DØ) to increase S/B
  - CDF includes particle ID based on TOF, dE/dx in drift chamber
- In semileptonic  $B_s$  decays do not reconstruct  $B_s$  momentum fully
  - ➔ Apply a “K-factor” to rescale momentum



# Flavor Tagging

- At the Tevatron, most  $b$  quarks are produced in  $b\bar{b}$  pairs
- Can use opposite-side  $b$  quark for tagging
- Same-side hadrons also useful (but usually less pure, because sensitive to fragmentation fluctuations)
- Both experiments combine tags in NN (CDF) or likelihood (DØ)
- Verify performance using  $B_d$  mixing

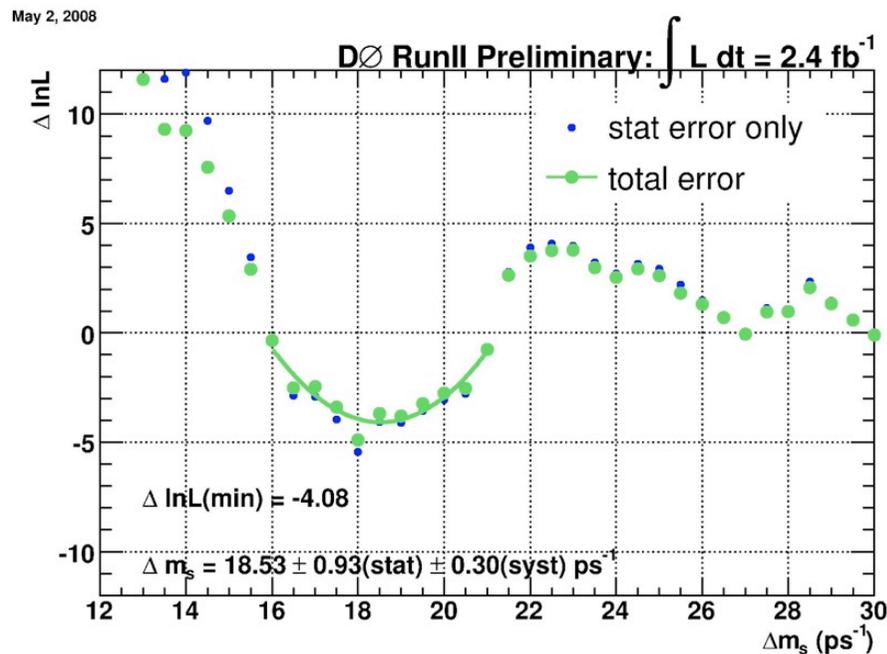


# Result

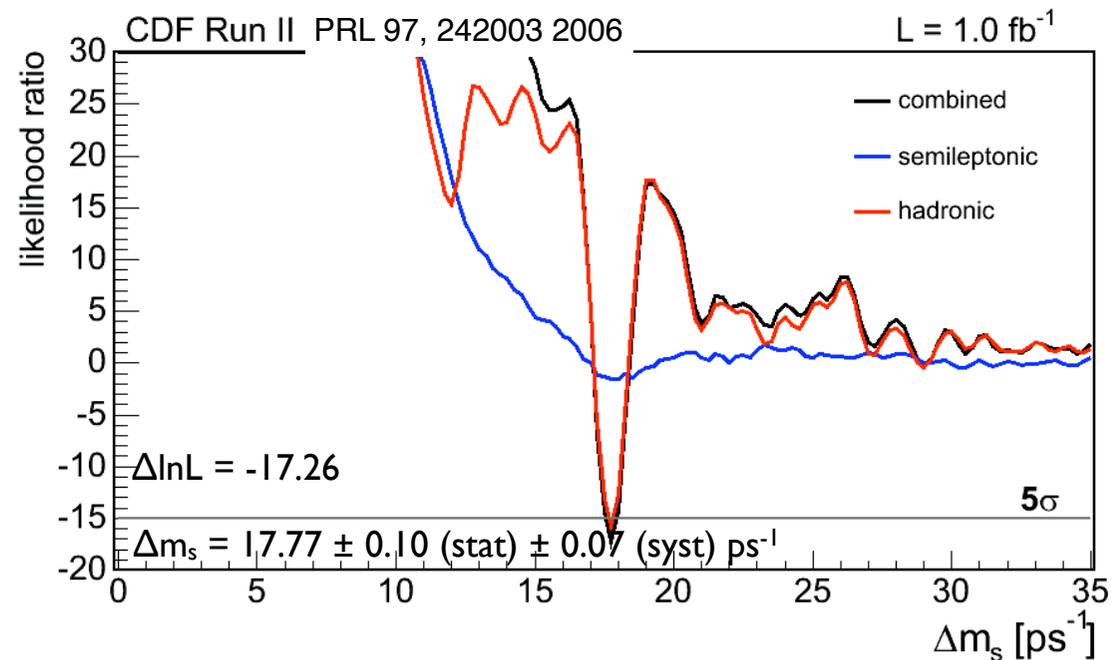
- Maximizing sensitivity requires using all information (uncertainties) on an event-by-event basis

➔ Unbinned maximum likelihood fits

DØ: small contribution from hadronic channels

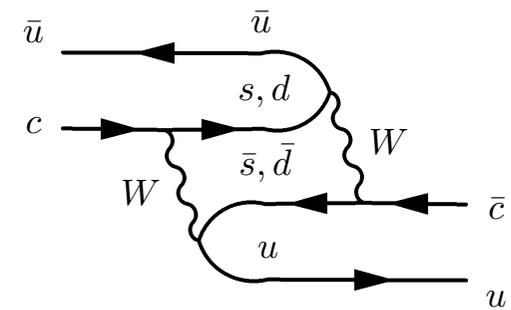
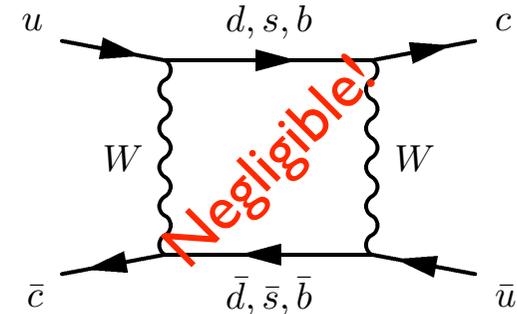


CDF: hadronic channels dominant  
large LI bandwidth, SVT & PID

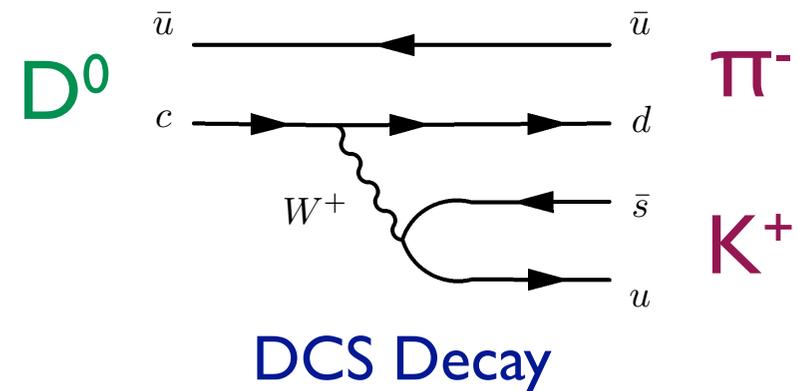


# D Mixing

- D oscillations expected to be slow in the SM
- Box diagram ( $\Delta C=2$ ) very small due to CKM & GIM suppressions
- “Long range” ( $2 \times \Delta C=1$ ) dominant, proportional to breaking of  $SU(3)_f$
- Cannot observe oscillation
- Mixing interference may be visible in doubly Cabibbo-suppressed decays

