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Nuclear Instruments and Methods in Physics Research A ■ (■■■■) ■■■-■■■

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Run II physics at the Fermilab Tevatron and advanced analysis methods

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Abstract

The Fermilab Tevatron has the unique opportunity to explore physics at the electroweak scale with the highest ever proton-antiproton collision energy of $\sqrt{s} = 1.96$ TeV and unprecedented luminosity. About 20 times more data are expected to be collected during the first phase of the collider Run II which is in its second year of data-taking. The second phase of Run II, expected to begin in 2005, will increase the integrated luminosity to about $10\text{--}15 \text{ fb}^{-1}$. Discovering a low-mass Higgs boson and evidence for Supersymmetry or for other new physics beyond the Standard Model are the main physics goals for Run II. It is widely recognized that the use of advanced analysis methods will be crucial to achieve these goals. I discuss the current status of Run II at the Tevatron, prospects and foreseen applications of advanced analysis methods.

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PACS: ■; ■; ■

Keywords: ■; ■; ■

1. Introduction

The first phase of the second major proton-antiproton collider run (Run IIa) is well underway at Fermilab. Major upgrades to the accelerator complex include a brand new 150 GeV proton synchrotron called the Main Injector and a permanent magnet based antiproton recycler storage ring. The Main Injector enables 10 times more protons to be injected into the Tevatron, as compared to run I. The recycler helps recover the unused antiprotons from colliding beams of the Tevatron, store and reuse them in subsequent

collisions. The collision energy is upgraded to $\sqrt{s} = 1.96$ TeV, up from $\sqrt{s} = 1.80$ TeV in Run I.

The CDF and DØ experiments also underwent major upgrades in preparation for Run II [1]. The CDF detector had the inner tracker replaced, a plug calorimeter added and muon detectors upgraded. The DØ detector acquired a new central tracker with silicon microstrip and scintillating fiber tracking layers inside a 2 T solenoidal magnetic field and new scintillating fiber pre-shower detectors. The muon system has been upgraded with a new layer of scintillators in the central region and an all new forward muon system. A forward proton spectrometer has been added to enhance capabilities for diffractive

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1 physics. Both experiments required new trigger
and data acquisition systems.

3 A rich harvest of physics is expected from an
order of magnitude more data that is expected to
5 be collected in Run IIa alone. The broad physics
program consists of the study of Quantum
7 Chromodynamics via the study of jets, (particu-
9 larly a high statistics study with the high transverse
energy jets), electroweak physics with the W and Z
bosons, beauty and charm quark physics, top
11 quark physics including the possible evidence and
study of the electroweak production of single top,
13 and searches for the Higgs boson and for signals of
new physics beyond the Standard Model, notably,
15 the signatures for supersymmetry, lepto-quarks,
technicolor or extra spatial dimensions.

17 In the following section, I give a short status
report on the standard physics signals that are now
19 being studied at the CDF and DØ experiments in
an effort to understand the detectors and
21 pursue studies on a wide range of physics topics.
Then, I discuss, in the subsequent sections, the
23 advanced analysis methods that are of importance
in improving the various aspects of physics
25 analysis and prospects for exciting physics appli-
cations.

29 2. Early physics results from run II

31 By the end of spring of 2002, after a year of
running, the Tevatron had delivered about
33 55 pb^{-1} each to the CDF and DØ experiments.
Most of these data have been utilized to commis-
35 sion and tune the detectors. Some data have been
used to look at some standard physics signals. The
37 best way to evaluate the performance of the
detectors and tune the event reconstruction algo-
39 rithms and assess calibration errors in these early
days of the run is to look at known signals in
41 accessible mass regions. I present here some
preliminary results [2] from such studies using
43 Run II data.

45 Fig. 1 shows the invariant mass spectrum from
two unlike sign tracks measured in the DØ Silicon
detector only, which reveals the $K_s^0 \rightarrow \pi^+ \pi^-$ decays.
47 Including measurements from the central fiber
tracker improves the mass resolution to 5 MeV.