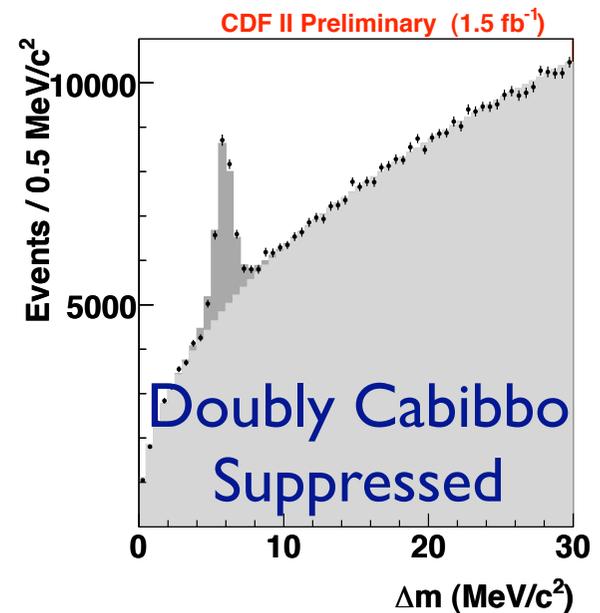
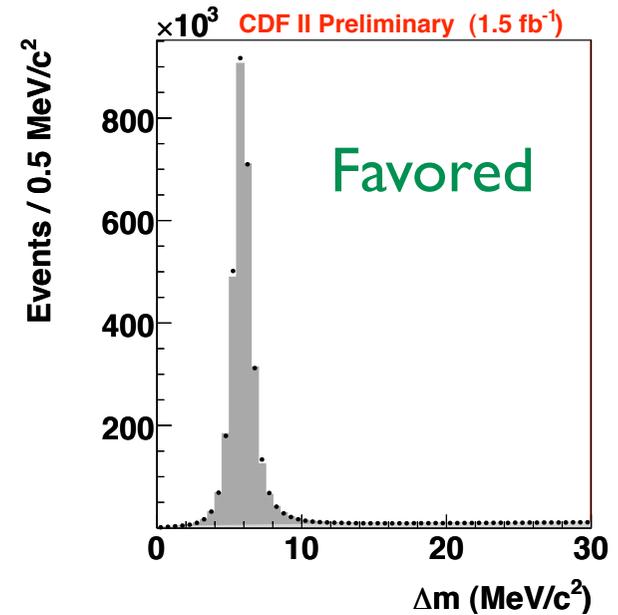


“Long Range”



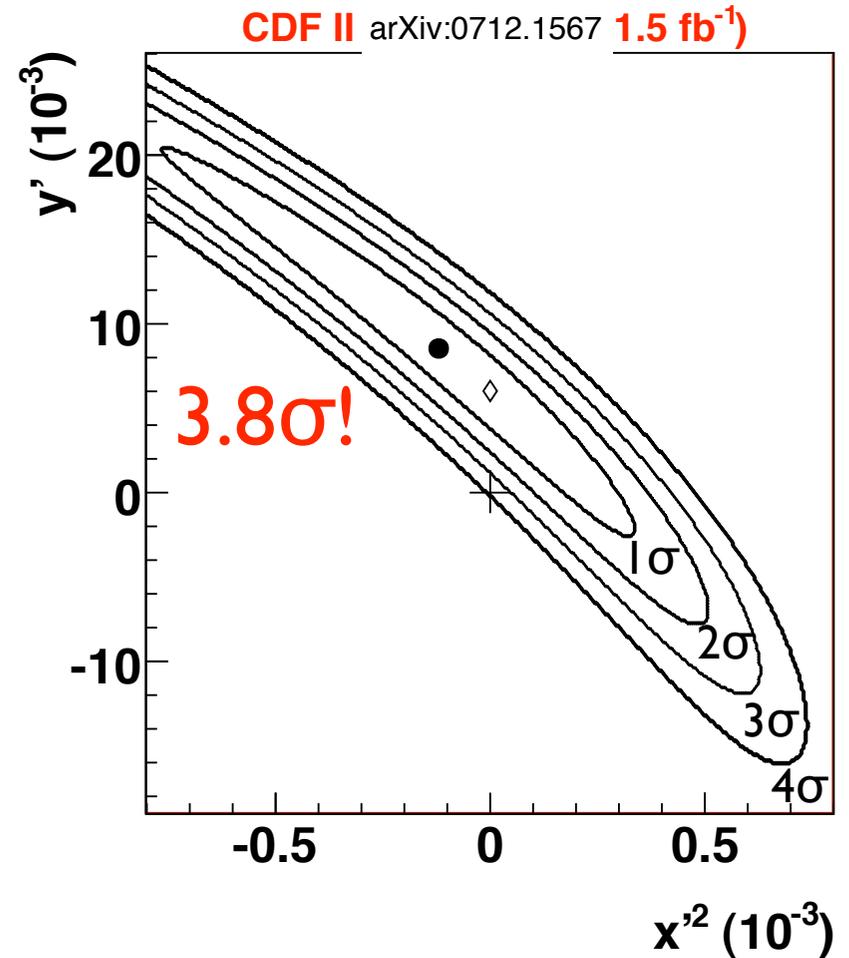
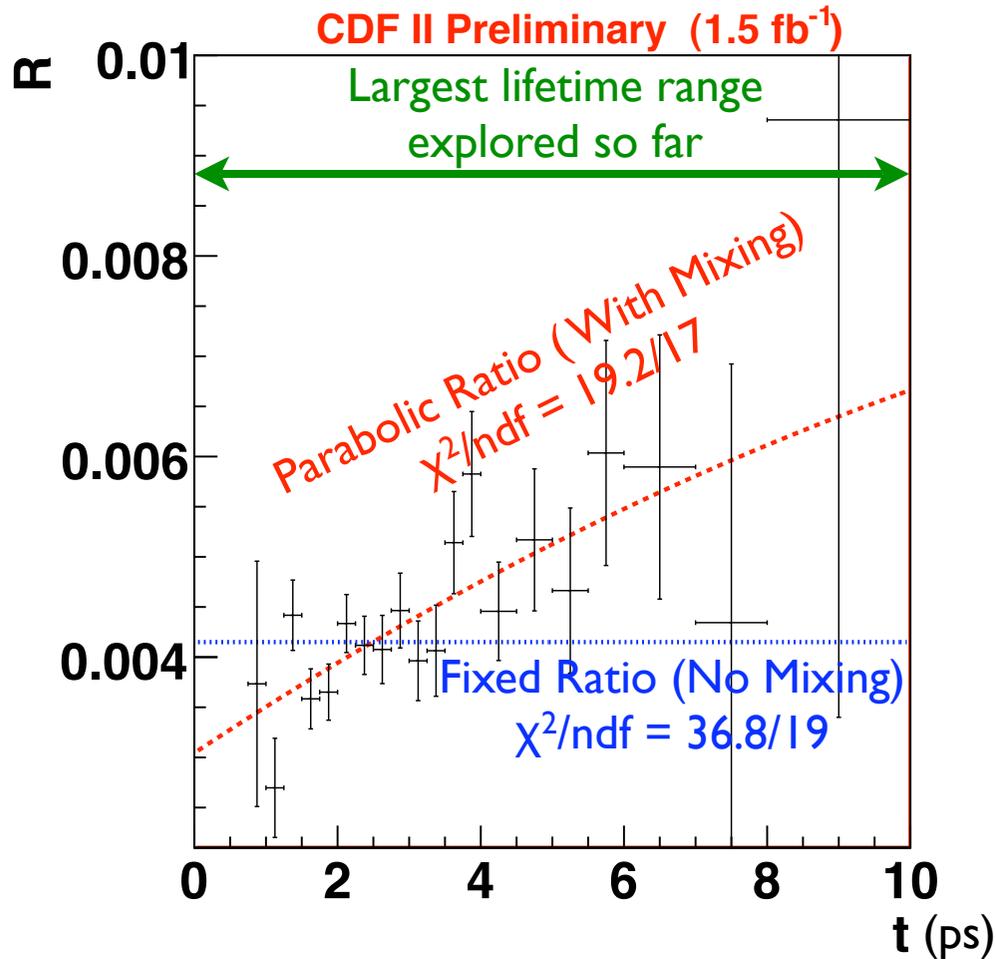
# Analysis Technique