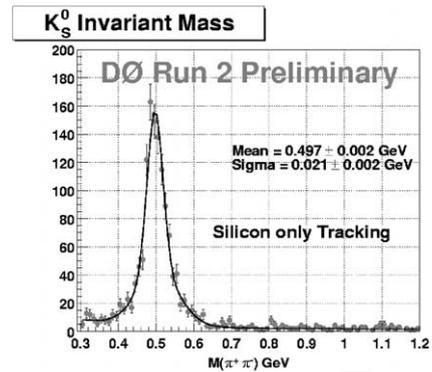


Fig. 1. The $K_s^0 \rightarrow \pi^+ \pi^-$ invariant mass spectrum using tracks
from the Silicon detector.

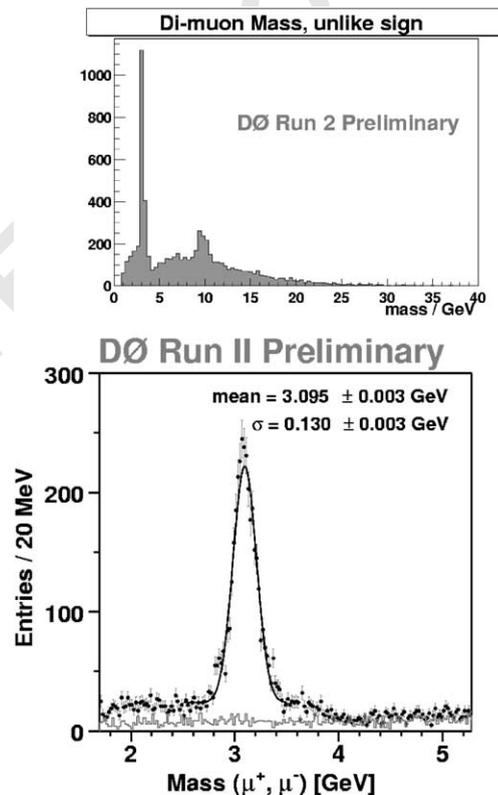


Fig. 2. The di-muon invariant mass spectrum showing the J/Ψ
and the Υ peaks (top). The di-muon invariant mass spectrum
after matching muons found in the muon system with tracks
from the central detector shows a clean signal of J/Ψ (bottom).

Better alignment of the sub-detectors using data is
expected to provide further improvement in track
parameter measurements.

The dimuon invariant mass spectrum showing the J/Ψ and the Υ peaks using muons tracked and measured in the $D\emptyset$ muon system alone and the cleaner J/Ψ peak resulting after matching the muons with the central detector tracks are displayed in Fig. 2.

The electroweak gauge bosons (W, Z) are of paramount importance both in their own right and in inclusive signal and/or background channels in many interesting physics processes. The $Z \rightarrow l^+l^-$ event samples serve as good calibration tools for lepton measurements. The invariant mass distributions of $Z \rightarrow ee$ from $D\emptyset$ and $Z \rightarrow \mu\mu$ from CDF are shown in Figs. 3 and 4, respectively.

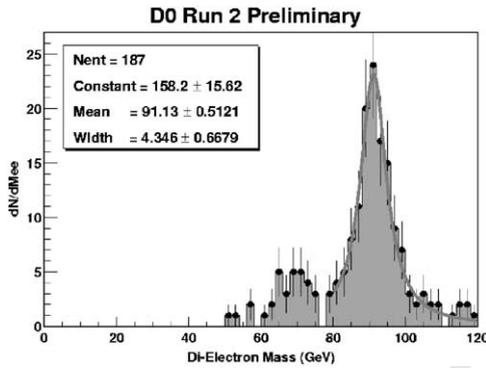


Fig. 3. The di-electron invariant mass spectrum (from $D\emptyset$) showing the Z boson peak.