- Look for mixing-induced time dependence of  $D^0 \rightarrow K^+ \pi^- / D^0 \rightarrow K^- \pi^+$  ratio
- Sample collected with IP trigger
- Use  $D^{*+} \rightarrow \pi^+ D^0, D^0 \rightarrow K\pi$  chain to “tag”  $D^0$  flavor at production
- Include PID, reject  $K\pi$  candidates that fall into  $D^0$  mass window with both mass assignments
  - Look at  $\Delta m = m(K\pi\pi) - m(K\pi) - m(\pi)$ : should be  $\sim 5$  MeV



# D Mixing!

$$R(t) = R_D + \sqrt{R_D} y' t + \frac{x'^2 + y'^2}{4} t^2$$



- Dominant systematics: signal and background shapes, fraction of D<sup>\*</sup>'s from B decays

# CP Violation

- In the decay amplitudes:  $B^+ \rightarrow J/\psi K^+$ 
  - $\Gamma(B \rightarrow f) \neq \Gamma(\text{CP}(B) \rightarrow \text{CP}(f))$
  - Only possibility in charged meson decays
- In mixing: **Same-Sign Dimuons**
  - Observe through asymmetry in charged-current neutral meson decays:  $A_{SL}$
- Interference between the two:  $B_s \rightarrow J/\psi \phi$ 
  - Interference between decays without/with mixing: need common final state

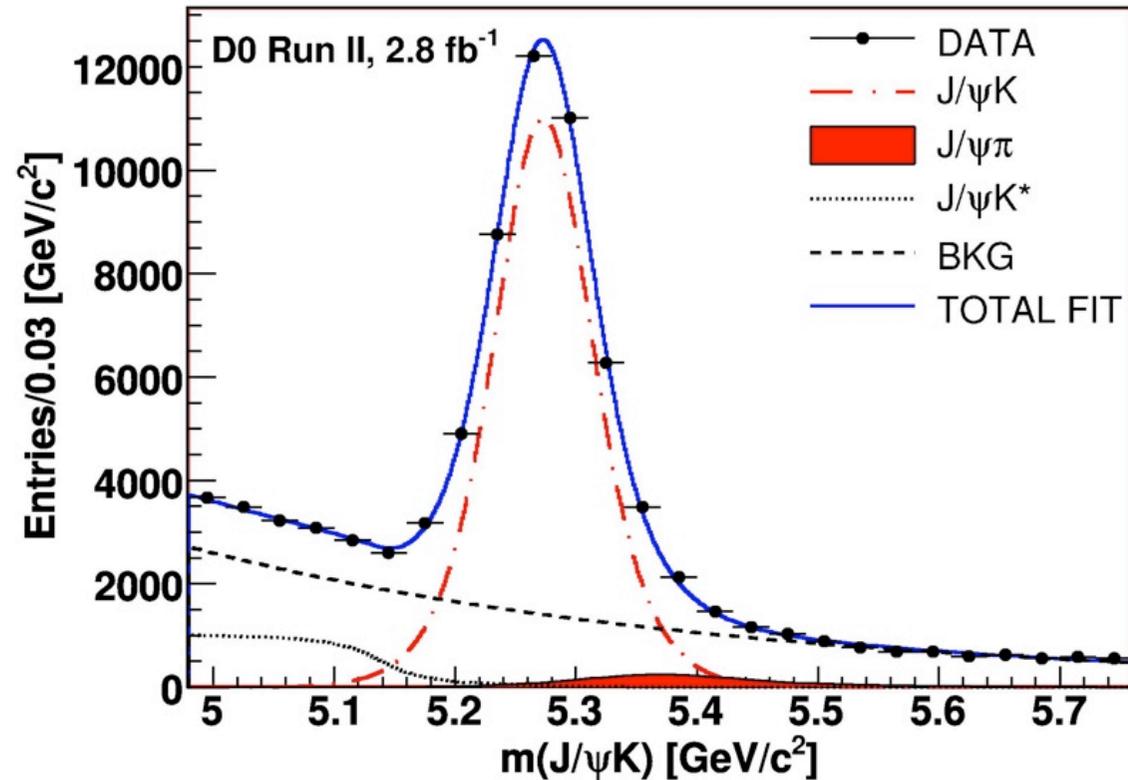
# $B^+ \rightarrow J/\psi K^+ (\pi^+)$

- Select sample with  $J/\psi$  decaying to a pair of muons
  - Very clean sample, 40k candidate events
- Fit for asymmetries:

- Divide sample in 8 based on solenoid polarity, sign of  $J/\psi K^+$  pseudo-rapidity  $\eta$ , and K charge

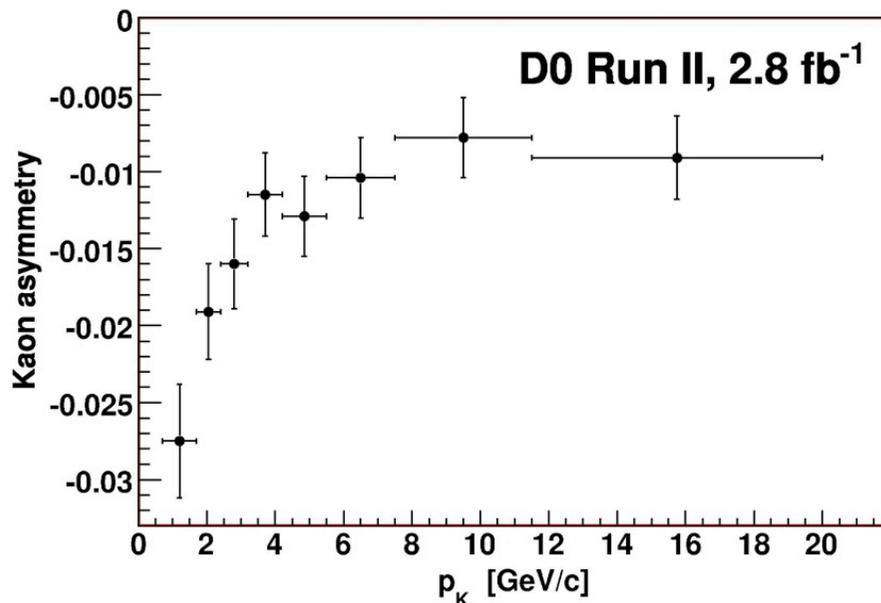
$$n_q^{\beta\gamma} = \frac{1}{4} N \epsilon^\beta (1 + qA)(1 + q\gamma A_{fb})(1 + \gamma A_{det}) \\ \times (1 + q\beta\gamma A_{ro})(1 + q\beta A_{q\beta})(1 + \beta\gamma A_{\beta\gamma})$$

- All detector & forward-backward asymmetries found compatible with 0



# $B^+ \rightarrow J/\psi K^+ (\pi^+)$ : Result

- Need to correct observed asymmetry for  $K^\pm$  reconstruction asymmetry
- Due to asymmetry in interactions (detector is made of matter)
- Measure in  $D^{*+} \rightarrow D^0 \pi^+$ ,  $D^0 \rightarrow \mu \nu_\mu K^-$



$$A_{CP}(B^+ \rightarrow J/\psi K^+) = 0.0075 \pm 0.0061 \text{ (stat)} \pm 0.0027 \text{ (syst)}$$

$$A_{CP}(B^+ \rightarrow J/\psi \pi^+) = -0.09 \pm 0.08 \text{ (stat)} \pm 0.03 \text{ (syst)}$$

arXiv:0802.3299

(Dominant systematic is mass distribution model)

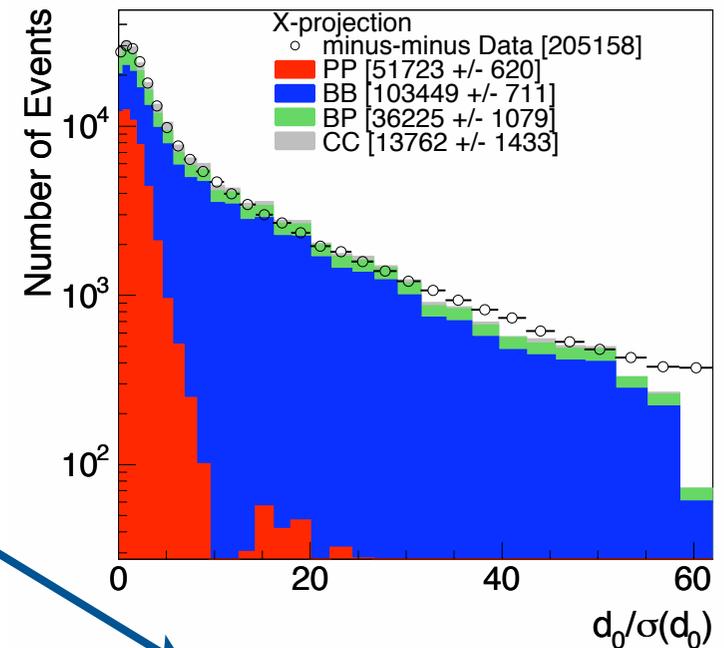
# Same-Sign Dimuons

- Measure  $A_{SL}^{\mu\mu} = \frac{N(b\bar{b} \rightarrow \mu^+ \mu^+ X) - N(b\bar{b} \rightarrow \mu^- \mu^- X)}{N(b\bar{b} \rightarrow \mu^+ \mu^+ X) + N(b\bar{b} \rightarrow \mu^- \mu^- X)}$
- Multiple techniques:
  - Use all dimuon events, and estimate contributions from all processes (incl. sequential decays, Drell-Yan, instrumentals, etc): DØ (2006) Phys. Rev. D 74 , 092001 (2006)
  - Use all dimuon events but use impact parameter distributions to unfold contributions from various sources: CDF
- Then derive  $A_{SL}^q$  from sample composition, or
  - Use flavor-specific decays, e.g.  $B_s \rightarrow \mu^+ \nu D_s^- X$ : DØ

# Inclusive Measurements

- New CDF measurement uses 2-D ( $\mu\mu$ ) impact parameter significance distribution
- Asymmetry from  $K/\pi$  faking muon measured in  $D^{*+}$  decays, + unfold direct and sequential decay contributions

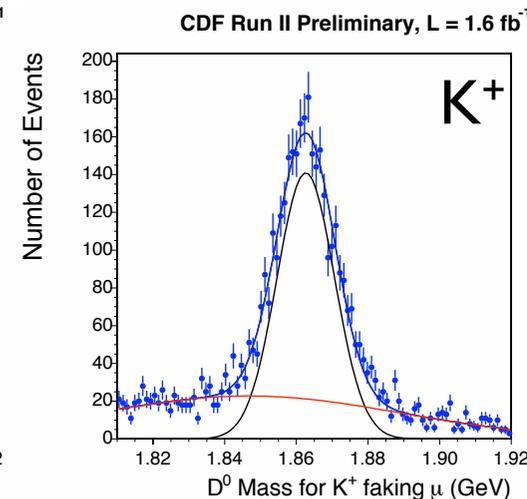
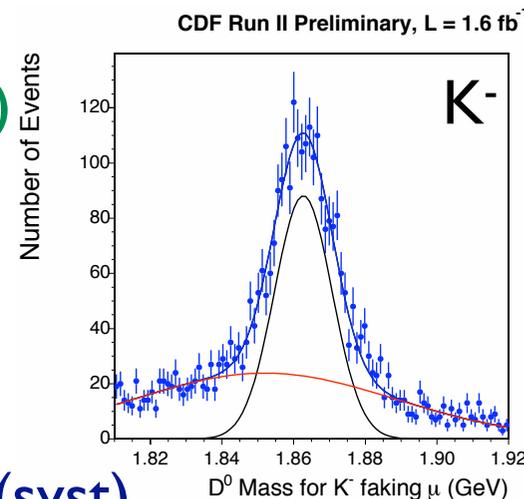
CDF Run II Preliminary, L = 1.6 fb<sup>-1</sup>



$$A^{\mu\mu}_{SL} = 0.0080 \pm 0.0090 \text{ (stat)} \pm 0.0068 \text{ (syst)}$$

DØ 2006 fully inclusive measurement using “8 subsamples technique”:

$$A^{\mu\mu}_{SL} = -0.0053 \pm 0.0025 \text{ (stat)} \pm 0.0018 \text{ (syst)}$$

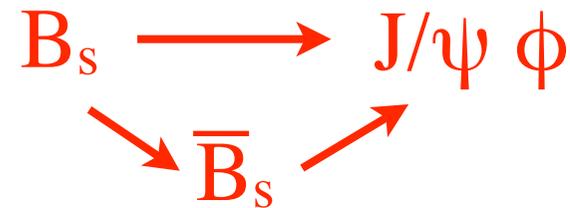
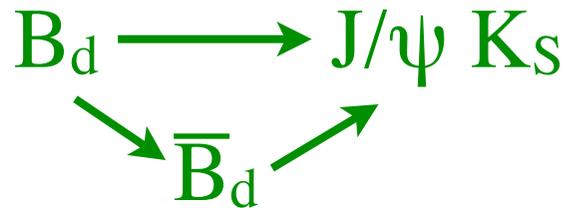


# $A^d_{SL}$ & $A^s_{SL}$

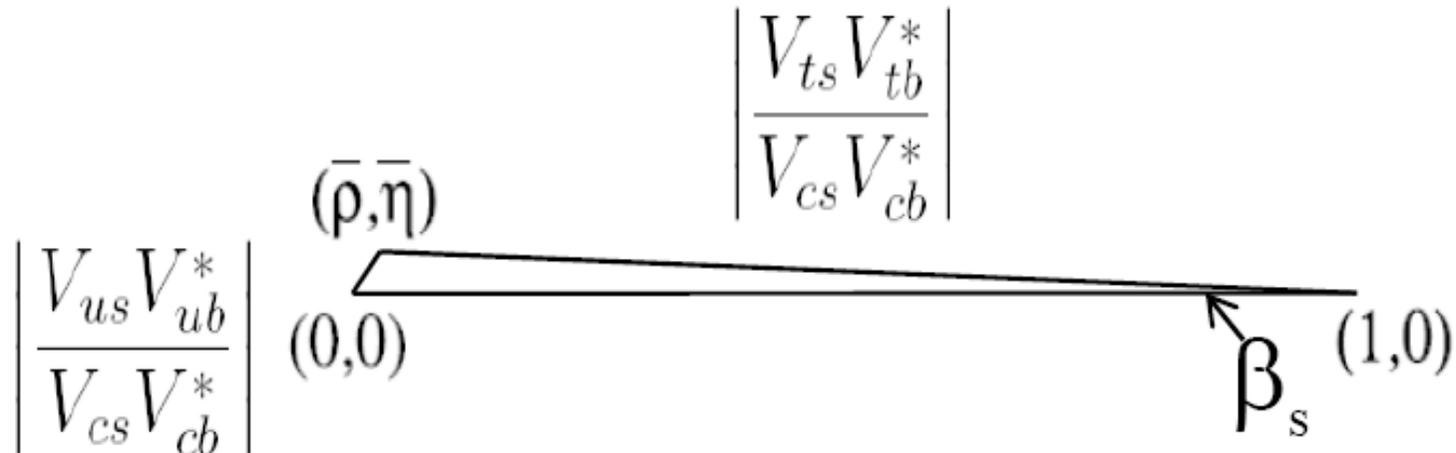
- $A^{\mu\mu}_{SL}$  has contributions from both  $B_d$  and  $B_s$ :
  - Use  $A^d_{SL}$  from the B-factories,  $B_d$  and  $B_s$  production ratios, and mixing parameters to extract  $A^s_{SL}$
- From CDF impact parameter analysis:
  - $A^s_{SL} = 0.020 \pm 0.021$  (stat)  $\pm 0.016$  (syst)  $\pm 0.009$  (inputs)
- From  $D\bar{0}$  inclusive analysis:
  - $A^s_{SL} = -0.0064 \pm 0.0101$  (uncertainties combined)  
Phys. Rev. D 76 , 057101 (2007 )
- From  $D\bar{0}$  exclusive measurement ( $B_s \rightarrow \mu^+\nu D_s^- X$ ):
  - $A^s_{SL} = 0.0245 \pm 0.0193$  (stat)  $\pm 0.0035$  (syst)  
Phys. Rev. Lett. 98 , 151801 (2007 )