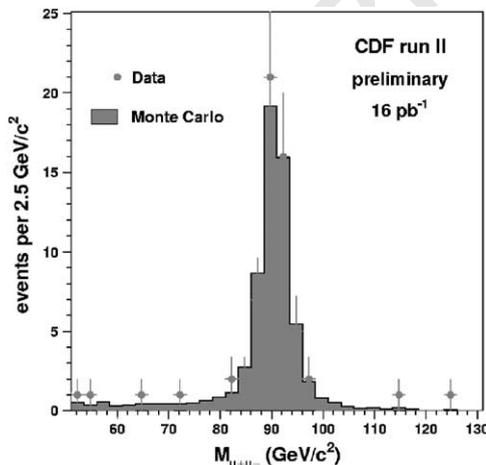


Fig. 4. The $Z \rightarrow \mu\mu$ signal from CDF Run II data [3].

The inclusive p_T spectrum of jets and the dijet mass spectrum measured in the $D\emptyset$ calorimeter in the central rapidity region of $|\eta| < 0.5$ are shown in Fig. 5. The jet energy corrections used are preliminary. With the full Run II data-set the transverse energy distribution of the jets should extend to beyond 600 GeV.

Enormous progress is being made at both experiments in understanding calibration and corrections, and in tuning event reconstruction and particle identification algorithms. A large number of physics analyses are in progress.

3. Advanced analysis methods

Uncovering the signals of new physics in a hadron collider environment is extremely challen-

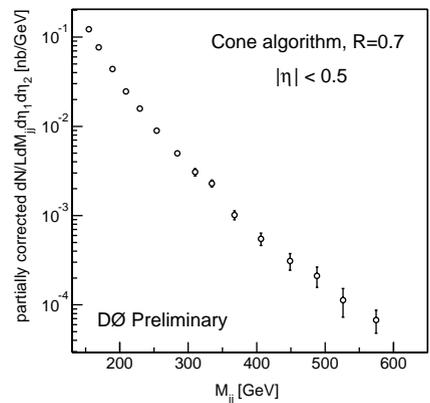
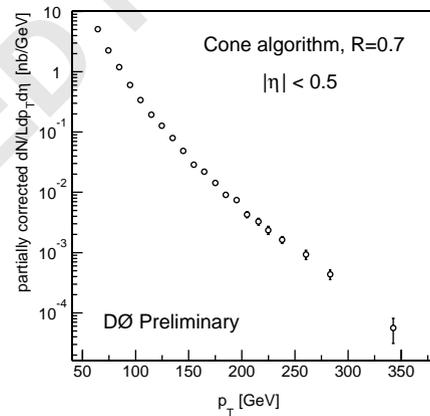


Fig. 5. Inclusive jet p_T spectrum (top) and dijet mass spectrum (bottom) from $D\emptyset$ ($\int L dt = 1.9 \text{ pb}^{-1}$).

ging because of a wide variety of processes that can mimic a given signature. Therefore, the use of advanced data analysis techniques are absolutely necessary for optimal separation of signal and background. The main data analysis tasks performed in HEP are particle identification, signal/background event classification, parameter estimation (precision measurements), functional approximation (fitting) and data-driven feature extraction or exploration. The best use of data is ensured only with multivariate treatment.

Suitable choice and representation of multivariate data are important first steps for a successful application. These could be labelled simply as intelligent pre-processing of data. In some applications this pre-processing might be the only necessary multivariate treatment of the data. The selection of variables for a given analysis application can be performed using the characteristic physics information or with algorithmic approach, employing, e.g., grid searches. Having selected a set of variables, one might like to apply a suitable transformation to the variables that would yield a representation of the data that most clearly exhibits certain desirable or “interesting” properties. That is, if \mathbf{x} is the original multidimensional datum, then we seek $\mathbf{s} = \mathbf{f}(\mathbf{x})$ which has the desirable properties. If a linear transformation is employed, then, $\mathbf{s} = \mathbf{W}\mathbf{x}$, where \mathbf{W} is the transfer matrix.