# $B_s \rightarrow J/\psi \phi$ : CPV in Interference

- Equivalent of  $B_d \rightarrow J/\psi K_S$  in  $B_d$  system
- Access to the equivalent of  $\sin(2\beta)$ :  $\sin(-\phi_s)$  or  $\sin(2\beta_s)$

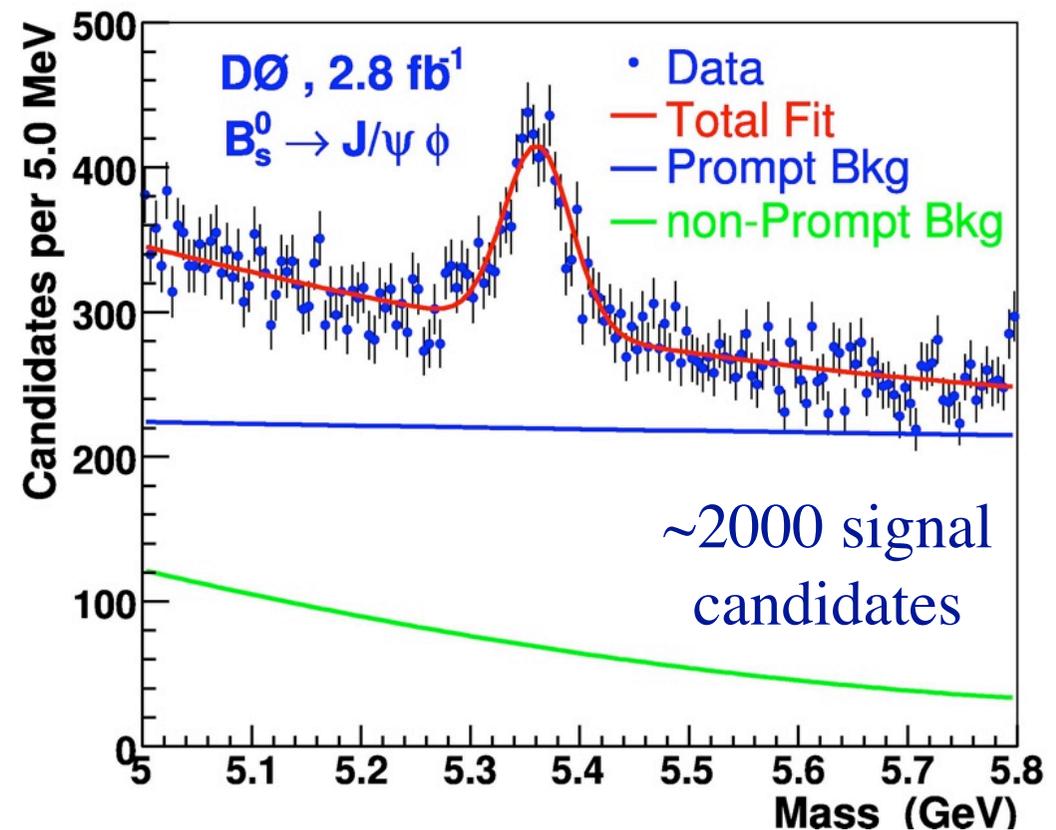
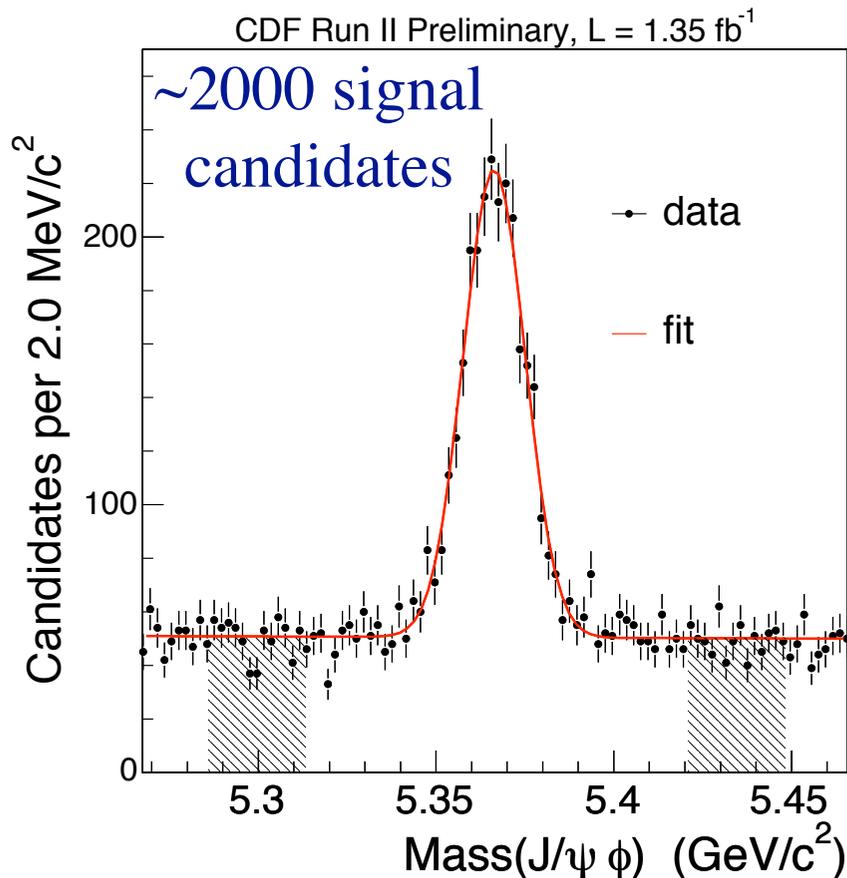


- But  $\beta_s$  is much smaller in the SM than  $\beta$ :