The transformation of variables is equivalent to extracting a map $f: R^d \rightarrow R^N$. If $N < d$, then we would have effected a dimensionality reduction. There are nonlinear algorithms that use probability density estimation—histogramming, kernel-based methods and the methods of adaptive mixtures, and those that use stochastic optimization such as neural networks (NN). For a review of these methods, see Ref. [4]. In the following, I have chosen to discuss a few potentially interesting methods for HEP applications.

3.1. Grid search, principal and independent component analysis

Grid searches provide a systematic way of finding good variables and optimal cuts in multidimensional space, albeit not taking into account

the correlations between variables. We developed a simple random grid search method [5] that can be used to compare the efficacy of variables as well as for a rapid search for optimal cuts for univariate classification. The results of such a grid search can be used as a benchmark to compare more sophisticated multivariate analyses.

To do a more advanced analysis, one would like suitably transformed variables as discussed earlier. Geometrically speaking, then, in a grid search one finds optimal cuts along the given coordinates while in the Principal and Independent Component Analyses (PCA & ICA) one finds interesting new directions (coordinates) in the multivariate space.

In the PCA algorithm (also known as Karhunen–Loeve transform or Hotelling transform), the variance along the axes is used as the interesting feature while finding transformed variables. The new set of orthogonal basis is obtained by finding eigenvectors \mathbf{u}_i and eigenvalues λ_i as solutions of the equation,

$$\mathbf{C}\mathbf{u}_i = \lambda_i\mathbf{u}_i \quad 71$$

where $\mathbf{C} = \mathbf{E}(\mathbf{x} - \bar{\mathbf{x}})(\mathbf{x} - \bar{\mathbf{x}})^T$ is the covariance matrix of the data set \mathbf{x} . The transformation matrix, \mathbf{W} has as its columns the eigenvectors and the transformed variables are $\mathbf{s} = \mathbf{W}\mathbf{x}$.

The ICA [6] is a relatively new technique, invented only in the past decade. It can be seen as a powerful extension of statistical factor analysis and PCA. The observed variables are assumed to be linear or nonlinear mixtures of unknown latent variables. The ICA technique enables transformation of data variables to extract these underlying statistically independent factors.

The ICA technique has been used in analyzing medical images, signal processing, and in the field of economics. Application to HEP would be a completely new exercise, which we have recently undertaken.

3.2. NN and their ensembles

Artificial NN, though inspired from biology conceptually, are rigorous mathematical models for developing the map - $f: R^d \rightarrow R^N$ where $N \ll d$ and generally $N \sim 1$, without requiring a mathe-

1 matical description of how the output(s) depend
2 on the inputs.

3 Good generalization, that is good predictions
4 for new inputs, is extremely important to minimize
5 classification errors or to avoid over-fitting of
6 data. The conventional methods for achieving
7 good generalization have been (a) optimizing the
8 size of the network given the training sample and
9 (b) regularizing the training by penalizing model
10 complexity. But there are new and sophisticated
11 approaches to achieve better generalization. (See,
12 e.g., Ref. [7].) And these involve using of
13 ensembles of networks such as “committees” or
14 “stacks.” The basic concept in the usage of
15 ensembles is to use many “nearly the best”
16 networks with varying models (i.e., in architecture
17 and input variables) rather than the “best”
18 network, in ways that would help reduce the
19 generalization error. It would be useful to arrive at
20 rigorous or heuristic approaches to efficiently
21 arrive at such ensembles.

23 3.3. Self organizing maps (SOM)

25 The SOM algorithm is an unsupervised techni-
26 que which can be used for model-independent
27 exploration of data by finding cluster patterns in
28 data. The idea of SOM was first introduced and
29 developed by Kohonen in early 1980s (hence called
30 Kohonen map, as well). The algorithm maps
31 multidimensional feature space onto, usually, a
32 two-dimensional space with a lattice of nodes.
33 Each node is associated with a vector of weight \mathbf{w}
34 of dimensionality \mathbf{d} of the original space. An input
35 vector is compared to all the weight vectors and
36 assigned to the node that best matches the input.

37 3.4. Support vector machines (SVM)

39 The SVM algorithm is a fairly new one. The
40 main idea is to map the feature space into a space
41 of sufficiently high dimensions ($f: \mathcal{R}^d \rightarrow \mathcal{R}^N; N \gg d$)
42 so that the optimal discriminating boundary
43 between classes is a hyperplane and hence, can
44 be found using linear methods. Given the feature
45 vector \mathbf{x} , the optimal hyperplane is $\mathbf{w} \cdot \mathbf{x} + b$ where
46 \mathbf{w} is the unit vector normal to the hyperplane and
47 $|b|$ is the distance of the plane from the origin.

For more details on the SVM method see 49
contribution from Vaiciulis [8]. 51

53 3.5. Multivariate analysis issues

The important issues to pay attention to in 55
performing a multivariate analysis are the follow- 57
ing:

- choosing a set of variables without losing 59
information, 61
- choosing the right method for the problem,
which in many cases, has to be done by trying 63
out a few methods, 65
- controlling model complexity, i.e., keeping the
number of free parameters in the multivariate 67
model small compared to the sample size, 69
- testing convergence of training in stochastic
optimization algorithms, i.e., to have a good 71
criteria to know when the training is optimal
and cannot be improved further, 73
- validating the learning or modeling, i.e., quan-
tifying the correctness of modeling or goodness 75
of learning, especially given a limited sample, 77
- computational efficiency of the method and/or
algorithm—it is important that the algorithm is 79
computationally efficient so that the analysis
can be repeated for many scenarios to ensure 81
the robustness of the results.

83 4. Applications and prospects

The key factors responsible for the sweeping 85
success of NN algorithms for multivariate analysis 87
are their power, ease of use and many successful 89
applications in HEP. To cite a few examples from 91
Run I Tevatron physics—(1) the top quark
discovery at $D\bar{O}$ benefited from comparisons of 93
conventional analysis with results from NN
analysis [9], (2) precision measurements of the 95
top quark mass at $D\bar{O}$ in lepton + jets and dilepton
channels where the advanced methods helped
reduce the statistical uncertainties by a factor of
two, (3) top quark study in all-jets decay mode and
searches for single top production at $D\bar{O}$ and
CDF, (4) world’s best limit on first generation
scalar leptoquark mass obtained by $D\bar{O}$. There are

many spectacular applications of multivariate methods at LEP and HERA experiments. Some example applications and prospects have been presented in other talks at this workshop [10].

In 1990, I believed that multivariate methods would provide huge gains in top quark searches. We employed multivariate methods, at DØ, particularly NN, to optimize signal selection cuts that helped in top quark physics studies from discovery to precision measurements [11]. Using advanced multivariate and Bayesian methods, the DØ collaboration measured the top quark mass to be $173.6 \pm 5.6 \pm 6.0$ GeV in the lepton + jets channel with a better than expected statistical precision of 5.6 GeV. This extraordinary feat in Run I of precision top quark mass measurement has now been surpassed by exploiting probabilistic information for each event in the matrix element method [12] using the same Run I sample. The comparisons of discrimination between signal and background are shown in Fig. 6. The new measurement yields a top mass of 179.9 GeV with a statistical uncertainty of 3.6 GeV. Run II, with an expected yield of the order of 500 b-tagged $t\bar{t}$ events in lepton + jets final state alone per fb^{-1}

recorded, ushers in an era of a variety of precision measurements in top quark physics.