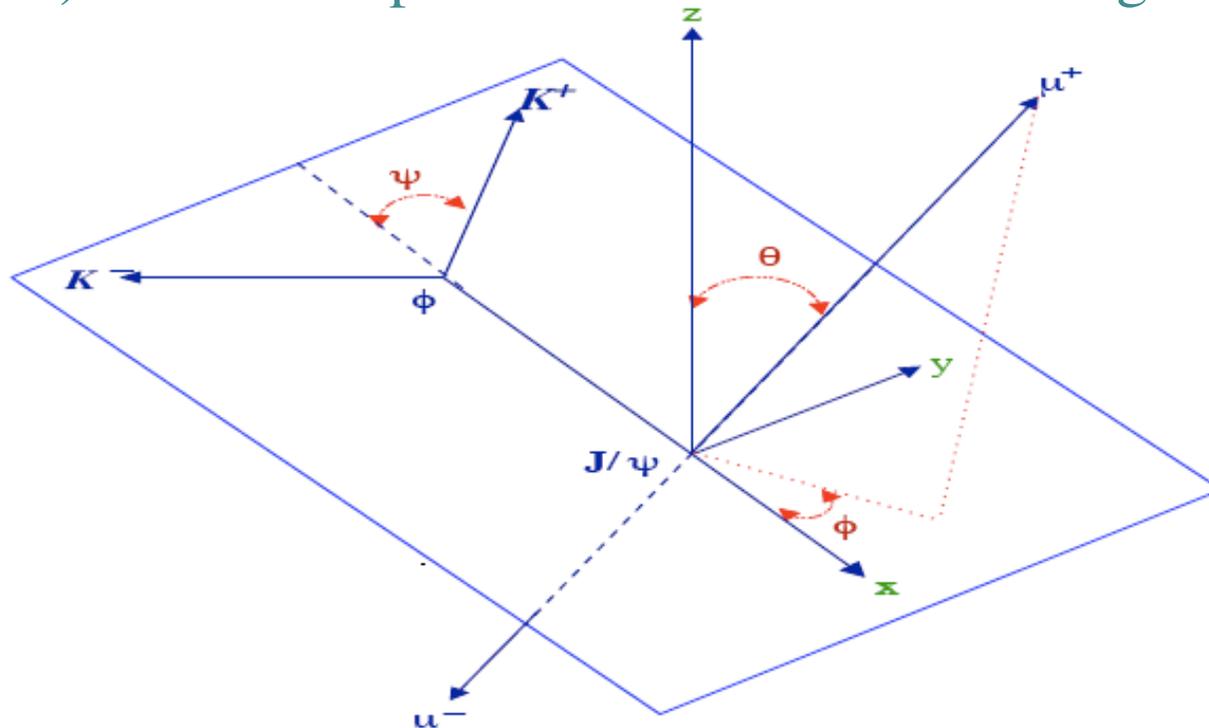
# $B_s \rightarrow J/\psi \phi$ Signal

- CDF uses neural network, with variables including PID from TOF & dE/dx in drift chamber
- DØ uses “square cuts” event selection (no PID)



# J/ψ φ CP? → Decay Angles

- VV final state ⇒ both CP eigenvalues possible.
- Disentangle by determining relative polarization of J/ψ and φ
- Express angular dependence in J/ψ rest frame (“transversity basis”) in terms of polarization ⇒ extract CP eigenvalue



# Flavor Tagging

- Needed to constrain flavor of decaying  $B_s$ 
  - Removes a twofold ambiguity in result
- Both experiments use both opposite-side and same-side tags
  - DØ: combined tagging power  $\epsilon\mathcal{D}^2 = 4.68 \%$
  - CDF:
    - OST tagging power  $\epsilon\mathcal{D}^2 = 1.28 \%$
    - SST tagging power  $\epsilon\mathcal{D}^2 = 3.65 \%$

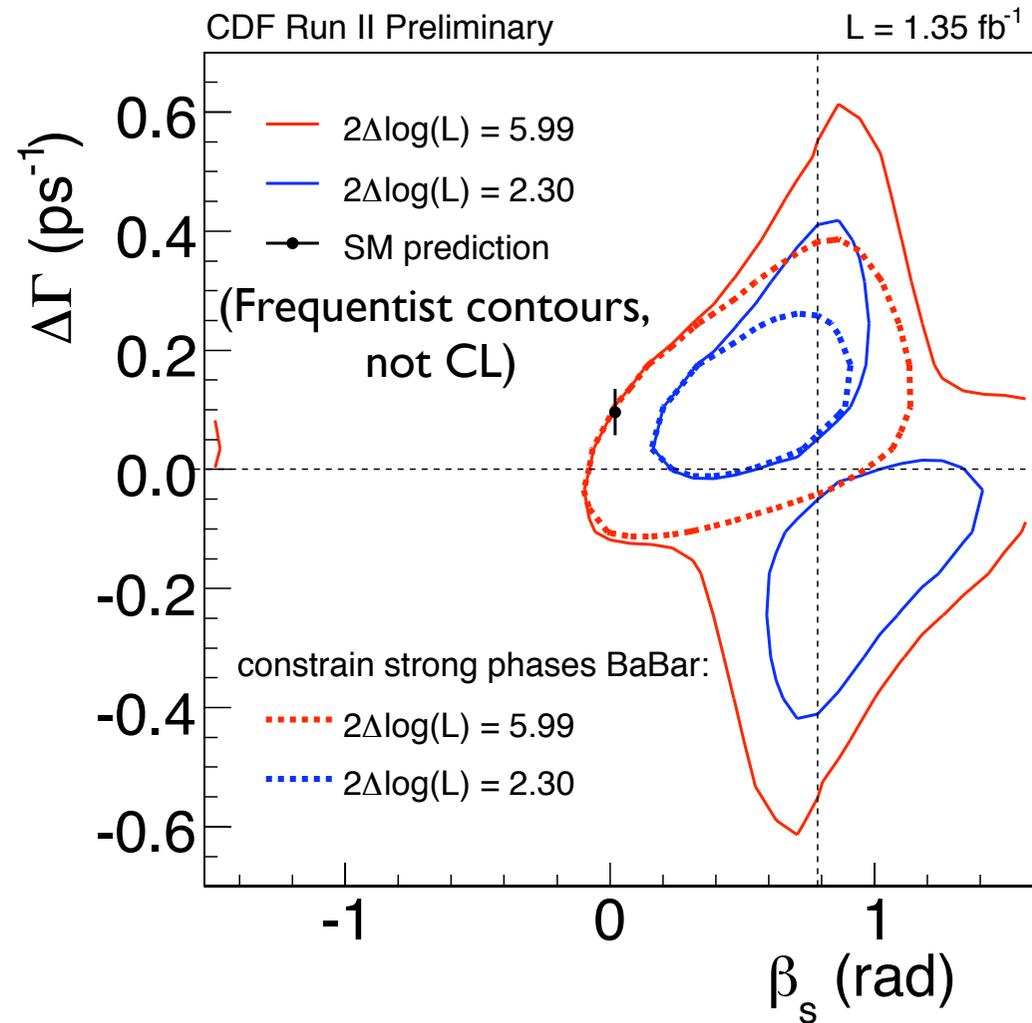
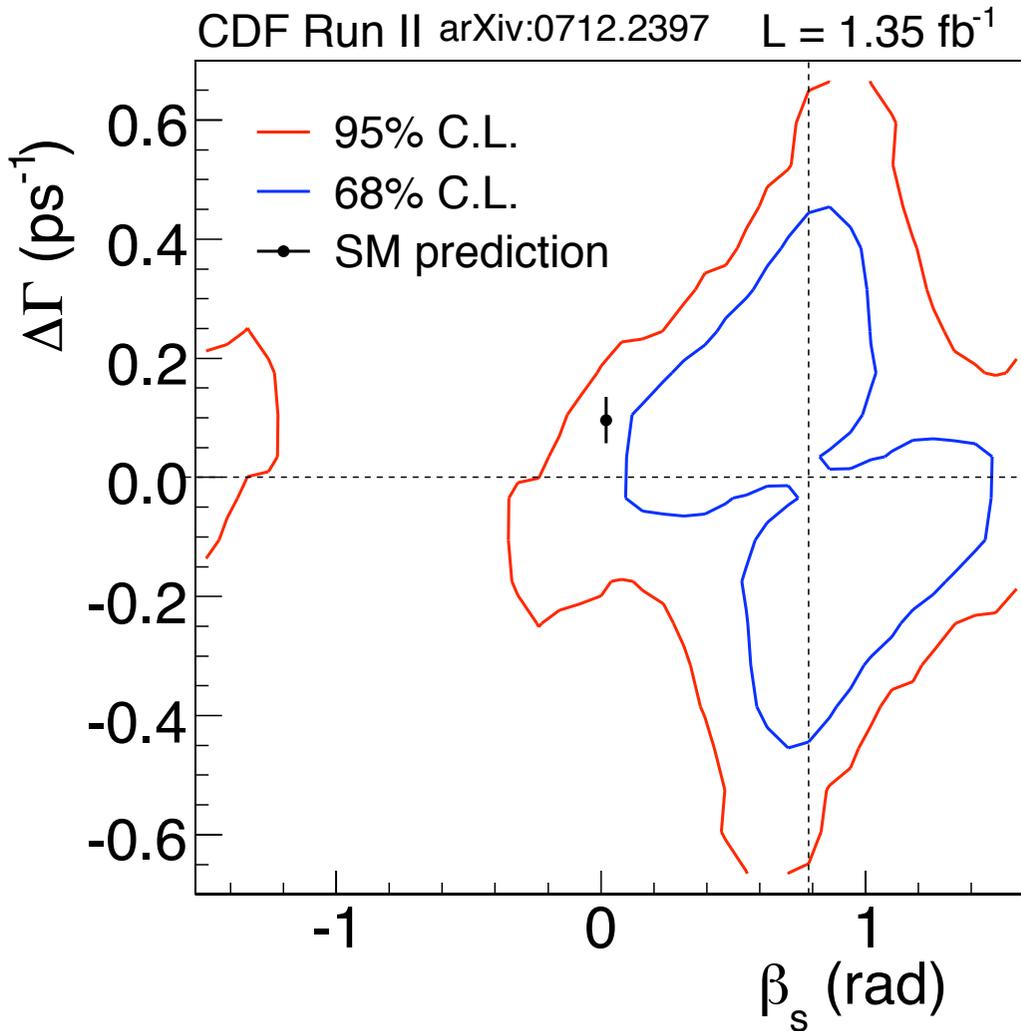
# Fit

- Use unbinned maximum likelihood fit to maximize sensitivity
  - Constrain  $\Delta m_s = 17.77 \pm 0.12 \text{ ps}^{-1}$
  - (Constrain or float strong phases)
  - Extract average lifetime,  $\Delta\Gamma_s$ ,  $\phi_s (= -2\beta_s)$ , magnitudes of polarization amplitudes, and strong phases
- NB: detector efficiencies are not flat vs transversity angles, correct
- CDF likelihood profiles not parabolic close to minima
  - Use Feldman-Cousins-like likelihood ratio ordering to build 2-D confidence region

# Result: CDF

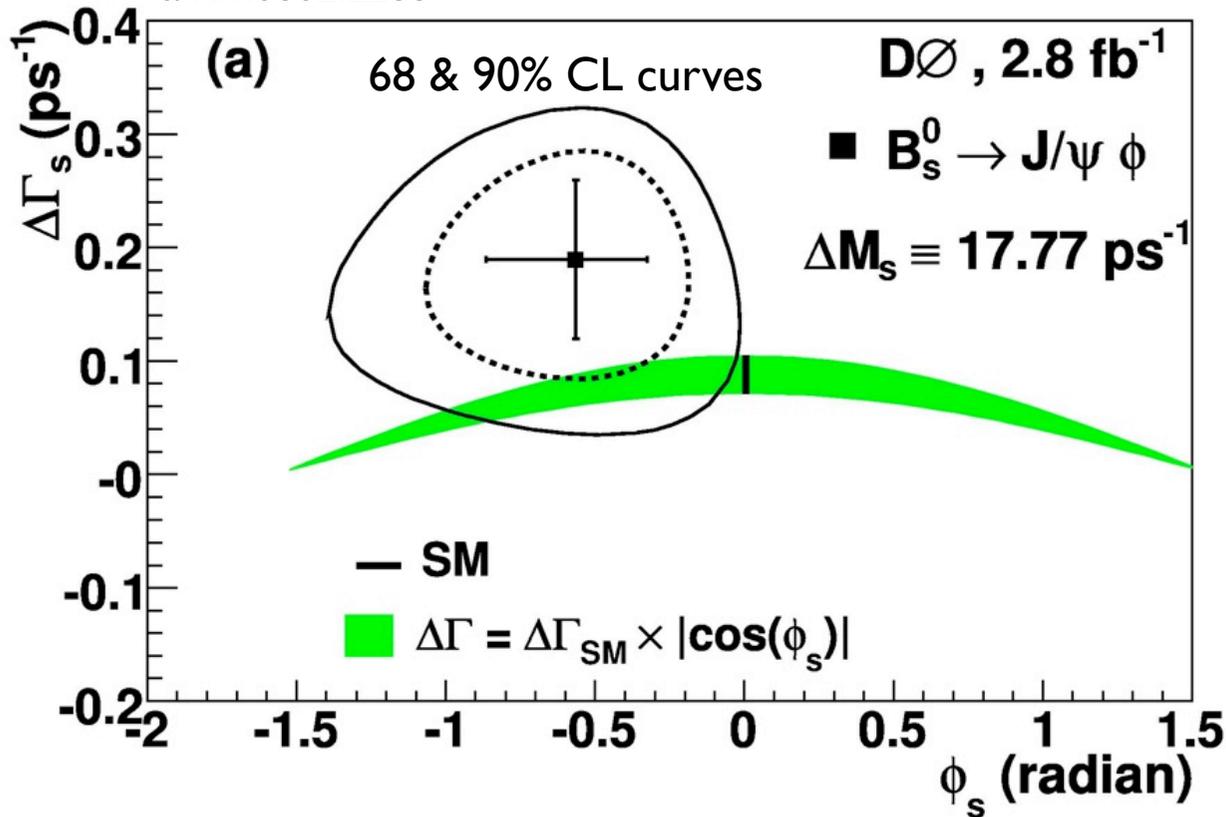
SM probability: 15% ✓

With BABAR constraints  
on strong phases from  
 $B^0 \rightarrow J/\psi K^{*0}$



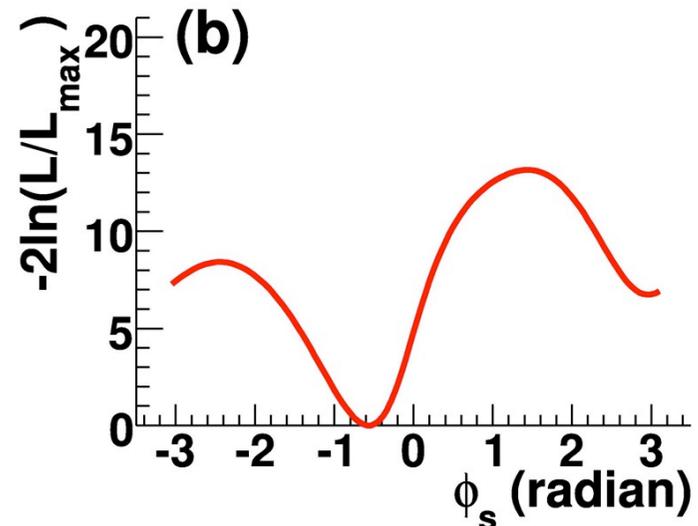
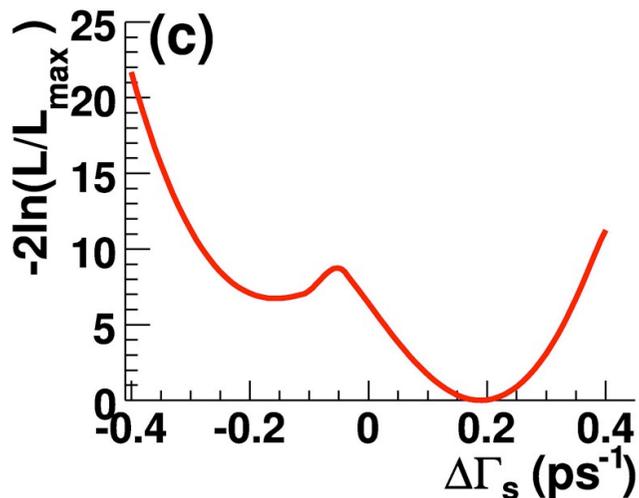
# Result: $D\bar{0}$

arXiv:0802.2255



(With BABAR constraints  
on strong phases from  
 $B^0 \rightarrow J/\psi K^{*0}$ )

SM probability:  
 $\sim 7\% \checkmark$



# Combination & Prospects

- *UTfit*: arXiv:0803.0659
  - Strong phases derived from BABAR  $B_d \rightarrow J/\psi K^*$  may not be completely valid, so try to unfold this from DØ result
    - (*UTfit* combination also uses asymmetries)
  - Some uncertainty with this, but any of the tried procedures lead to values of  $\phi_s$   $3\sigma$  or more from the Standard Model
- For both CDF and DØ, the measurement uncertainty is completely dominated by statistics
  - ➔ Result will still improve quite a bit
- If confirmed, this would be the first evidence for CP violation outside the CKM mechanism.