Topping the list of interesting searches in Run II is that for the Higgs boson. The Higgs mechanism is one vital piece of the standard model that still awaits experimental evidence. Therefore, the Higgs boson would be the most sought after particle in Run II. The discovery of an SM-like Higgs boson will lend credence to the popular theories of the origin of mass. The Tevatron Run II Higgs working group explored the discovery reach for the Higgs boson and the results are shown in Fig. 7. The details of the analysis are described in published papers and the working group report [13]. There are valid and intriguing reasons for the prevailing optimism that the Higgs boson and Supersymmetry may be around the corner. The most favored Higgs boson mass from constraints from precision measurements is in the neighborhood of 100 GeV. In most SUSY models, the Higgs mass is below 150 GeV. The Tevatron, although, has good prospects for discovering a low-mass Higgs boson, it is not going to be easy. It is important to emphasize, however, that the discovery reach at a given mass requires half the integrated luminosity if multivariate methods are adopted instead of conventional univariate methods.

Searches for signatures from new physics beyond the Standard Model such as leptoquark production, supersymmetry or technicolor, are also employing multivariate methods in various stages of Run II data analysis. Advanced multi-

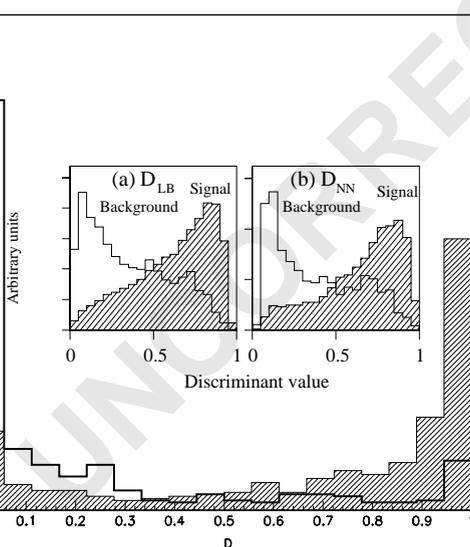


Fig. 6. Likelihood discriminant distributions for signal (hatched histograms) and background events in $t\bar{t} \rightarrow$ lepton + jets channel using the new matrix element method [12]. The inset shows results from earlier analyses using a multivariate likelihood method (left) and NN (right).

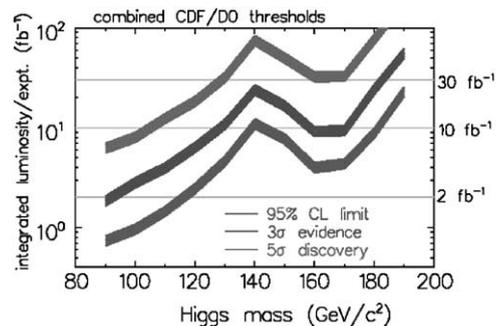


Fig. 7. The required integrated luminosity for 5σ , 3σ observation or 95% C.L. exclusion of the SM Higgs boson in Run II. For details of the analysis see Ref. [13].

1 variate and statistical techniques [14] form a
 3 powerful combination that enable optimal use of
 5 data, consistent treatment of uncertainties and
 7 meaningful model comparisons.

5. Summary

9 Run II is well underway at Fermilab. Early
 11 physics results from the upgraded CDF and DØ
 13 experiments promise an exciting physics program
 15 in the years ahead. A new era of precision
 17 measurements in standard model physics and of
 19 exciting opportunities to discover the agent(s) of
 21 electroweak symmetry breaking and new physics
 23 beyond the standard model has commenced. There
 25 are strong theoretical motivations for new dis-
 27 coveries and valid reasons for the prevailing
 29 optimism. The multivariate methods will provide
 31 sensitivity to new particles with masses beyond the
 33 reach of conventional methods of analysis based
 35 on univariate cuts. Advanced statistical methods
 adopting a fully probabilistic approach will enable
 better precision measurements and better explora-
 tions of model parameters. In short, the use of
 advanced multivariate and statistical techniques
 will enable new discoveries and produce results
 with better precision, robustness and clarity.

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