# Conclusions

- Evidence for D mixing seen by CDF
- $A_{CP}(B^+ \rightarrow J/\psi K^+)$  and  $A^{s_{SL}}$  compatible with 0
- $B_s$  mixing parameters:
  - $\Delta m_s$ : evidence by  $D\emptyset$ , observation by CDF
  - $\Delta\Gamma_s$ : good agreement with Standard Model
  - $\phi_s$ : suggestion of CP violation beyond the CKM mechanism?

To be continued....

# $B_{d,u}$ and $B_s$

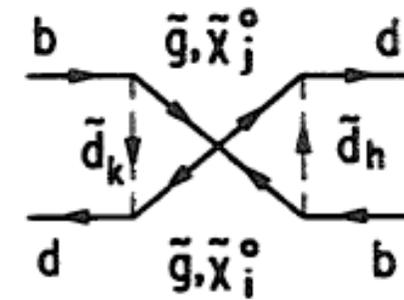
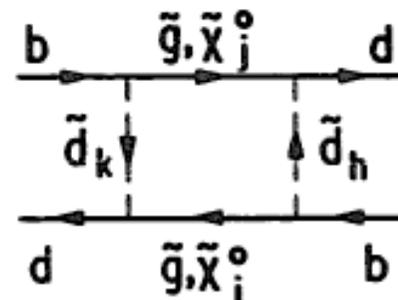
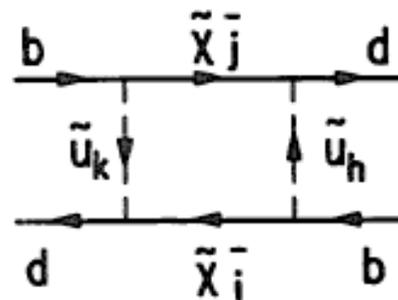
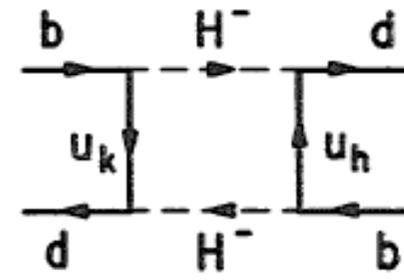
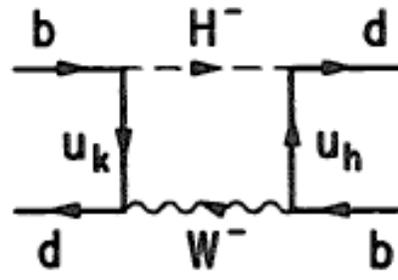
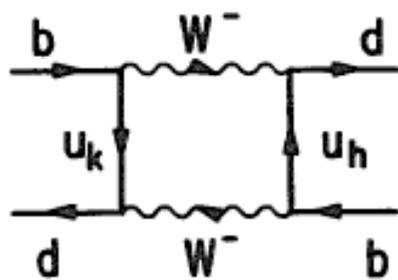
- Many aspects of CP violation in  $B_{d,u}$  well measured
  - Lots from B-factories, and important Tevatron contributions
    - e.g.  $B^+ \rightarrow J/\psi K^+$
  - Tevatron also has access to large  $B_s$  sample!
- CP violation expected to be small in b-c transitions from  $B_s$  in the Standard Model

$$V_{CKM} =$$

$$\begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) & A\lambda^2 \\ A\lambda^3[1 - (1 - \frac{1}{2}\lambda^2)(\rho + i\eta)] & -A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix}$$

# New Physics in B Mixing

- Supersymmetric contributions for example (See Bertolini et al., Nucl. Phys. B353, 591 (1991)), but note that you still need flavor violation
- See for example Foster et al., Phys.Lett.B641:452-460,2006



# B Mesons Decay!

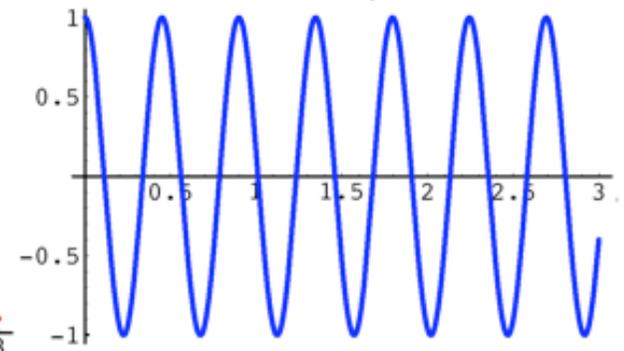
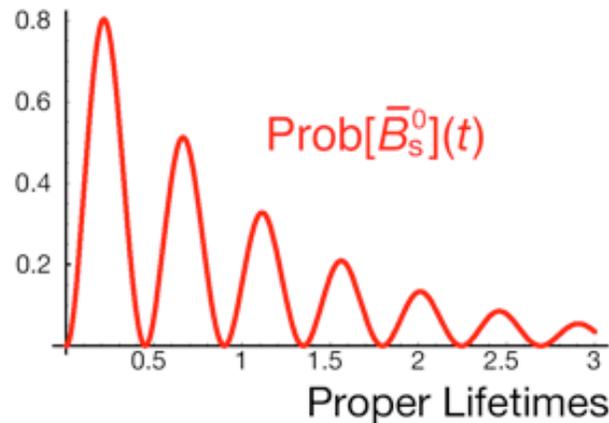
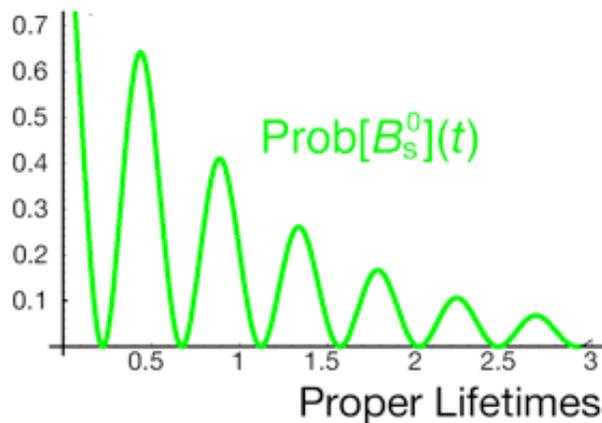
- If initially start with a  $B_s^0$

$$\text{Prob}[B_s^0](t) = \frac{1}{4} [\exp(-\Gamma_1 t) + \exp(-\Gamma_2 t) + 2\exp(-\Gamma t) \cos(\Delta m_s t)]$$

$$\text{Prob}[\bar{B}_s^0](t) = \frac{1}{4} [\exp(-\Gamma_1 t) + \exp(-\Gamma_2 t) - 2\exp(-\Gamma t) \cos(\Delta m_s t)]$$

Extract frequency

- For  $B_s^0$



Take asymmetry of two:

$$A = \frac{N[B^0](t) - N[\bar{B}^0](t)}{N[B^0](t) + N[\bar{B}^0](t)}$$

- What we get from it:  $\Delta m_s \propto |V_{tb}^* V_{ts}|^2$

- $\Delta m_d \propto |V_{tb}^* V_{td}|^2$
- $\Delta m_s \propto |V_{tb}^* V_{ts}|^2$

↑ ↑  
~1 tiny

↑ ↑  
~1 still small, but larger than  $V_{td}$